

Strategies of white-box testing to drive test case design

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Strategies

- Code coverage
- Test Driven Development
- Control Flow Diagrams
 - Path coverage

Code coverage

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Coverage

How thoroughly a test suite exercises a program

Example

```
1 int foo (int a, int b, int c, int d, float e) {
2     if (a == 0) {
3         return 0;
4     }
5     int x = 0;
6     if ((a==b) || ((c == d) && bug(a) )) {
7         x=1;
8     }
9     e = 1/x;
10    return e;
11 }
```

bug(): if a=1 it returns true
and false if a!=1.

Coverage

- Coverage is a measure of the completeness of the set of test cases
 - Method coverage
 - Statement coverage
 - Branch coverage
 - Condition coverage

Method coverage

- Measure: *percentage of methods that have been executed at least once by test cases*
- Test cases should exercise 100% of the methods
- It is irresponsible to deliver non-tested methods
 - Testers need to ensure 100% method coverage

TC1

There is only one method

```
int foo (int a, int b, int c, int d, float e)
```

for $a=0$ `foo` returns 0 no matter the values of the other parameters

calling `foo` with input (0,0,0,0,0) we attain 100% method coverage in our example

```
1 int foo (int a, int b, int c, int d, float e) {
2     if (a == 0) {
3         return 0;
4     }
5     int x = 0;
6     if ((a==b) || ((c == d) && bug(a) )) {
7         x=1;
8     }
9     e = 1/x;
10    return e;
11 }
```

`bug()`: if $a=1$ it returns true
and false if $a!=1$.

Statement coverage

- Measure: *percentage of statements that have been executed by test cases*
 - Achieve 100% statement coverage: cover statements with test cases

Statement coverage

Check coverage of TC1 first:
executed statements on lines 1-4
only out of 11 lines of code

Statement coverage: ~36%
(4/11) with TC1

```
1 int foo (int a, int b, int c, int d, float e) {  
2     if (a == 0) {  
3         return 0;  
4     }  
5     int x = 0;  
6     if ((a==b) || ((c == d) && bug(a) )) {  
7         x=1;  
8     }  
9     e = 1/x;  
10    return e;  
11 }
```

bug(): if a=1 it returns true
and false if a!=1..

We need another test case!

Reach the execution of line 5 → a!=0

TC2

- TC2(1, 1, 1, 1,1), expected return value = 1.
- executes statements on lines 5-11
- **100% statement coverage obtained!**

Branch Coverage

- Measure: *percentage of the decision points evaluated as both true and false in test cases*
 - Achieve 100% branch coverage: cover all branches as both true and false with test cases

Branch Coverage

Two decision points:

one at line 2 and the other at line 6

```
if (a == 0) {}
```

```
if ((a==b) OR ((c == d) AND bug(a))) {}
```

```
1 int foo (int a, int b, int c, int d, float e) {  
2     if (a == 0) {  
3         return 0;  
4     }  
5     int x = 0;  
6     if ((a==b) || ((c == d) && bug(a) )) {  
7         x=1;  
8     }  
9     e = 1/x;  
10    return e;  
11 }
```

bug(): if a=1 it returns true
and false if a!=1..

Branch Coverage

- For decision/branch coverage, we evaluate an entire Boolean expression of the condition as one true-or-false predicate

Branch Coverage

Line #	Predicate	True	False
3	(a == 0)	TC1(0, 0, 0, 0, 0) return 0	TC2(1, 1, 1, 1, 1) return 1
7	((a==b) OR ((c == d) AND bug(a)))	TC2(1, 1, 1, 1, 1) return 1	

```
1 int foo (int a, int b, int c, int d, float e) {
2     if (a == 0) {
3         return 0;
4     }
5     int x = 0;
6     if ((a==b) || ((c == d) && bug(a) )) {
7         x=1;
8     }
9     e = 1/x;
10    return e;
11 }
```

bug(): if a=1 it returns true
and false if a!=1.

TC3

- With TC1 and TC2 we have executed three of the four necessary conditions
 - 75% branch coverage so far



We need another test case!

TC3

- TC3(1, 2, 1, 2, 1) return ??
- **Division by 0** that can cause future failures!
 - That was due to a local variable that we could not control by using strategies based on the analysis of the input space of `foo()`!
 - It depends on how we implemented the method

!((a==b) OR ((c == d) AND bug(a))) = (a!=b) AND ((c != d) OR !bug(a)))

Branch coverage

Line #	Predicate	True	False
3	(a == 0)	TC1(0, 0, 0, 0, 0) return 0	TC2(1, 1, 1, 1, 1) return 1
7	((a==b) OR ((c == d) AND bug(a)))	TC2(1, 1, 1, 1, 1) return 1	TC3(1,2,1,2,1) Division by zero

```
1 int foo (int a, int b, int c, int d, float e) {
2     if (a == 0) {
3         return 0;
4     }
5     int x = 0;
6     if ((a==b) || ((c == d) && bug(a) )) {
7         x=1;
8     }
9     e = 1/x;
10    return e;
11 }
```

TC3 defined for both (a!=b) AND (c != d)

bug(): if a=1 it returns true
and false if a!=1.

Condition Coverage

- Measure: *percentage of Boolean sub-expressions of the program that have been evaluated as both true or false outcome in test cases*
- Condition coverage measures the outcome of each of these sub-expressions independently of each other

Condition Coverage

We need another TC!

Predicate	True	False
(a == 0)	TC1(0, 0, 0, 0, 0) return 0	TC2(1, 1, 1, 1, 1) return 1
(a == b)	TC2(1, 1, 1, 1, 1) return 1	TC3(1,2,1,2,1) Division by zero
(c == d)		TC3(1,2,1,2,1) Division by zero
bug(a)		

```
1 int foo (int a, int b, i
2     if (a == 0) {
3         return 0;
4     }
5     int x = 0;
6     if ((a==b) || ((c == d) && bug(a) )) {
7         x=1;
8     }
9     e = 1/x;
10    return e;
11 }
```

To reach the execution of (c==d) must be a!=b and a!=0

bug(): if a=1 it returns true

and false if a!=1.

TC4

for $a \neq 1$ $\text{bug}(a) = \text{TRUE}$ and return 1, otherwise division by zero. It does not matter for cond. cov whether to enter the if-block!

Predicate	True	False
$(a == 0)$	TC1(0, 0, 0, 0, ...) return 0	TC2(1, 1, 1, 1, 1) return 1
$(a == b)$	TC2(1, 1, 1, 1, ...) return 1	TC3(1,2,1,2,1) Division by zero
$(c == d)$	TC4(1,2,1,1,1) return 1	TC3(1,2,1,2,1) Division by zero
$\text{bug}(a)$		

```

1 int foo (int a, int b, int c, int d, float e) {
2     if (a == 0) {
3         return 0;
4     }
5     int x = 0;
6     if ((a==b) || ((c == d) && bug(a) )) {
7         x=1;
8     }
9     e = 1/x;
10    return e;
11 }

```

$\text{bug}()$: if $a=1$ it returns true
and false if $a \neq 1$.

TC4

We need another TC!

Predicate	True	False
(a == 0)	TC1(0, 0, 0, 0, 0) return 0	TC2(1, 1, 1, 1, 1) return 1
(a == b)	TC2(1, 1, 1, 1, 1) return 1	TC3(1,2,1, 2,1) Division by zero
(c == d)	TC4(1,2,1,1,1) return 1	TC3(1,2,1, 2,1) Division by zero
bug(a)	TC4(1,2,1,1,1) return 1	

```
1 int foo (int a, int b, int c, int d, float e) {
2     if (a == 0) {
3         return 0;
4     }
5     int x = 0;
6     if ((a==b) || ((c == d) && bug(a) )) {
7         x=1;
8     }
9     e = 1/x;
10    return e;
11 }
```

bug(): if a=1 it returns true
and false if a!=1.

TC5

a!=b but a!=1 ->
change only a

Predicate	True	False
(a == 0)	TC1(0,0,0,0,0) return 0	TC2(1,1,1,1,1) return 1
(a == b)	TC2(1,1,1,1,1) return 1	TC3(1,2,1,2,1) Division by zero
(c == d)	TC4(1,2,1,1,1) return 1	TC3(1,2,1,2,1) Division by zero
bug(a)	TC4(1,2,1,1,1) return 1	TC5(3,2,1,1,1) Division by zero

```

1 int foo (int a, int b, int c, int d, float e) {
2     if (a == 0) {
3         return 0;
4     }
5     int x = 0;
6     if ((a==b) || ((c == d) && bug(a) )) {
7         x=1;
8     }
9     e = 1/x;
10    return e;
11 }

```

Again, c == d or c!=d
changes only the return value

bug(): if a=1 it returns true
and false if a!=1.

Note

- Condition coverage does not imply branch coverage!
- Predicate: $A \ \&\& \ B$ - e.g.: $a=b \ \&\& \ c=d$

Condition	Branch	Example
TF, FT	F,F	T(1,1,0,1) and T(1,0,1,1)
TT, FF	T,F	T(1,1,1,1) and T(1,0,1,0)

- Condition coverage does not subsume branch coverage!

but I can build a test suite for condition coverage that contains a test suite for branch coverage

Traceability matrix

Predicate	True	False
(a == 0)	TC1(0,0,0,0,0) return 0	TC2(1,1,1,1,1) return 1
(a == b)	TC2(1,1,1,1,1) return 1	TC3(1,2,1,2,1) Division by zero
(c == d)	TC4(1,2,1,1,1) return 1	TC3(1,2,1,2,1) Division by zero
bug(a)	TC4(1,2,1,1,1) return 1	TC5(3,2,1,1,1) Division by zero

JaCoCo

- It is an Eclipse plug-in
- With Maven: In the node build and sub-node plugins of the POM file include

```
<plugin>
  <groupId>org.jacoco</groupId>
  <artifactId>jacoco-maven-plugin</artifactId>
  <version>0.8.2</version>
  <executions>
    <execution>
      <goals>
        <goal>prepare-agent</goal>
      </goals>
    </execution>
    <!-- attached to Maven test phase -->
    <execution>
      <id>report</id>
      <phase>test</phase>
      <goals>
        <goal>report</goal>
      </goals>
    </execution>
  </executions>
</plugin>
```

Exercise

```
public class Hailstone {
    public static void main(String[] args) {
        int n = 3;
        while (n != 1) {
            if (n % 2 == 0) {
                n = n / 2;
            } else {
                n = 3 * n + 1;
            }
        }
    }
}
```

- Run this class with JaCoCo code coverage highlighting turned on, by choosing Run → Coverage As → Java Application.
- By changing the initial value of n, you can observe how JaCoCo highlights different lines of code differently.

Exercise

```
public class Hailstone {
    public static void main(String[] args) {
        int n = ?;
        while (n != 1) {
            if (n % 2 == 0) {
                n = n / 2;
            } else {
                n = 3 * n + 1;
            }
        }
    }
}
```



Executed



Not Executed



**Partially
Executed Branch**

Exercise

When $n=3$ initially, what color is the line $n = n/2$ after execution?

```
public class Hailstone {
    public static void main(String[] args) {
        int n = ?;
        while (n != 1) {
            if (n % 2 == 0) {
                n = n / 2;
            } else {
                n = 3 * n + 1;
            }
        }
    }
}
```



Executed



Not Executed



Partially
Executed Branch

Exercise

When $n=3$ initially, what color is the line $n = n/2$ after execution?

```
public class Hailstone {
    public static void main(String[] args) {
        int n = ?;
        while (n != 1) {
            if (n % 2 == 0) {
                n = n / 2;
            } else {
                n = 3 * n + 1;
            }
        }
    }
}
```



Executed



Not Executed



Partially
Executed Branch

n
3
10
5
16
8
4
2
1

Exercise

When $n=3$ initially, what color is the line $n = n/2$ after execution?



Executed

```
public class Hailstone {
    public static void main(String[] args) {
        int n = ?;
        while (n != 1) {
            if (n % 2 == 0) {
                n = n / 2;
            } else {
                n = 3 * n + 1;
            }
        }
    }
}
```



Executed



Not Executed



Partially Executed Branch

n
3
10
5
16
8
4
2
1

Exercise

When $n=3$ initially, what color is the line $n = n/2$ after execution?



Executed

When $n=16$ initially, what color is the line $n = 3 * n + 1$ after execution?

```
public class Hailstone {
    public static void main(String[] args) {
        int n = ?;
        while (n != 1) {
            if (n % 2 == 0) {
                n = n / 2;
            } else {
                n = 3 * n + 1;
            }
        }
    }
}
```



Executed



Not Executed



Partially Executed Branch

n
3
10
5
16
8
4
2
1

Exercise

When $n=3$ initially, what color is the line $n = n/2$ after execution?



Executed

When $n=16$ initially, what color is the line $n = 3 * n + 1$ after execution?



Not Executed

```
public class Hailstone {  
    public static void main(String[] args) {  
        int n = ?;  
        while (n != 1) {  
            if (n % 2 == 0) {  
                n = n / 2;  
            } else {  
                n = 3 * n + 1;  
            }  
        }  
    }  
}
```



Executed



Not Executed



Partially Executed Branch

n
3
10
5
16
8
4
2
1

Exercise

When $n=3$ initially, what color is the line $n = n/2$ after execution?

Executed

When $n=16$ initially, what color is the line $n = 3 * n + 1$ after execution?

Not Executed

What initial value of n would make the line `while (n != 1)` yellow after execution?

Executed

Not Executed

Partially Executed Branch

```
public class Hailstone {
    public static void main(String[] args) {
        int n = ?;
        while (n != 1) {
            if (n % 2 == 0) {
                n = n / 2;
            } else {
                n = 3 * n + 1;
            }
        }
    }
}
```

n
3
10
5
16
8
4
2
1

Exercise

When $n=3$ initially, what color is the line $n = n/2$ after execution?

Executed

When $n=16$ initially, what color is the line $n = 3 * n + 1$ after execution?

Not Executed

What initial value of n would make the line $\text{while} (n \neq 1)$ yellow after execution?

Partially Executed Branch $n=1$

```
public class Hailstone {
    public static void main(String[] args) {
        int n = ?;
        while (n != 1) {
            if (n % 2 == 0) {
                n = n / 2;
            } else {
                n = 3 * n + 1;
            }
        }
    }
}
```

Executed

Not Executed

Partially Executed Branch

n
3
10
5
16
8
4
2
1

Testing

- Testing is a **dynamic activity**
- It can be done only when the artefacts to be tested are “executable”

Testing as a development technique

- Move forward testing to the earliest possible is one of the practices of agile methods:
 - **Test First in XP**
- Testing has been also used to develop new code:
 - **Test Driven Development**

Test Driven Development (TDD)

- Practice for writing unit tests and production code *concurrently and at a very fine level of granularity*
- Programmers
 - **first write a small portion of a unit test, and**
 - **then they write just enough production code to make that unit test compile and execute**

Test Driven Development (TDD)

- This cycle lasts somewhere between **30 seconds and five minutes**. Rarely does it grow to ten minutes.
- Once a unit test is done, the developer goes on to the next test until they run out of tests for the task they are currently working on

Test Driven Development (TDD)

- Use compilation and execution to drive development

Example - TDD in Java

- Specification:
TextFormatter: it takes arbitrary strings and horizontally centers them in a line
- Methods:
 - a. *setLineWidth()*
 - b. *center()*
- Parameters
 - a. size b. string

Example - TDD in Java

- Start by creating a test method and instantiate within it an object of the class you want to test

```
First we write the test  
  
public void testCenterLine(){  
    Formatter f = new Formatter();  
}  
does not compile
```

Example - TDD in Java

- Start by creating a test method and instantiate within it an object of the class you want to test

<i>First we write the test</i>
<pre>public void testCenterLine(){ Formatter f = new Formatter(); }</pre> <p>does not compile</p>

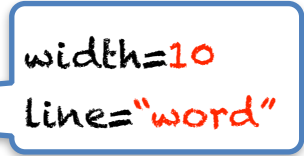
<i>First we write the test</i>	<i>Then we write the production code</i>
<pre>public void testCenterLine(){ Formatter f = new Formatter(); }</pre> <p>does not compile</p>	<pre>class Formatter{ }</pre> <p>compiles and passes</p>

Example - TDD in Java

- Select one method to develop 
- Choose input representative values to test it

```
public void testCenterLine(){
    Formatter f = new Formatter();
    f.setLineWidth(10);
    assertEquals(" word ", f.center("word"));
}

does not compile
```



width=10
line="word"

```
public void testCenter(){
    Formatter f = new Formatter();
    f.setLineWidth(10);
    assertEquals(" word ",f.center("word"));
}
```

does not compile

```
public class Formatter {

    public void setLineWidth(int width) { }

    public String center(String word){
        return "";
    }
}
```

compiles and fails

padding

term

padding

- Develop the method in a simple way to avoid it fails; thinking of the parameters' values you have chosen; first attempt

```
public void testCenter(){
    Formatter f = new Formatter();
    f.setLineWidth(10);
    assertEquals(" word ",f.center("word"));
}
```

```
import java.util.Arrays;

public class Formatter {
    private int width;
    private char spaces[];

    public void setLineWidth(int width) {
        this.width = width;
        spaces = new char[width];
        Arrays.fill(spaces, ' ');
    }

    public String center(String word){
        StringBuffer b = new StringBuffer();
        int padding = width/2 - word.length();
        b.append(spaces, 0, padding);
        b.append(word);
        b.append(spaces, 0, padding);
        return b.toString();
    }
}
```

compiles and unexpectedly fails

Example - TDD in Java

- Re-thinking of the logic

```
public void testCenter(){
    Formatter f = new Formatter();
    f.setLineWidth(10);
    assertEquals(" word ",f.center("word"));
}
```

/ as before*/*

```
public String center(String word){
    StringBuffer b = new StringBuffer();
    //int padding = width/2 - word.length();
    int padding = (width - word.length())/2;
    b.append(spaces, 0, padding);
    b.append(word);
    b.append(spaces, 0, padding);
    return b.toString();
}
```

compiles and passes

padding

term

padding

Example - TDD in Java

- Changed parameter value into “hello”

```
public void testCenterLine() {
    Formatter f = new Formatter();
    f.setLineWidth(10);
    assertEquals(" word ", f.center("word"));
}

public void testOddCenterLine() {
    Formatter f = new Formatter();
    f.setLineWidth(10);
    assertEquals(" hello ", f.center("hello"));
}
compiles and fails
```


Exercise

- How many test cases?
- Let's reason using category partition testing!

How many tests w. brute force?

width	term.length
odd	odd
even	even

How many tests w. brute force?

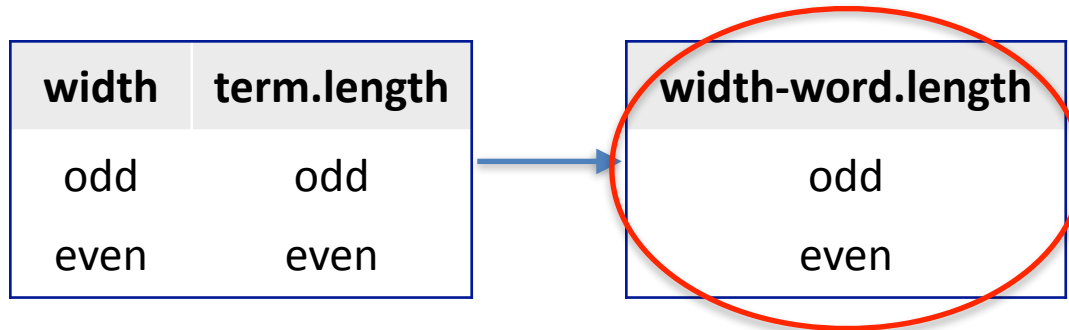
- One-parameter problem!

width	term.length
odd	odd
even	even

- $\text{padding} = (\text{width} - \text{word.length}) / 2$

How many tests w. brute force?

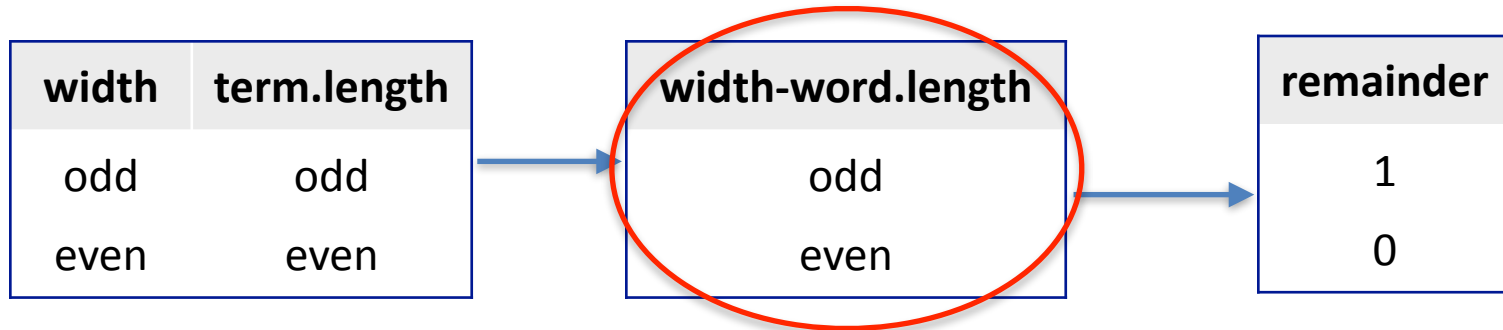
- One-parameter problem!



- $\text{padding} = (\text{width} - \text{word.length}) / 2$

How many tests w. brute force?

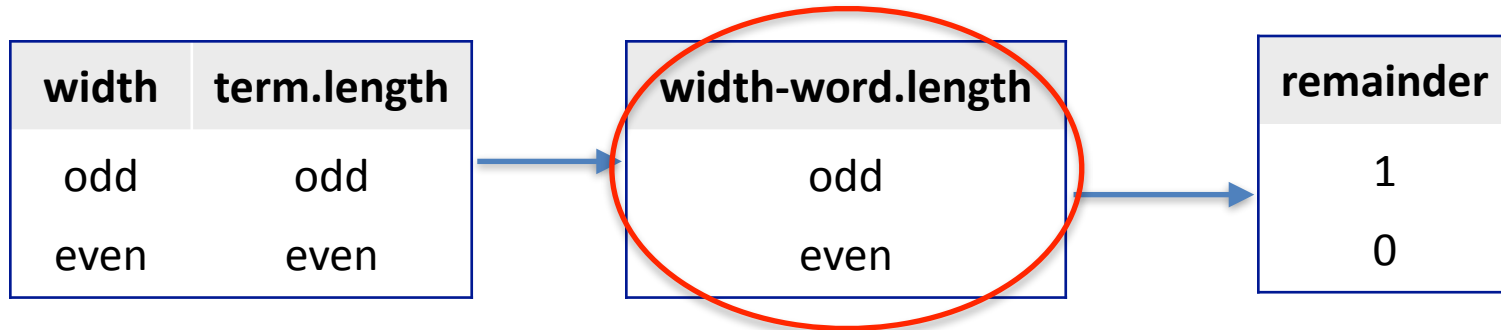
- One-parameter problem!



- $\text{padding} = (\text{width} - \text{word.length}) / 2$
- $\text{remainder} = \text{padding} \% 2$

How many tests w. brute force?

- One-parameter problem!



- $\text{padding} = (\text{width} - \text{word.length}) / 2$
- $\text{remainder} = \text{padding} \% 2$

padding

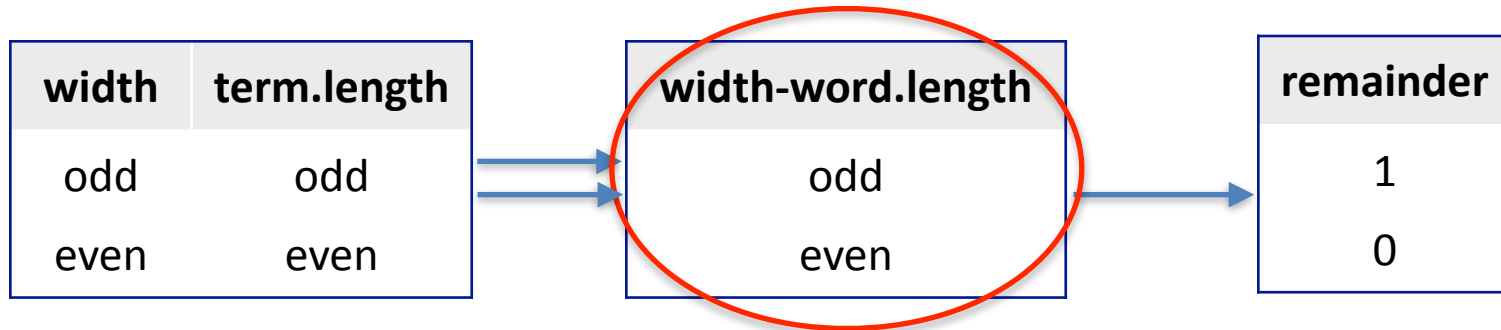
term

padding

remainder

How many tests w. brute force?

- One-parameter problem!



- $\text{padding} = (\text{width} - \text{word.length}) / 2$
- $\text{remainder} = \text{padding} \% 2$

padding

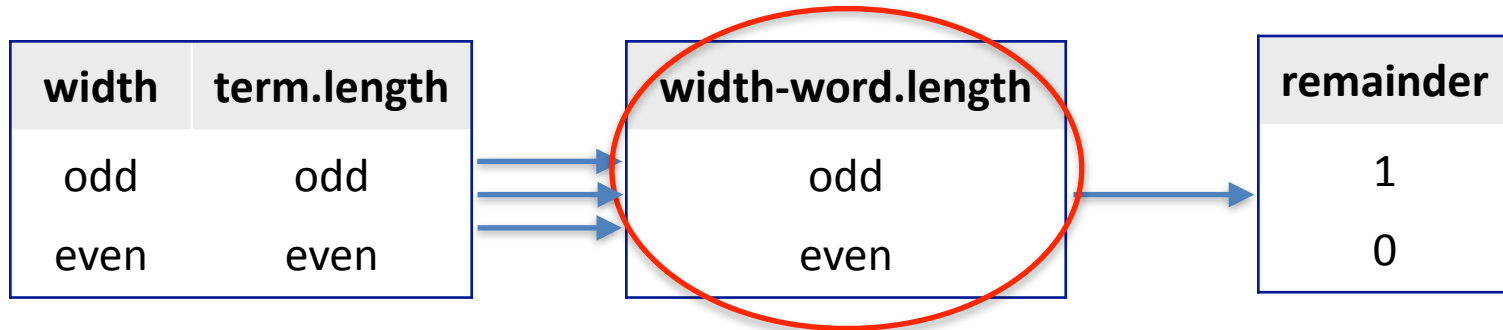
term

padding

remainder

How many tests w. brute force?

- One-parameter problem!



- $\text{padding} = (\text{width} - \text{word.length}) / 2$
- $\text{remainder} = \text{padding} \% 2$

padding

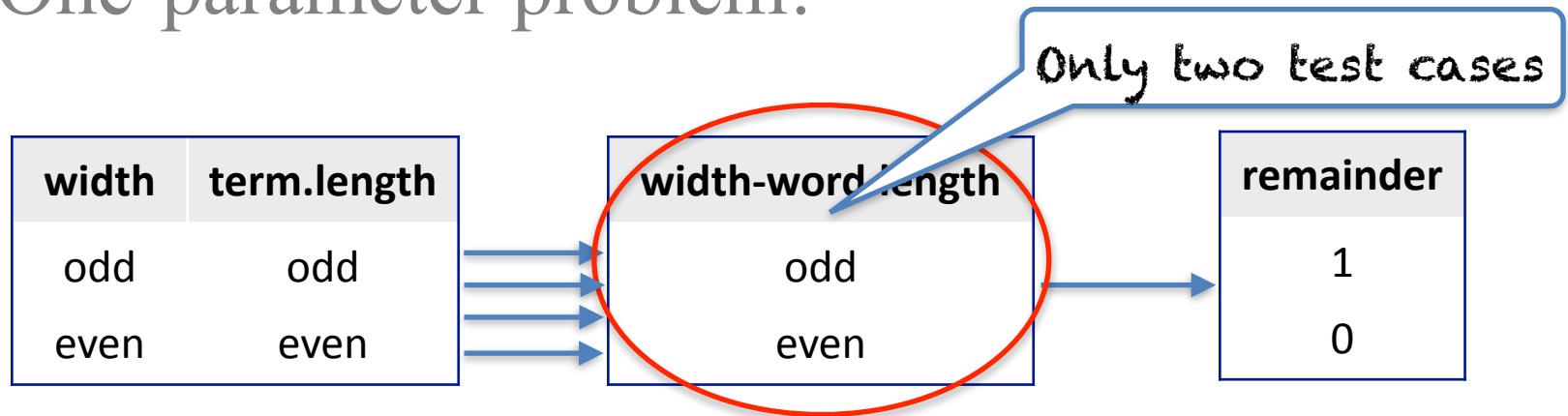
term

padding

remainder

How many tests w. brute force?

- One-parameter problem!



- $\text{padding} = (\text{width} - \text{word.length}) / 2$
- $\text{remainder} = \text{padding} \% 2$

padding

term

padding

remainder

Test cases

- **width-string.length**
- $\text{odd} = 2k+1$, $\text{even} = 2k$ with $k > 0$
- $k \neq r$
 - $\text{odd} - \text{odd} = 2(k-r) : \text{even}$
 - $\text{even} - \text{even} = 2(k-r) : \text{even}$
 - $\text{even} - \text{odd}$ or $\text{odd} - \text{even} = 2(k-r) \pm 1 : \text{odd}$
- **In addition**
 - $\text{padding} = 0$ or
 - $\text{string.length} = \text{width} = 0$
 - $\text{padding} < 0$

Test cases

- **width-string.length**

- odd = $2k+1$, even = $2k$ with $k>0$

- $k \neq r$

- odd - odd = $2(k-r)$: even

- even - even = $2(k-r)$: even

- even - odd or odd - even = $2(k-r) \pm 1$: odd

- **In addition**

- padding=0 or

- string.length=width=0

- padding<0

Only two test cases

other default test cases

Combinatorial partition testing

width	word.length
even [Property: evenL]	even [Property: evenS] if([evenL])
odd [Property: oddL]	odd [Property: oddS] if([evenL])
0[single]	>word.length if([evenL]) [error]
	=word.length if([evenL])
	<word.length if([evenL])
	0 [single]

- line = 10
- string = “word” and “hello”
- string= “circumstances”
- string = “challenges”
- width = 0
- word.length=0

width=0 is used with 0
for word.length; cannot
be used anywhere else

Solution

```
public String center(String term) {  
    int remainder = 0;  
    StringBuffer b = new StringBuffer();  
    int padding = (width - term.length()) / 2;  
    remainder = term.length() % 2;  
    b.append(spaces, 0, padding);  
    b.append(term);  
    b.append(spaces, 0, padding + remainder);  
    return b.toString(); }  
compiles and passes
```

Models of program execution

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A model of program execution

A model of program execution is a representation of a software execution simpler but that preserves some key attributes of it

- This representation will help to define a strategy for testing

State Space

- Representation of the program execution with a sequence of states and transitions
- **The state space is a set of possible states and transitions**
- For almost all programs, the state space is potentially infinite

Abstraction function

- The states are represented in the space by an abstraction function
- The abstraction function might suppress some states to create the finite model

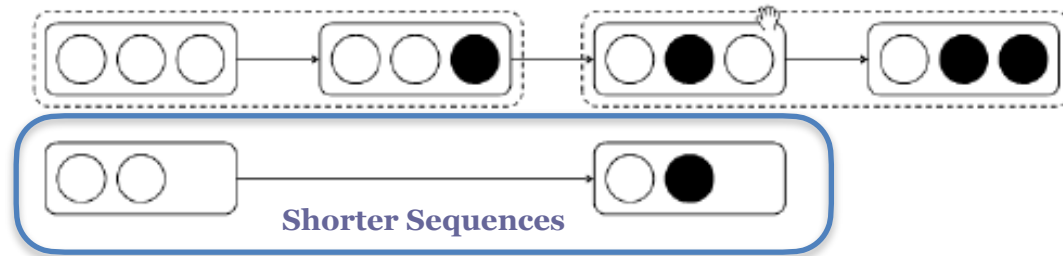
Effects of abstraction

- **Coarsening:** execution sequences are collapsed into shorter sequences
- **Non determinism:** states are merged

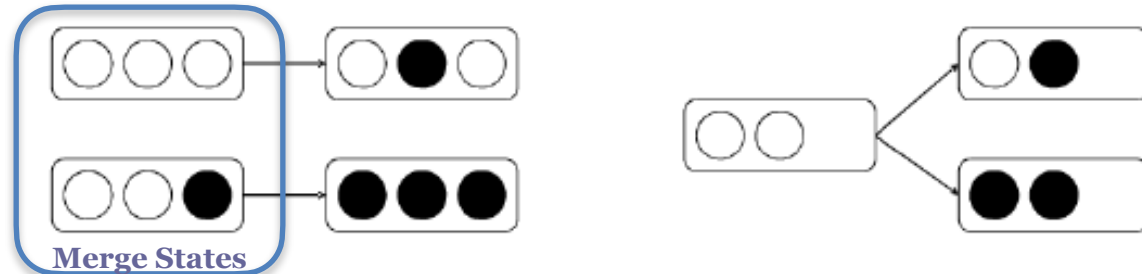
Effects of abstraction

For example, assume the third state is neglected

1. Coarsening of execution model



2. Introduction of nondeterminism



Pezze & Young



Example: Control Flow Graphs

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Control Flow Graphs

- It is a directed graph
 - **Node (state)**= portion of code
 - **Directed Edge** = flow of execution between two portions

Control flow structure

- The control flow structure is modeled with **direct graphs**
- A direct graph is a set of arcs and nodes with one defined direction
 - A set of statements without branch corresponds to a **node**, a flow of control from a statement to another to an arch
 - There is a **start node** and an **end node**
 - Each other node resides on a path between these two
 - Each node has an **in-degree** and an **out degree**
 - The start/end node has zero in - degree/out - degree

Control flow structure

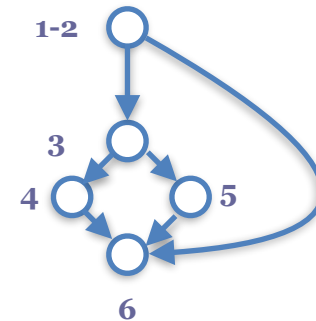
- A program is transformed in a direct graph called **control flow graph** that depicts the **execution control** of a program and the instruction to be executed
- It is a **static representation** of the program
- It makes visible the control structure
- Out-degree = 1 defines **procedural nodes** all the other nodes are called **predicate nodes**

Control Flow Graphs

- CFG keeps information of instructions to be executed and **ignores values of variables or data structures**
- Example of **non deterministic abstraction**

```
1 boolean z = FALSE;  
2 if(z && y<=2){  
3   if(z){  
4     y++;  
5   }else{y--;}  
6 }
```

It does not depend on the value of z or the data structures in the branches



- CFG also models the non- feasible path!

CFG to design test cases

- We can use this information to design test cases
- Let's see how to do it ...
 - First let's introduce the **McCabe complexity** measure which will help us to limit the number of test cases

McCabe Cyclomatic Complexity

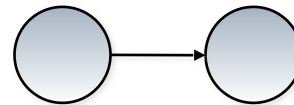
- Map codes to flow graphs
- Map flow graphs to numbers

CC definition

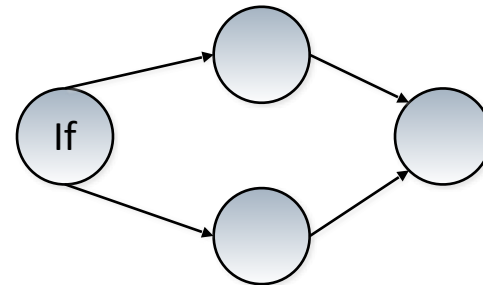
- $CC = \#$ of connected regions
- $CC = \#$ branches + 1
- $CC = \#$ elements in a base
- $CC = \#$ decision point + 1
- $CC = \#$ arcs - $\#$ nodes + 2 (Euler characteristic)

