

DETERMINISTIC FINITE AUTOMATA

29/10/2010
E2.1

EXERCISE 1

give a DFA accepting the following language over the alphabet $\{a, b\}$: the set of all strings such that the second last symbol is b .

EXERCISE 2

give a DFA accepting the following language over the alphabet $\{x, y\}$: the set of strings that either begin or end (or both) with yx .

EXERCISE 3

give a DFA accepting the following language over the alphabet $\{0, 1\}$: the set of strings such that the number of 0's is divisible by five and the number of 1's is divisible by three.

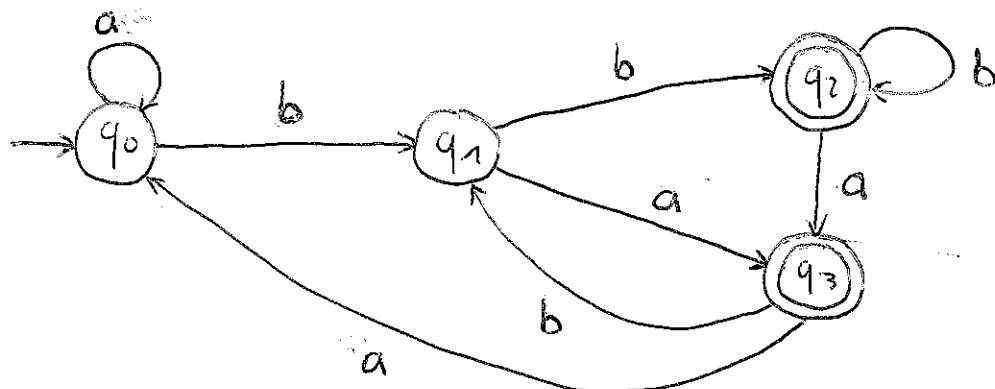
EXERCISE 4

give a DFA accepting the following language over the alphabet $\{a, b, c, d\}$: the set of strings consisting of zero or more a's followed by zero or more b's, followed by zero or more c's.

SOLUTIONS

E2.2

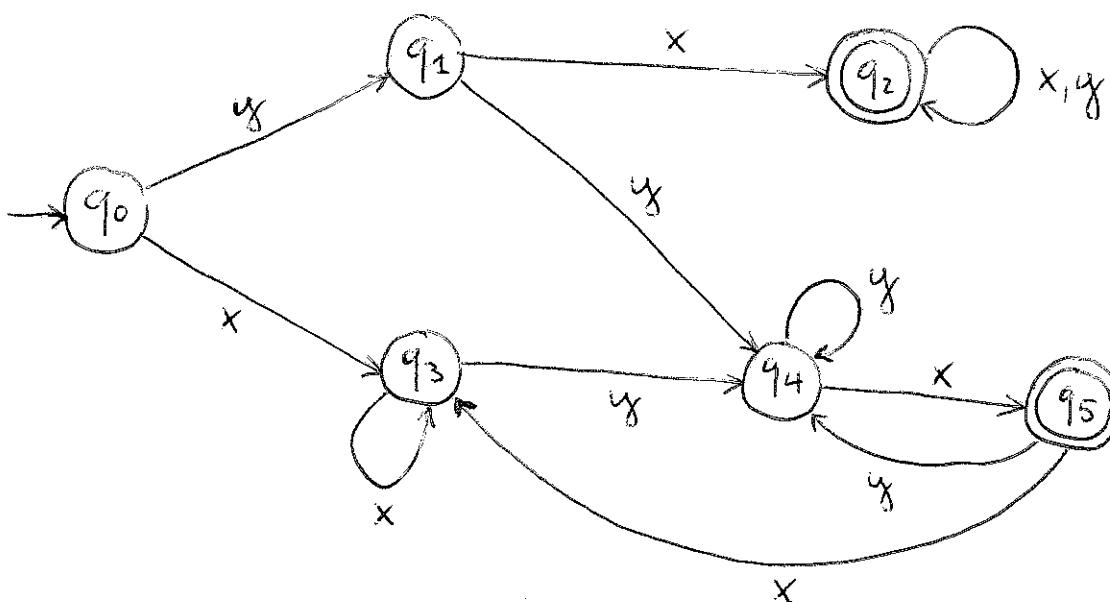
1) The DFA looks as follows:



We show that it accepts bbaaba but not abbbbaaa

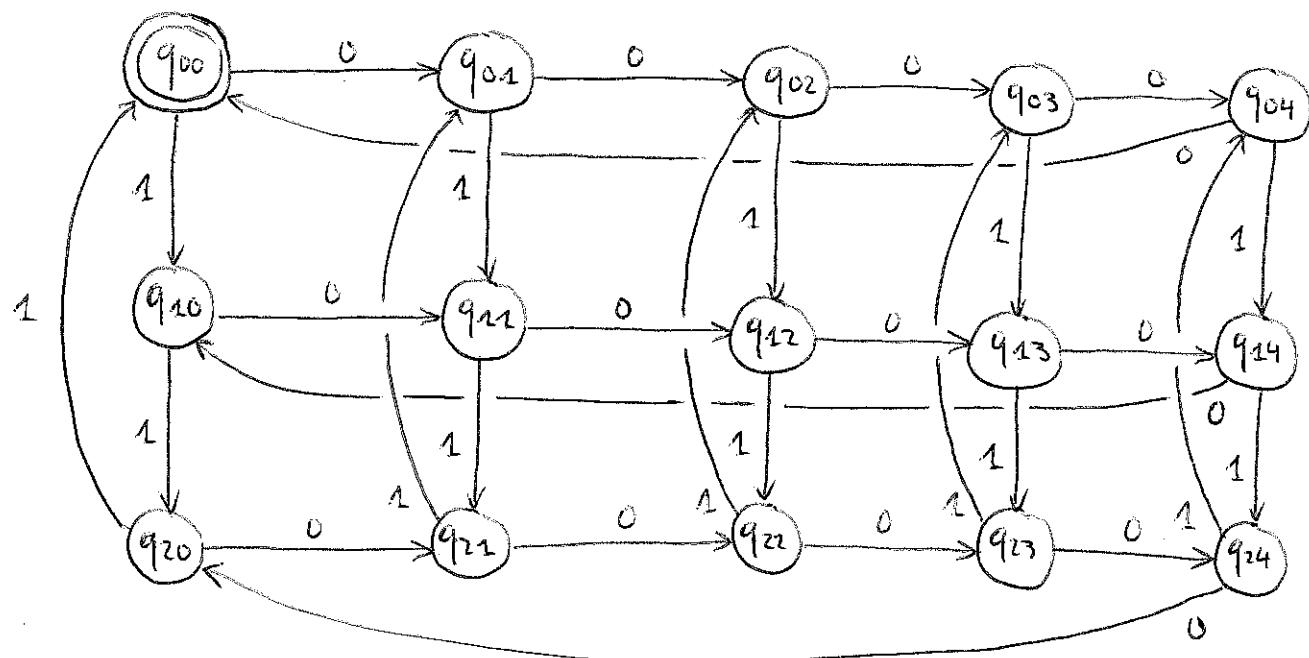
- $(q_0, b) \rightarrow q_1, (q_1, b) \rightarrow q_2, (q_2, a) \rightarrow q_3, (q_3, a) \rightarrow q_0$
 $(q_0, b) \rightarrow q_1, (q_1, a) \rightarrow q_2$ q_2 is a final state
- $(q_0, a) \rightarrow q_0, (q_0, b) \rightarrow q_1, (q_1, b) \rightarrow q_2, (q_2, b) \rightarrow q_2$
 $(q_2, a) \rightarrow q_3, (q_3, a) \rightarrow q_0$ q_0 is not a final state

2) The DFA looks as follows:



3) The DFA looks as follows:

EZ.3



4) The DFA looks as follows:

