# Controlled Aggregate Tree Shaped Questions over Ontologies

Camilo Thorne and Diego Calvanese

KRDB Centre Free University of Bozen-Bolzano 4, Via della Mostra, 39100 (Italy) {thorne,calvanese}@inf.unibz.it

**Abstract.** Controlled languages (CLs) are ambiguity-free subsets of natural languages such as English offering a good trade-off between the formal rigor of ontology and query languages and the intuitive appeal of natural language. They compositionally map (modulo a *compositional translation*  $\tau(\cdot)$ ) into (or *express*) formal query languages and ontology languages. Modulo compositionality, they inherit the computational properties of such ontology/query languages. In the setting of OBDAS, we are interested in capturing *query answering* and measuring computational complexity w.r.t. the data queried (a.k.a. *data complexity*). In this paper we focus in defining a CL capable of expressing a subset SQL *aggregate queries*, and study its data complexity w.r.t. several ontology languages and extensions of the query language.

#### 1 Introduction

Ontology-based data access systems (OBDASs) have been proposed by the semantic web community as a way of integrating and querying information coming from heterogeneous sources [16]. Such systems have two main components, (*i*) an ontology and (*ii*) a collection of (possibly multiple) databases of which the ontology, typically an OWL ontology (or an ER, UML, etc., conceptual model), provides a unified, common view or interface. OWL ontologies are formally underpinned by description logics (DLs), which are expressive enough to capture conceptual models [3]. Formal queries, in general fragments of SQL (or SPARQL) queries, such as (unions) of conjunctive queries, are formulated w.r.t. the ontology and later rewritten and evaluated (under OWA) over the datasources [6].

Controlled English interfaces to such systems (targeting non-expert users) have been proposed [5, 9] as a trade-off between the English utterances covered by the system and its performance (measured in terms of, e.g., precision, recall and accuracy), following the desiderata laid by [2] for natural language interfaces to databases. Controlled languages (CLs) are ambiguity-free fragments of a natural language. This allows their being symbolically (and, moreover, compositionally) translated, without any loss of information, into OWL assertions and/or queries to be sent to the back-end OBDAS [5]. The ACE (Attempto Controlled English) CL, and its fragment ACE-OWL (that maps into OWL), is perhaps the best known in the literature [9]. However, the kind of constraints and queries support by OBDASs affect their scalability. Answering e.g. selectproject-join SQL queries over OWL ontologies is (at least) worst-case exponential on

the data (**coNP**-hard) [3]. These considerations generalize to the CLs supported by OB-DAS, in the sense that, modulo compositional translations, they inherit (i.e., *express*) the computational properties of the ontology and query languages.

This raises the issue of how to extend the expressivity/coverage of the CLs without blowing up the performance of the OBDAS. In this paper we propose to consider the class of SQL *aggregate queries*, viz., select-project-join queries with GROUP BY and HAVING clauses and aggregation functions such as COUNT, SUM, MIN, AVG, etc., in combination with several ontology languages and declarative fragments of English. CLs that translate into aggregate queries have been mostly proposed for plain database settings [11]. The main contributions of this paper are the following:

- 1. We define an interrogative CL, ATQ-English, that compositionally translates into aggregate tree-shaped queries (ATQs). We also look at how to express several ontology languages (that overlap in expressive power with OWL).
- 2. We consider bare ATQs and extensions (closed under boolean operations and/or equipped with comparisons) together with those ontology languages and study their data complexity. Aggregates do not increase significatively data complexity but syntactic constructs that go beyond selections, joins and projections, do.

## 2 Tree Shaped Aggregate Queries over Ontologies

**Relational Databases.** We assume as given a countably infinite domain  $\Delta := \Delta_O \cup \Delta_V$  partitioned into a domain  $\Delta_O$  of object constants and a domain  $\Delta_V$  of values (containing numbers; in what follows  $\mathbb{Q}$  and its subsets). We call *tuple* any finite sequence  $\bar{c}$  of domain elements. A *database schema*  $\mathbf{R}$  is a finite set of relation names. A *relation name* R is a predicate symbol of arity n (a nonnegative integer). A *database instance* (DB) D of  $\mathbf{R}$  is a pair  $(\Delta, \cdot^D)$  where  $\Delta$  is the domain and  $\cdot^D$  is an *interpretation function* over  $\mathbf{R}$ , that is, a function mapping each relation symbol R of arity n in  $\mathbf{R}$  to a subset  $R^D$  of  $\Delta^n$ , i.e., to a *relation instance*. Observe that databases are basically FO interpretation structures of  $\mathbf{R}$  [1]. The *size* |D| of D is defined as the number of tuples in its relation instances. The set of such tuples is denoted adom(D).