Examples

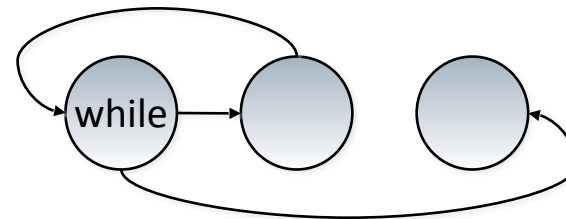
- Sequence



- If ... then ... else



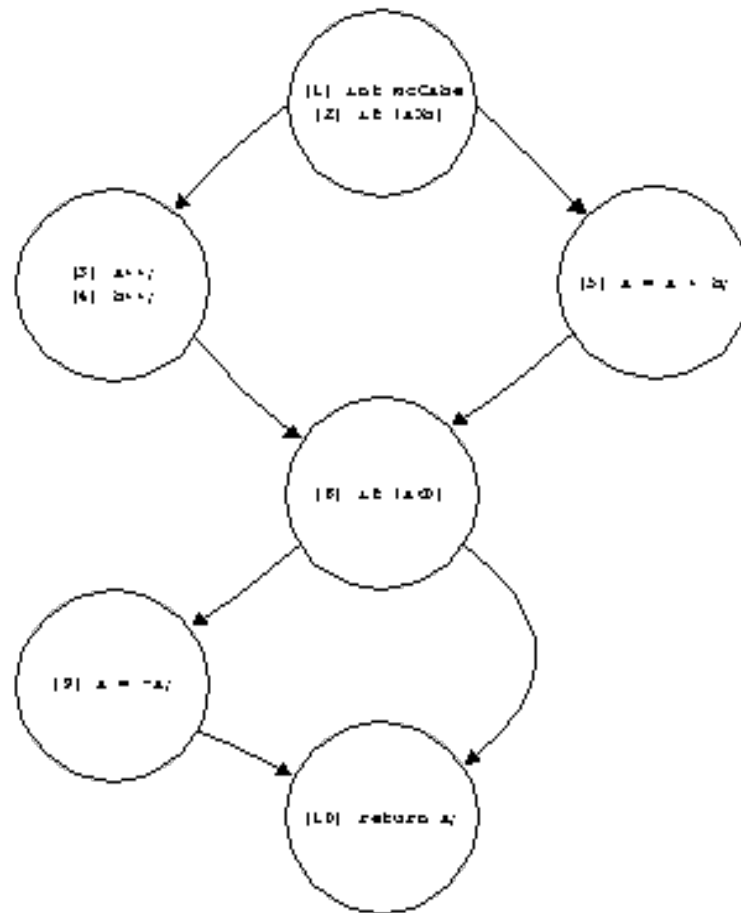
- While



Example

```
[1]  int mcCabe(int a, int b) {  
[2]      if (a >b) {  
[3]          a++;  
[4]          b--;  
[5]      } else {  
[6]          a=a + b;  
[7]      }  
[8]      if (a < 0) a=-a;  
[9]      return a;  
[10] }
```

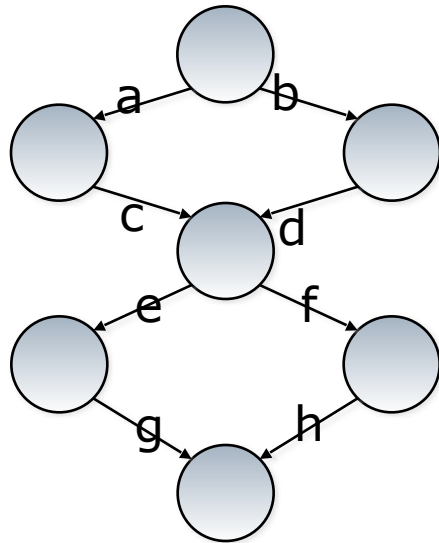
Exercise



CC as independent paths

- A **complete path** is a path starting from the starting node and ending to the end node
- One complete path is **linearly independent** from the others if it does not exist a combination of the other complete paths to which is equal
- How to combine paths ...

Describe the base of the following graph



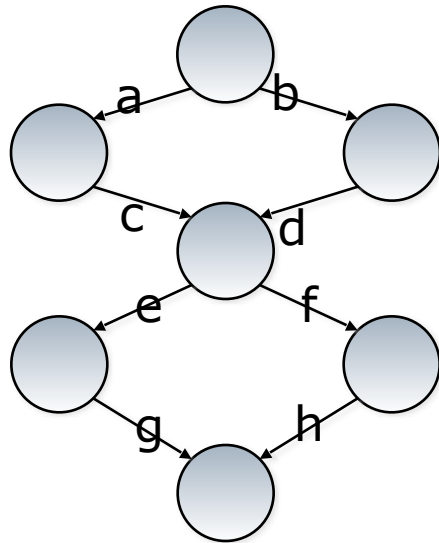
Rule to combine paths:
The arcs go from top to bottom

-a : is the arc in the opposite direction

-aceg: is the opposite complete path of aceg

ab: is first a and then b

Describe the base of the following graph



Rule to combine paths:

The arcs go from top to bottom

-a : is the arc in the opposite direction

-aceg: is the opposite complete path of aceg

ab: is first a and then b

Complete paths:

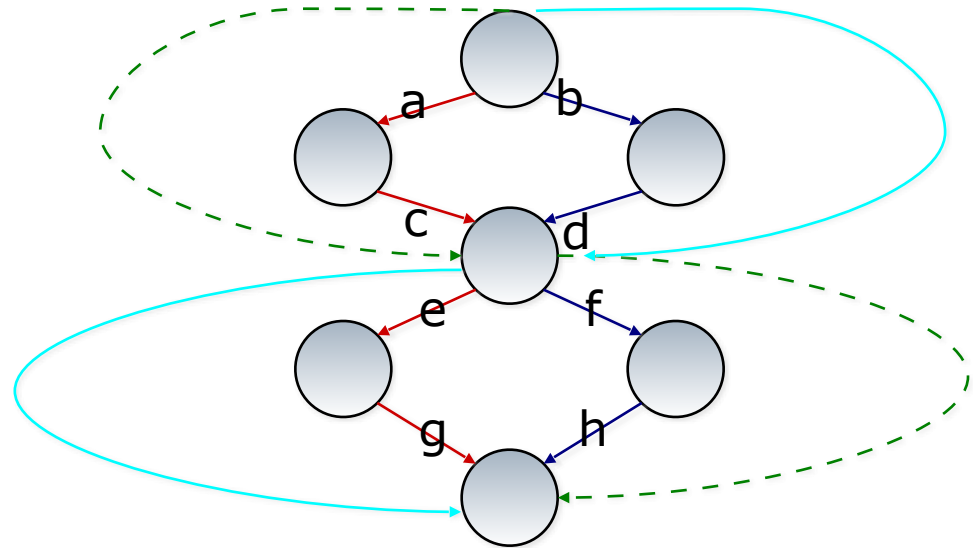
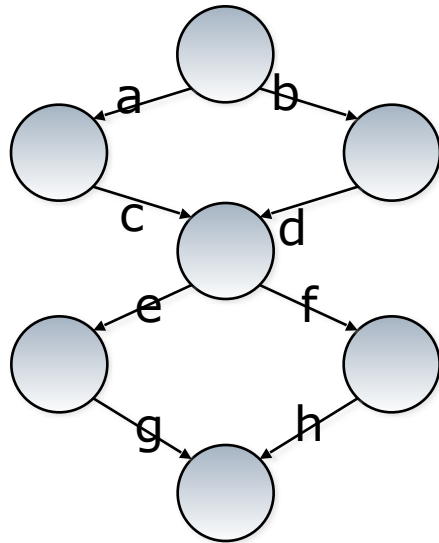
aceg

bdfh

bdeg

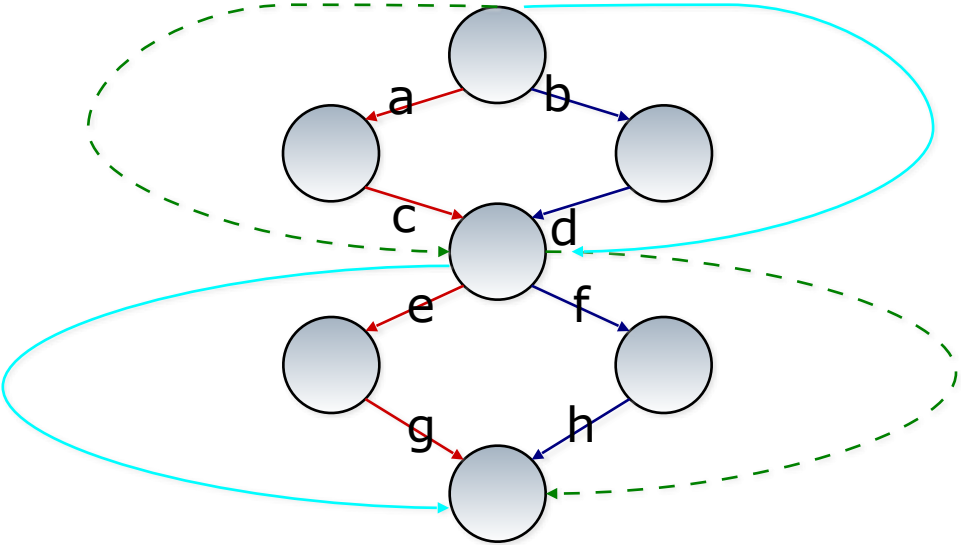
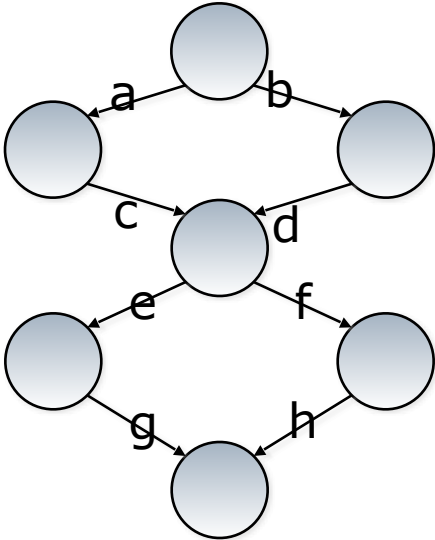
acfh