**Conditions.** A *term* t is either a variable (like x, y, ...) or a constant (like c, d, ...). An *atom* is an expression of the form  $R(\bar{t})$ , where R is a relation name of arity n and  $\bar{t}$  is a sequence of n terms. An atom is *ground* when all its terms are constants. A *condition*  $\Phi$  is a (possibly empty) conjunction of FO atoms closed under negation and existential quantification. We define  $\forall \bar{x}\Phi := \neg \exists \bar{x} \neg \Phi, \Phi_1 \lor \Phi_2 := \neg(\neg \Phi_1 \land \neg \Phi_2)$  and  $\Phi_1 \Rightarrow \Phi_2 := \neg \Phi_1 \lor \Phi_2$ . We denote by  $Var(\Phi)$  the set of variables occurring in condition  $\Phi$ , and by  $FV(\Phi)$  its free variables. A condition is called a *sentence* (or also, *boolean*) if it contains no free variables. A condition  $\Phi(x)$  is said to be *tree shaped* if (i) it is an atom A(x), (ii) it is a condition  $\exists yR(x, y)$ , (iii) it is a condition  $\exists y(R(x, y) \land \Phi(y))$ , where  $\Phi(y)$  is tree shaped, or (iv) it is a condition  $\Phi_1(x) \land \Phi_2(x)$  where  $\Phi_1(x)$  and  $\Phi_2(x)$  are tree shaped. The free variables x of  $\Phi(x)$  is called the *root* of  $\Phi$ . **Ontologies and OBDASs.** An *ontology*  $\mathcal{O}$  is formally defined as a set of sentences. Ontologies typically express *constraints* (termed also *axioms* or *assertions*) on the data, viz., they provide the conceptual model of a domain of interest, describing the classes of objects such a domain of interest comprises, their attributes or properties, and their relations. An *ontology language*  $\mathcal{L}$  is a class of constraints, obtained by suitably restricting their syntax. i.e., a fragment of FO with a distinct expressive power [16]. Ontologies provide a single, unified, global view on datasources for accessing data in ontology-based systems. An *ontology-based data access system* (OBDAS) is a pair ( $\mathcal{O}$ , D) where D is a DB and  $\mathcal{O}$  is an ontology.

**Aggregate Queries.** We consider now the following standard SQL *aggregation functions*, viz., **max**, **min**, **count**, **countd**, **sum** and **avg**. In what follows  $\alpha$  will denote an arbitrary aggregation function. Given this, we call an *aggregation term* any expression of the form  $\alpha(y)$ , where y is called an *aggregation variable*. An *aggregate tree-shaped query* (ATQ) over **R** is a query of the form

$$q(x,\alpha(y)) \leftarrow \Phi \tag{1}$$

where q is the *head* relation x is a grouping variable,  $\alpha(y)$  is an aggregation term and  $\Phi := \Phi_1 \wedge R(x, y) \wedge \Phi_2$  with  $\Phi_1$  a condition rooted in  $y, \Phi_2$  a condition rooted in x, R(x, y) an atom,  $\{x, y\} = FV(\Phi)$  and  $y \neq x$ .

The core  $\check{q}$  of an ATQ  $q(x, \alpha(y)) \leftarrow \Phi$  is defined as  $\check{q}(x, y) \leftarrow \Phi$ . Queries with conjunctive bodies but no aggregation terms in their heads are known in the literature as *conjunctive queries* (CQs). If the sequence of head variables is empty, a CQ is said to be *boolean* [1]. In general, different constraints on the syntax of head relations and conditions give way to different classes of queries. A *query language*  $\mathcal{L}$  is any such class.

**Certain Answers and QA.** Aggregation functions in SQL are defined over bags  $\{\cdot\}$ , called *groups*, which are collections of possibly repeated symbolic and numerical values (from  $\Delta$ ), and return a rational number. OBDASs and ontologies, on the other hand, deal with incomplete information, i.e., their DBs D are a partial description of the domain of interest that the ontology "completes" by intuitively characterizing the space of all the DBs D' compatible with D [7]. Naively asking an aggregate query q over each D' may thus yield no meaningful answer: it might return a different group and a different quantity over each D' [7]. To overcome this we (*i*) ask for the tuples satisfying the condition of the query over that group [7]. Finally, the associated query answering problem allows us to study computational properties (i.e., data complexity).

An assignment  $\gamma$  over a condition  $\Phi$  is a function that maps  $Var(\Phi)$  to  $\Delta$  and each constant in  $\Phi$  to itself. Assignments are extended to complex syntactic objects like atoms and conditions in the usual way. An assignment  $\gamma$  is said to satisfy a condition  $\Phi$  over D, denoted  $D, \gamma \models \Phi$ , whenever  $\Phi$  evaluates to true in D under  $\gamma$ , i.e., the standard notion of satisfaction in FO [1]. We denote by  $Sat_D(\Phi)$  the set of satisfying assignments of  $\Phi$  over D. A DB D' is said to extend a DB D, if, for each n-ary relation symbol  $R, R^D \subseteq R^{D'}$ .