Describe the base of the following graph

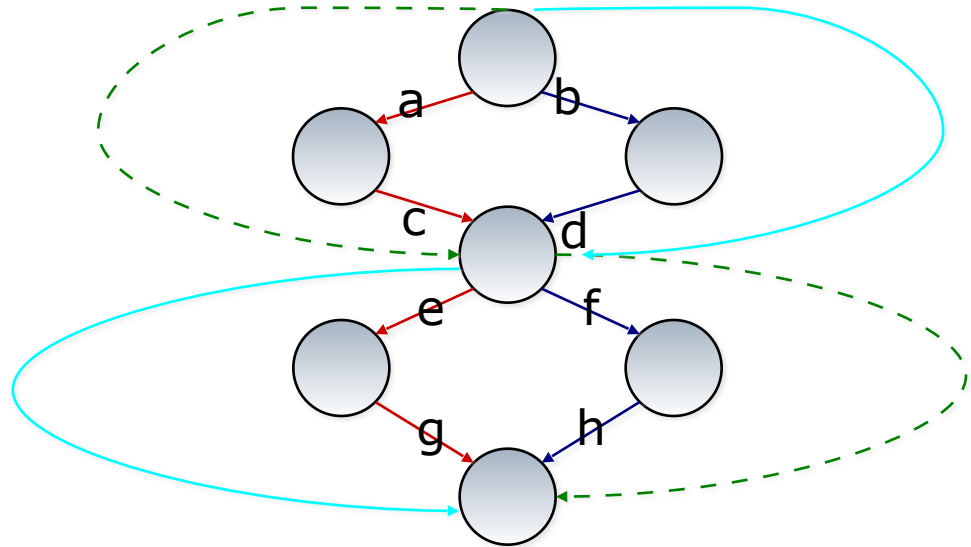
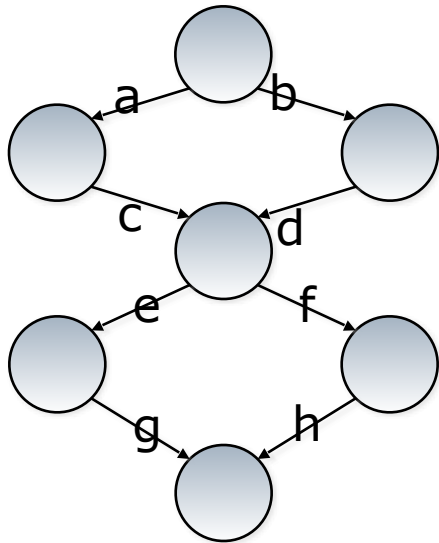


The path $acfh = aceg - bdeg + bdfh$

Describe the base of the following graph



Describe the base of the following graph



The path $acfh = aceg - bdeg + bdfh$

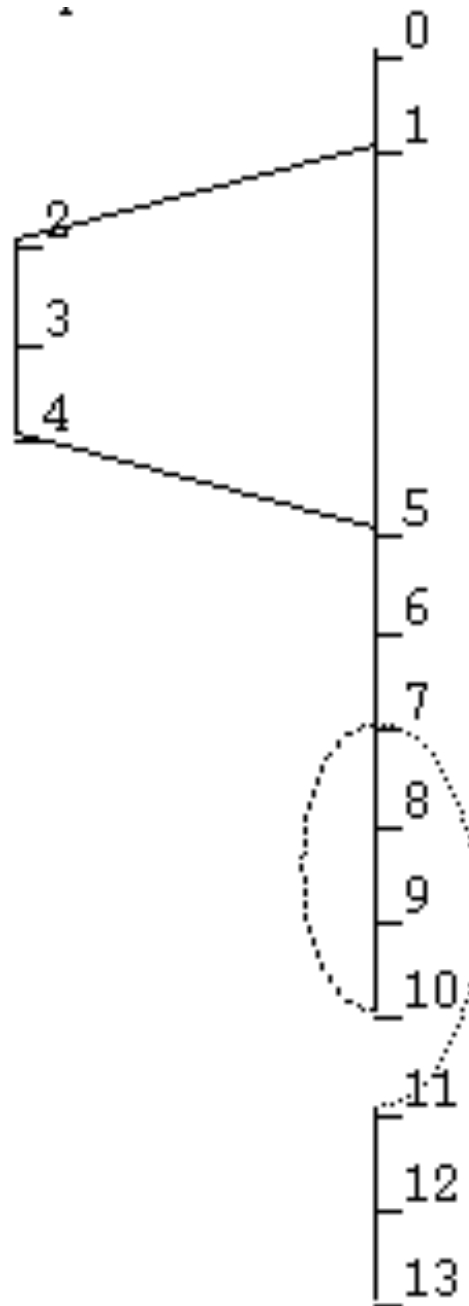
Base

- Minimum number of independent complete paths

Draw the flow graph and Compute the CC

```
2      A0      euclid(int m, int n)
3      A0      /* Assuming m and n both greater than 0,
4      A0      * return their greatest common divisor.
5      A0      * Enforce m >= n for efficiency.
6      A0      */
7      A0      int r;
8      A1      if (n > m) {
9      A2          r = m;
10     A3          m = n;
11     A4          n = r;
12     A5      }
13     A6      r = m % n;      /* m modulo n */
14     A7      while (r != 0) {
15     A8          m = n;
16     A9          n = r;
17     A10         r = m % n;   /* m modulo n */
18     A11     }
19     A12     return n;
20     A13     }
```

Result



Use CFG in testing

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Path coverage

- Path coverage is every possible path through the program taken by some test case
- McCabe complexity is used to determine how many complete execution paths (i.e. test cases designed from them) a tester need to consider
- As with code coverage this is a measure that approximates completeness

Statement and Path coverage

- Reformulate statement coverage: Design test cases so that every node lies on at least one complete path
- Path coverage: Design test cases such that every possible arc is executed at least once

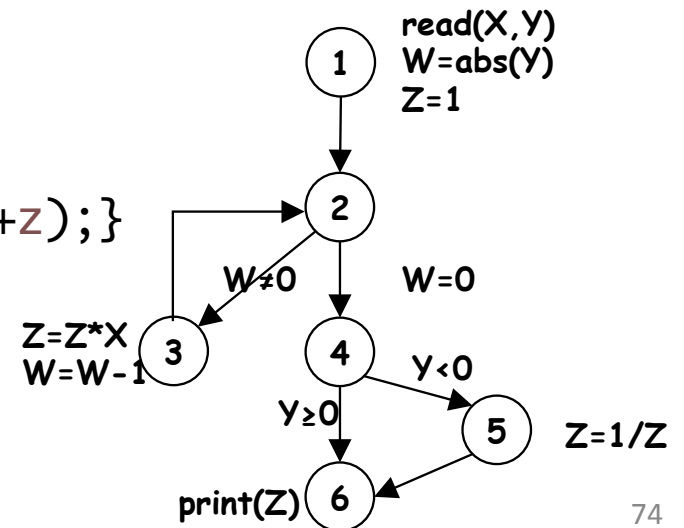
Template for path coverage

- Draw the CFG
- Count the possible independent complete paths
- Create a table with all the possible arcs as column headers
- Create a test case per execution of an arc in an independent path

The power function

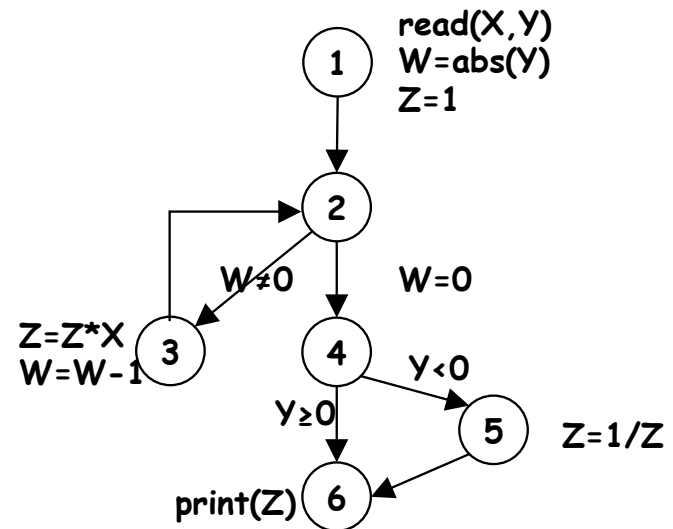
Program computing $Z=X^Y$

```
public class PowerFunction {  
    public static void main(String[] args) {  
        int x = Integer.parseInt(args[0]);  
        int y = Integer.parseInt(args[1]);  
        int w = Math.abs(y);  
        int z = 1;  
  
        while(w!=0){  
            z=z*x;  
            w=w-1;  
        }  
        if(y<0){z=1/z;}  
        System.out.println("result is "+z);  
    }  
}
```



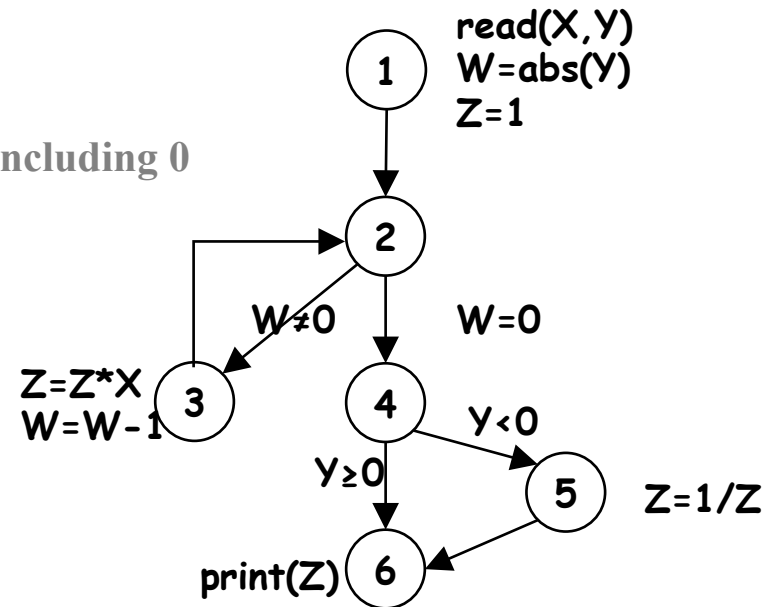
Path coverage

- All arcs are executed in at least one path
 - **Infeasible path**
 - 1 -> 2 -> 4 -> 5 -> 6
 - **As many ways to iterate as values of $\text{abs}(Y)$ including 0**
 - 1 -> 2 -> (3 -> 2)* -> 4 -> 6
 - 1 -> 2 -> (3 -> 2)+ -> 4 -> 5 -> 6
- $w=0,1,-1$ what for the infeasible path?



Issues

- Path coverage (CC=3, 4 complete paths)
 - **Infeasible path**
 - 1 -> 2 -> 4 -> 5 -> 6
 - **As many ways to iterate as values of abs(Y) including 0**
 - 1 -> 2 -> (3 -> 2)* -> 4 -> 6
 - 1 -> 2 -> (3 -> 2)+ -> 4 -> 5 -> 6
- Branch coverage
 - Three test cases:
 - $Y < 0$: 1 -> 2 -> (3 -> 2)+ -> 4 -> 5 -> 6
 - $Y \geq 0$: 1 -> 2 -> (3 -> 2)* -> 4 -> 6
- Statement coverage
 - One test case is enough:
 - $Y < 0$: 1 -> 2 -> (3 -> 2)+ -> 4 -> 5 -> 6



Subsumption

- 100% path coverage subsumes both 100% statement coverage and branch coverage

CFG and issues with coverage

- Some paths are infeasible
- Some edges are hidden
-

Some complete paths may be infeasible

- Infeasible path: a program path that cannot be executed for any input

A input(score)

B if score < 45

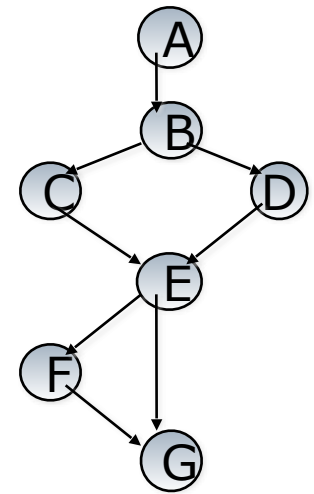
C then print ('fail')

D else print ('pass')

E if score > 70

F then print ('with distinction')

G end



Some complete paths may be infeasible

- Infeasible path: a program path that cannot be executed for any input

A input(score)

B if score < 45

C then print ('fail')

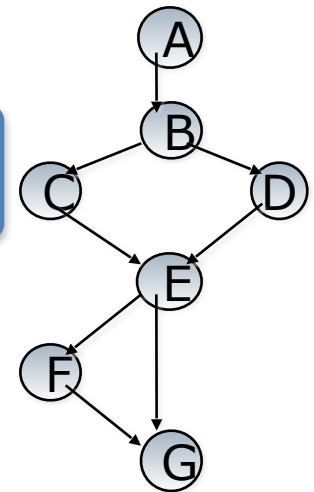
D else print ('pass')

E if score > 70

F then print ('with distinction')

G end

Which path is not feasible

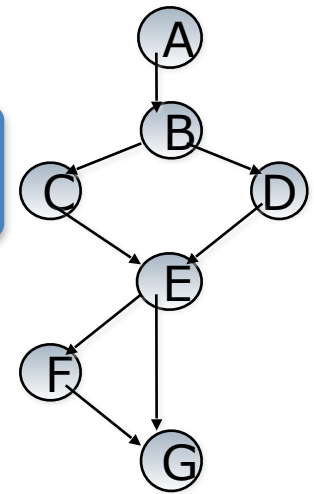


Some complete paths may be infeasible

- Infeasible path: a program path that cannot be executed for any input

```
A input(score)
B if score < 45
C   then print ('fail')
D   else print ('pass')
E if score > 70
F   then print ('with distinction')
G end
```

Which path is not feasible



- The path A-B-C-E-F-G is infeasible and
- It will be never executed
- We create a test case for the non-feasible path: wasting time

Some paths are implicit

```
if x < 0 then
    x := -x;
end if
z := x;
```

The else condition is implicit

```
else
    null;
```

- A test case exercising only $x < 0$ reaches the 100% statement coverage, but it does not prevent a bug to occur if $x \geq 0$
- With CGF we can create a test case also $x \geq 0$. Good!