Let  $(\mathcal{O}, D)$  be an OBDAS. Consider an ATQ q of the form  $q(x, \alpha(y)) \leftarrow \Phi$  with grouping variables x, aggregation variables y and condition  $\Phi$ . Let c be a tuple. A *certain assignment* is a mapping  $\delta \colon FV(\Phi) \to adom(D)$  where, for each D' that is a model of  $\mathcal{O}$  and extends D, there exists an assignment  $\gamma \in Sat_{D'}(\Phi)$  s.t., for all  $x \in FV(\Phi)$ ,  $\delta(x) = \gamma(x)$ . We denote by  $Sat_D^{\mathcal{O}}(\Phi)$  this set. The *certain group* of tuple c is the bag

$$H_c := \{ \delta(y) \mid c = \delta(x), \delta \in Sat_D^{\mathcal{O}}(\Phi) \}$$

$$(2)$$

and the set of *certain answers* of q over  $(\mathcal{O}, D)$  is the set

$$cert(q, \mathcal{O}, D) := \{ (\delta(x), \alpha(H_{\delta(x)})) \mid \delta \in Sat_D^{\mathcal{O}}(\Phi) \}.$$
(3)

The query answering (QA) decision problem for ATQs over OBDASs is the decision problem stated as follows: **Input:** a tuple (c, n), an ATQ q an OBDAS  $(\mathcal{O}, D)$ . **Question:** does  $(c, n) \in cert(q, \mathcal{O}, D)$ ? We are interested in the complexity of QA measured considering D as its sole input, that is, in the so-called *data complexity* of QA [18].

*Example 1.* Consider the database schema  $\mathbf{R}_s$ :={*takesCourse,comesFrom,takesPlace, Country,Student,University*}, where s in  $\mathbf{R}_s$  stands for "student". A database of  $\mathbf{R}_s$  is the database  $D_s$ 

| takesCourse  |            | Student |                | Course     |       | Country | takesPlace  | comesFrom    |
|--------------|------------|---------|----------------|------------|-------|---------|-------------|--------------|
|              | Course     | SName   | University     | CName      | CCred | CoName  | CName PName | SName CoName |
| Luca<br>Luca | TOC<br>ADS | Luca    | PName<br>Unibz | TOC<br>ADS | 4     | Italy   | TOC Unibz   | Luca Italy   |
|              | German     | James   | CHIDZ          | German     | 0     | UK      | German LC   | James UK     |

where "TOC" stands for computational complexity and computability theory, "ADS" for algorithms and data structures, "LC" for Language Centre and "Unibz" for Bolzano University. (for convenience we use attribute names to denote relation positions). The following set  $O_s$  of constraints

$$\begin{aligned} \forall x (\exists y takesCourse(x, y) \Rightarrow Student(x)) & \forall x (\exists y takesCourse(y, x) \Rightarrow Course(x)) \\ \forall x (\exists y comesFrom(x, y) \Rightarrow Student(x)) & \forall x (\exists y comesFrom(y, x) \Rightarrow Country(x)) \\ \forall x (\exists y takesPlace(x, y) \Rightarrow Course(x)) & \forall x (\exists y takesPlace(y, x) \Rightarrow Place(x)) \\ \forall x (\exists y hasCredits(x, y) \Rightarrow Student(x)) & \forall x (University(x) \Rightarrow Place(x)) \end{aligned}$$

provide a conceptual model of the domain of students. Hence, the pair  $(\mathcal{O}_s, D_s)$  constitutes an OBDAS. Consider now the **count** ATQ  $q_0$  over  $\mathbf{R}_s$ 

$$q_0(x, \mathbf{count}(y)) \leftarrow \exists z(\mathit{Student}(y) \land \mathit{takesCourse}(y, z) \land \mathit{comesFrom}(y, x) \land \mathit{Country}(x))$$
(q\_0)

which we would had written in SQL as

```
SELECT s2.CName, COUNT(s2.SName)
FROM Student s1, comesFrom s2
WHERE EXISTS (SELECT *
    FROM takesCourse s3
    WHERE s1.SName = s2.SName AND s2.SName = s3.SName)
GROUP BY s1.CName
```

The query  $q_0$  asks for the number of courses taken by students of each country. Asking  $q_0$  to  $(\mathcal{O}_s, D_s)$  gives  $cert(q_0, \mathcal{O}_s, D_s) = \{(\text{Italy}, 1), (\text{UK}, 1)\}$ .

### **3** Expressing Query Answering (QA)

Translating English declarations and questions into ontology constraints and queries symbolically and compositionally can be modelled by English formal semantics *compositional translations*  $\tau(\cdot)$ , in the spirit of Montague and Clifford [12, 8], which use intermediate expressions called *meaning representations* from higher order logic (HOL), i.e., FO enriched with the  $\lambda$ -application,  $\lambda$ -asbtraction,  $\beta$ -reduction and the types of the simply-typed  $\lambda$ -calculus. The function  $\tau(\cdot)$  is recursively defined on English components by enriching (formal) grammars with semantic actions [10]: it exploits the syntax of the CL utterance by  $\lambda$ -applying the siblings of every syntactic constituent and by  $\lambda$ -abstracting the free variables introduced (in the MR) by subordinated clauses [10]. For every language L, we define  $\tau(L) := \{\tau(w) \mid w \in L\}$ .

Given a formal language L', to *express* L' *in* CL we define a declarative CL L and a compositional translation  $\tau(\cdot)$  s.t.  $\tau(L) = L'$ . Given an ontology language  $\mathcal{L}$  and a query language  $\mathcal{Q}$ , to *express* QA *in* CL we express  $\mathcal{L}$  and  $\mathcal{Q}$ .

**Expressing Ontologies.** CLs are tightly linked to ontologies. Traditionally, they were used for tasks such as ontology authoring. More recently, they have been used for declaring and querying information. The OWL web ontology language<sup>1</sup> is the W3C standard for web-based ontologies and ontology-based systems, and is formally underpinned by description logics (DLs), which are decidable fragments of FO specifically tailored for representing and reasoning about knowledge [3]. In particular, OWL 2 corresponds to the DL SROIQ (with data types). The CL ACE-OWL [9] expresses OWL in controlled English. OWL however does not scale to data in ontology based systems: inference and query answering are **coNP**-hard in data complexity.

It is of interest, then, to consider CLs for which the data complexity of QA is tractable. One such CL is Lite-English (see [4] for its definition), for which QA is as hard as for DBs (in **LogSpace**). Lite-English expresses the DL *DL-Lite* [4]. A meaning-ful fragment of OWL closed under boolean operations in the DL  $\mathcal{ALCT}$ , expressed by the CL DL-English [17]. It is also of interest to consider fragments of everyday English whose expressiveness overlaps with OWL. The Fragments of English (FOE) [14] are obtained incrementally by considering all the (grammatical) utterances one can build using only copula, common nouns and the **Dets** "some", "every" and "no", i.e., the syllogistic fragment, and then exteding coverage to further English constructs. See Figure 1.

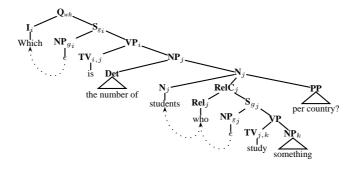
**Expressing ATQs.** We express ATQs with the CL ATQ-English. Sets are seen, in formal semantics, as characteristic functions of type  $e \to t$ . Similarly, bags can be seen as functions of type  $e \to \mathbb{N}$ . To express SQL aggregation functions we use *aggregate determiners* of type  $(e \to \mathbb{N}) \to \mathbb{Q}$ ). They are applied to **N** constituents which are made to denote bags:

$$\begin{split} \tau(\text{the greatest number of}) &:= \lambda P^{\mathbb{Q} \to \mathbb{N}} . \mathbf{max}(P) : (e \to \mathbb{N}) \to \mathbb{Q}, \\ \tau(\text{the smallest number of}) &:= \lambda P^{\mathbb{Q} \to \mathbb{N}} . \mathbf{min}(P) : (e \to \mathbb{N}) \to \mathbb{Q}, \\ \tau(\text{the total number of}) &:= \lambda P^{\mathbb{Q} \to \mathbb{N}} . \mathbf{sum}(P) : (e \to \mathbb{N}) \to \mathbb{Q}, \end{split}$$

<sup>&</sup>lt;sup>1</sup> http://www.w3.org/TR/owl-ref

| COP          | Copula, common and proper nouns, negation, universal and existential quantifiers                                                                                                                                             |
|--------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| COP+TV       | COP plus transitive verbs                                                                                                                                                                                                    |
| COP+TV+DT    | V COP+TV plus ditransitive verbs                                                                                                                                                                                             |
| COP+Rel      | COP plus relative pronouns                                                                                                                                                                                                   |
| Lite-English | Copula, left (positive and negative) universal quantification,<br>left relative pronouns, adjectives, common nouns, indeterminate<br>pronoun "something" and intransitive and transitive verbs                               |
| DL-English   | Copula, left (positive and negative) universal quantification,<br>relative pronouns, adjectives, common nouns (of which "thing"),<br>existential quantifiers, intransitive and transitive verbs,<br>negation and conjunction |

| COP     | $\Phi_l(x) \to A(x)$                                                              | $  \forall x(\Phi_l(x) \Rightarrow \pm \Phi_r(x))$    | No student failed.      |
|---------|-----------------------------------------------------------------------------------|-------------------------------------------------------|-------------------------|
|         | $\Phi_r(x) \to \Phi_l(x)$                                                         | $\exists x(\Phi_l(x) \land \Phi_r(x))$                | Some student failed.    |
| COP+    | $\Phi_l(x) \to A(x)$                                                              | $\forall x(\Phi_l(x) \Rightarrow \pm \Phi_r(x))$      | No student failed.      |
| TV      | $\Phi_r(x) \to \Phi_l(x) \mid \forall y(A(x) \Rightarrow \pm \psi(x, y))$         | $\exists x(\Phi_l(x) \land \Phi_r(x))$                | Some student studies    |
|         | $  \exists y(A(x) \land \psi(x, y))$                                              |                                                       | every course.           |
| COP+    | $\Phi_l(x) \to A(x)$                                                              | $\forall x(\Phi_l(x) \Rightarrow \pm \Phi_r(x))$      | Every student           |
| TV+     | $\Phi_{tv}(x) \to \Phi_l(x) \mid \forall y(A(x) \Rightarrow \pm \psi(x, y))$      |                                                       | gives no credit         |
| DTV     | $\exists y(A(x) \land \psi(x,y))$                                                 |                                                       | to some student.        |
|         | $\Phi_{dtv}(x,y) \to \forall z (A(x) \Rightarrow \pm \chi(x,y,z))$                | $\exists x(\Phi_l(x) \land \Phi_r(x))$                | Some student            |
|         | $\exists z(A(x) \land \chi(x, y, z))$                                             |                                                       | borrows some book       |
|         | $\Phi_r(x) \to \Phi_{tv}(x) \mid \forall y(A(x) \Rightarrow \pm \Phi_{dtv}(x,y))$ |                                                       | from some library.      |
|         | $  \exists y(A(x) \land \Phi_{dtv}(x,y))$                                         |                                                       |                         |
| COP+    | $\Phi_l(x) \to A(x) \mid \pm \Phi_l(x) \land \pm \Phi_l(x)$                       | $\forall x (\pm \Phi_l(x) \Rightarrow \pm \Phi_r(x))$ | Some student who is not |
| Rel     | $\Phi_r(x) \to \Phi_l(x)$                                                         | $\exists x(\pm \Phi_l(x) \land \pm \Phi_r(x))$        | diligent is smart.      |
| DL-Lite | $\Phi_l(x) \to A(x) \mid \exists y \psi(x, y)$                                    | $\forall x(\Phi_l(x) \Rightarrow \pm \Phi_r(x))$      | Everybody who studies   |
|         | $\Phi_r(x) \to \Phi_l(x)$                                                         |                                                       | something is a student. |
| ALCI    | $\Phi_l(x) \to A(x) \mid \exists y \psi(x, y)$                                    | $\forall x (\pm \Phi_l(x) \Rightarrow \pm \Phi_r(x))$ | Every student that      |
|         | $ \pm \Phi_l(x) \wedge \pm \Phi_l(x) $                                            |                                                       | is not diligent         |
|         | $\exists y\psi(x,y)\wedge\pm\Phi_{l}(y)$                                          |                                                       | is not a good student.  |
|         | $\Phi_r(x) \to \Phi_l(x)$                                                         |                                                       |                         |
|         |                                                                                   |                                                       |                         |



**Fig. 1. Top:** Coverage of the declarative CLs discussed in this paper and the ontology languages they express. Note that  $\psi(x, y)$  (resp.  $\chi(x, y, z)$ ) stands for some binary (resp. ternary) atom. By  $\pm$  we convey the fact that an atom or condition may or may not be negated. Complete utterances in these fragments are all of the form **Det N VP**, where **Det** maps, modulo  $\tau(\cdot)$ , into either  $\forall$  or  $\exists$ , **N** (recursively) into  $\Phi_l(x)$ , the subject, and **VP** (recursively) into  $\Phi_r(x)$ , the predicate [14, 17, 4]. Notice that subjects and predicates, but for COP+REL and DL-English, express different properties (they are non-symmetrical). **Below:** GROUP BY clauses are captured by **PP** components.

```
\tau(\text{the average number of}) := \lambda P^{\mathbb{Q} \to \mathbb{N}} . \mathbf{avg}(P) : (e \to \mathbb{N}) \to \mathbb{Q},
\tau(\text{the number of}) := \lambda P^{e \to \mathbb{N}} . \mathbf{count}(P) : (e \to \mathbb{N}) \to \mathbb{Q},
\tau(\text{the number of distinct}) := \lambda P^{e \to \mathbb{N}} . \mathbf{countd}(P) : (e \to \mathbb{N}) \to \mathbb{Q}.
```

MRs make use of a set  $\{e, t, \mathbb{N}, \mathbb{Q}\}$  of basic types. Notice that booleans  $(\{0, 1\})$  are positive integers and that as a result bag-typed expressions are implicitly polymorphic. The gammar of ATQ-English is specified as follows. We express GROUP BY clauses (followed possibly by a HAVING clause) from SQL by means of **PP**s that combine with subordinate clauses. We disregard morphology and polarity issues, which can be easily dealt with by considering *definite clause grammar* (DCG) rules, where parsing is based on SLD-resolution and unification [10].

| $\mathbf{Q}_{wh} \rightarrow \mathbf{I}_i \ \mathbf{N}_i \ \mathbf{S}_{g_i}? \qquad \tau(\mathbf{Q}_{wh}) := \lambda \bar{z}.\tau(\mathbf{I}_i)(\tau(\mathbf{N}_i))(\lambda i.\tau(\mathbf{S}_{g_i}))$                                                                                                                                                                                                      |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $\mathbf{Q}_{wh} \rightarrow \mathbf{I}_i \; \mathbf{S}_{g_i}? \qquad \qquad \tau(\mathbf{Q}_{wh}) := \lambda \bar{z} \cdot \tau(\mathbf{I}_i) (\lambda i \cdot \tau(\mathbf{S}_{g_i}?))$                                                                                                                                                                                                                   |
| $\mathbf{Q}_{Y/N} \rightarrow \text{does } \mathbf{N} \mathbf{P}_i \ \mathbf{V} \mathbf{P}_i? \ \tau(\mathbf{Q}_{Y/N}) := \tau(\mathbf{N} \mathbf{P}_i)(\tau(\mathbf{V} \mathbf{P}_i))$                                                                                                                                                                                                                     |
| $\mathbf{Q}_{Y/N} \rightarrow \mathrm{is} \mathbf{NP}_i \mathbf{VP}_i$ ? $\tau(\mathbf{Q}_{Y/N}) := \tau(\mathbf{NP}_i)(\tau(\mathbf{VP}_i))$                                                                                                                                                                                                                                                               |
| $\mathbf{S}_{g_i} \rightarrow \mathbf{NP}_{g_i} \mathbf{VP}_i \qquad \tau(\mathbf{S}_{g_i}) := \tau(\mathbf{NP}_{g_i})(\tau(\mathbf{VP}_i))$                                                                                                                                                                                                                                                                |
| $\mathbf{N}_i \rightarrow \mathbf{Adj}  \mathbf{N}_i \qquad \qquad \tau(\mathbf{N}_i) := \tau(\mathbf{Adj})(\tau(\mathbf{N}_i))$                                                                                                                                                                                                                                                                            |
| $\mathbf{N}_i \rightarrow \mathbf{N}_i \ \mathbf{Rel} \mathbf{C}_i \ \mathbf{PP} \qquad \tau(\mathbf{N}_i) := \tau(\mathbf{Rel}_i)(\tau(\mathbf{N}_i))(\tau(\mathbf{PP}))$                                                                                                                                                                                                                                  |
| $ \operatorname{\mathbf{RelC}}_i \to \operatorname{\mathbf{Rel}}_i \operatorname{\mathbf{S}}_{g_i} \qquad \tau(\operatorname{\mathbf{RelC}}_i) := \tau(\operatorname{\mathbf{Rel}}_i)(\lambda i \cdot \tau(\operatorname{\mathbf{S}}_{g_i})) \qquad \operatorname{\mathbf{VP}}_i \to \operatorname{is} \operatorname{\mathbf{Adj}} \tau(\operatorname{\mathbf{VP}}_i) := \tau(\operatorname{\mathbf{Adj}})$ |
| $\mathbf{VP}_i \rightarrow \mathbf{VP}_i \ \mathbf{Crd} \ \mathbf{VP}_i \qquad \tau(\mathbf{VP}) := \tau(\mathbf{Crd})(\tau(\mathbf{VP}_i))(\tau(\mathbf{VP}_i)) \ \mathbf{VP}_i \rightarrow \text{is a } \mathbf{N}_i \tau(\mathbf{VP}_i) := \tau(\mathbf{N}_i)$                                                                                                                                           |
| $\mathbf{VP}_i \to \mathbf{TV}_{i,j} \ \mathbf{NP}_j \qquad \tau(\mathbf{VP}_i) := \tau(\mathbf{TV}_{i,j})(\tau(\mathbf{NP}_j)) \qquad \mathbf{VP}_i \to \mathbf{IV}_i  \tau(\mathbf{VP}_i) := \tau(\mathbf{IV}_i)$                                                                                                                                                                                         |
| $\mathbf{NP}_{i} \rightarrow \mathbf{Det} \ \mathbf{N}_{i} \qquad \tau(\mathbf{NP}_{i}) := \tau(\mathbf{Det})(\tau(\mathbf{N}_{i})) \qquad \mathbf{NP}_{i} \rightarrow \mathbf{Pro}_{i} \ \tau(\mathbf{NP}_{i}) := \tau(\mathbf{Pro}_{i})$                                                                                                                                                                  |
| $\mathbf{PP} \to \mathbf{PP} \ \mathbf{RelC}_i \qquad \tau(\mathbf{PP}) := \tau(\mathbf{PP})(\tau(\mathbf{RelC}_i)) \qquad \mathbf{NP}_i \to \mathbf{Pn}_i  \tau(\mathbf{NP}_i) := \tau(\mathbf{Pn}_i)$                                                                                                                                                                                                     |

Notice that  $\bar{z} \subseteq FV(\tau(N_i)) \cup FV(\tau(S_{g_i}))$  (this is the expedient that allows us to capture grouping variables). We say that a condition  $\Phi$  is *equivalent* to a HOL expression  $\alpha = \lambda \bar{x} \cdot \beta : \tau$ , in symbols  $\Phi \equiv \alpha$ , when  $\Phi = \beta$ .

#### **Theorem 1.** ATQ-English expresses ATQs.

*Proof.* ( $\Rightarrow$ ) We need to show that for every Wh-question Q in ATQ-English there exists an ATQ q of the form s.t.  $\tau(Q) \equiv q$ . Questions Q come in three kinds, (*i*) aggregate Whquestions, (*ii*) non-aggregate Wh-questions and (*iii*) (non-aggregate) Y/N-questions. To prove this result, we prove something more general, namely that for each (recursive) **N** and/or **VP** constituent of ATQ-English, there exists a tree-shaped condition  $\Phi(x)$  s.t. they map to, modulo  $\tau(\cdot)$ ,  $\lambda x. \Phi(x) : e \to \mathbb{N}$ . This we can prove by an easy induction on **VP**s and **N**s, taking care that types, polarity and morphosyntactic features, unify. For simplicity, we disregard gap-filler indexes. It is then easy to see that, for instance, "which is **Det N** per **N**" maps to  $\lambda x^e \cdot \lambda n^{\mathbb{Q}} \cdot n \approx \alpha(\lambda y^e \cdot \Phi(y) \land \Phi'(y)): e \to (\mathbb{Q} \to t)$ , that "does **NP VP**" maps to  $\exists x \Phi(x) : t$ , or that "which **N VP**" maps to  $\lambda x^e \cdot \Phi(x): e \to \mathbb{N}$ .

( $\Leftarrow$ ) We need to show that for each ATQ q there exists a question Q in ATQ-English s.t.  $\tau(Q) \equiv q$ . In order to prove this, we prove, by induction on tree-shaped conditions  $\Phi(x)$  rooted in x, that there exists either a **N** or a **VP** constituent in ATQ-English s.t.  $\tau(\mathbf{N}) \equiv \Phi(x)$  (resp.  $\tau(\mathbf{VP}) \equiv \Phi(x)$ ):

- 1. (Basis) If  $\Phi(x) = A(x)$ , then it has as preimage the **N** A or the **VP** "is a A", while if  $\Phi(x) = \exists y(R(x,y))$ , it has as preimage the **N** or **VP** "Rs something".
- 2. (Inductive step) If  $\Phi(x) = \Phi'(x) \land \Phi''(x)$ , by IH  $\Phi'(x)$  is the image of some **N** or **VP** and similarly for  $\Phi''(x)$ . Hence,  $\Phi(x)$  has as preimage either "**N RelC**" (where, e.g., **RelC** rewrites into the **VP** associated to  $\Phi''(x)$ ) or "**VP** and **VP**". The argument is similar for  $\Phi(x) = \exists y R(x, y) \land \Phi'(y)$ .

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Clearly then, the ATQ  $q(x, \alpha(x)) \leftarrow \Phi(x) \land R(x, y) \land \Phi'(y)$  (or, more precisely, its equivalent HOL MR) will have as preimage in ATQ English the question "which is **Det** N per N'?", where **Det** is an aggregate determiner. On the other hand,  $q(x) \leftarrow \Phi(x)$  will be the image of "what/who **VP**?" and  $q() \leftarrow \exists x \Phi(x)$  will be the image of "does anybody **VP**?" or "is anybody **VP**?".

Example 2. Consider the following Wh-question:

Which is the number of students who study something, per country? (Q0)

It gives rise to the **count** aggregate query  $q_0$  of Example 1 via the parse tree from Figure 1, which is generated by combining our grammar with the following lexicon. Aggregate determiners express the definite **NP** "the number of **N**" while the *grouping complement* (a **PP** attachment) "per **N**" expresses grouping:

 $\begin{array}{l} & -\tau(\mathrm{which}):=\lambda R^{\mathbb{Q}\to(\mathbb{Q}\to t)}.\lambda n^{\mathbb{Q}}.R(n,m):(\mathbb{Q}\to(\mathbb{Q}\to t))\to(\mathbb{Q}\to t).\\ & -\tau(\mathrm{is}):=\lambda n^{\mathbb{Q}}.\lambda m^{\mathbb{Q}}.n\approx m:\mathbb{Q}\to(\mathbb{Q}\to t).\\ & -\tau(\mathrm{e}):=\lambda P^{\mathbb{Q}\to t}.P(n):(\mathbb{Q}\to t)\to t.\\ & -\tau(\mathrm{students}):=\lambda x^{e}.Student(x):e\to\mathbb{N}.\\ & -\tau(\mathrm{something}):=\lambda P^{e\to t}.\exists y^{e}P(y):(e\to\mathbb{N})\to t\\ & -\tau(\mathrm{who}):=\lambda P^{e\to\mathbb{N}}.\lambda q^{e\to\mathbb{N}}.\lambda x^{e}.(P(x)\wedge Q(x)):(e\to\mathbb{N})\to((e\to\mathbb{N})\to(e\to\mathbb{N})).\\ & -\tau(\mathrm{per\ country}):=\lambda P^{e\to\mathbb{N}}.\lambda y^{e}.(P(y)\wedge Country(z)\wedge comesFrom(y,z)):(e\to\mathbb{N})\to((e\to\mathbb{N})\to(e\to\mathbb{N})\to(e\to\mathbb{N})).\\ & -\tau(\mathrm{per\ country}):=\lambda Q^{e\to\mathbb{N}}.\lambda P^{e\to\mathbb{N}}\lambda y^{e}.(P(y)\wedge Country(z)\wedge comesFrom(y,z)\wedge Q(z)):\\ & (e\to\mathbb{N})\to((e\to\mathbb{N})\to(e\to\mathbb{N})).\\ & -\tau(\mathrm{study}):=\lambda \alpha^{(e\to\mathbb{N})\to\mathbb{N}}.\lambda x^{e}.\alpha(\lambda y^{e}.takesCourse(x,y)):((e\to\mathbb{N})\to\mathbb{N})\to(e\to\mathbb{N}). \end{array}$ 

The value of  $\tau(\cdot)$  on the whole question (after  $\lambda$ -application and abstraction and  $\beta$ -normalization) is

$$\lambda x^{e}.\lambda m^{\mathbb{Q}}.m \approx \mathbf{count}(\lambda y^{e}.Student(y) \land \exists z^{e}(takesCourse(y, z)) \land comesFrom(y, x) \land Country(x)) \colon e \to (\mathbb{Q} \to t),$$

i.e., the value of  $\tau(\cdot)$  on the (root) component  $\mathbf{Q}_{wh}$  (see again Figure 1). Clearly,  $\tau(\mathbf{Q0}) \equiv q_0$ .

**Expressing Comparisons,**  $\lor$ ,  $\neg$  and  $\forall$ . By covering comparative (both majorative and diminutive) and equative adjectives we can capture comparisons, i.e., the constants  $\theta \in \{\leq, \geq, <, >, \approx\}$  of type  $\mathbb{Q} \rightarrow (\mathbb{Q} \rightarrow t)$  over the rationals  $\mathbb{Q}$  (which we assume to be totally ordered) and comparison atoms  $t \theta t'$  [1]. Another way of increasing the coverage of our CL consists in considering all the quantifiers and boolean operators definable on conditions, viz.,  $\lor$ ,  $\forall$  and  $\neg$  (disjunction is equivalent to the UNION and UNION ALL query constructors in SQL). Thus doing we express:

- 1. Tree-shaped conditions with comparisons,  $t \theta t'$  ( $\leq$ -ATQs).
- 2. Negations (with e.g. "does not") of tree-shaped conditions,  $\neg \Phi(x)$  ( $\neg$ -ATQs).
- 3. Unions (with "or") of tree-shaped conditions,  $\Phi(x) \lor \Phi'(x)$  ( $\lor$ -ATQs).
- 4. Universal (with "only") tree-shaped conditions,  $\forall x(R(x, y) \Rightarrow \Phi(y)) \ (\forall -ATQs)$ .

*Example 3.* Given the Adj "heavy", put: (i) heavier $(x, y) := \exists n \exists n' (hasCredits(x, n) \land$  $hasCredits(y,n') \land n \ge n'), (ii) s-heavier(x,y) := \exists n \exists n' (hasCredits(x,n) \land hasCredits(y,n'))$  $\wedge n > n'$ ) and (iii) as-heavy $(x, y) := \exists n \exists n' (hasCredits(x, n) \land hasCredits(y, n') \land n \approx$ n') of type  $e \to (e \to t)$ , where *hasCredits* is an expression of type  $e \to (\mathbb{Q} \to t)$ . Next, we create lexical entries for "is heavier than", "is strictly heavier than" (the majoratives) and for "is as heavy as" (the equative), as well as entries for the logical operations:

- $-\tau(\text{is heavier than}):=\lambda\alpha^{(e\to\mathbb{N})\to t}.\lambda x^e.\alpha(\lambda y^e.higher(x,y)):((e\to\mathbb{N})\to t)\to(e\to t).$
- $\tau$  (is as heavy as):= $\lambda \alpha^{(e \to \mathbb{N}) \to t}$ .  $\lambda x^e \cdot \alpha (\lambda y^e \cdot as high(x, y))$ :  $((e \to \mathbb{N}) \to t) \to (e \to t)$ .
- $-\tau(\text{is strictly heavier than}) := \lambda \alpha^{(e \to \mathbb{N}) \to t} \cdot \lambda x^e \cdot \alpha(\lambda y^e \cdot s \cdot higher(x, y)) : ((e \to \mathbb{N}) \to t)$  $\rightarrow (e \rightarrow t).$

- $\tau(\text{only}) \coloneqq \lambda Q.\lambda P. \forall x (P(x) \Rightarrow Q(x)) \colon (e \to \mathbb{N}) \to ((e \to \mathbb{N}) \to t).$
- $\begin{array}{l} -\tau(\mathsf{who}) \coloneqq \lambda P^{e \to \mathbb{N}} \cdot \lambda x^e \cdot P(x) \colon (e \to \mathbb{N}) \to (e \to \mathbb{N}) \cdot \\ -\tau(\mathsf{some}) \coloneqq \lambda P^{e \to \mathbb{N}} \cdot \lambda Q^{e \to \mathbb{N}} \cdot \exists x^e (P(x) \land Q(x)) \colon (e \to \mathbb{N}) \to ((e \to \mathbb{N}) \to t) \cdot \end{array}$

Content words can be easily added as follows. TVs like "comes from" give way to the entry  $\tau$  (comes from):= $\lambda \alpha^{(e \to \mathbb{N}) \to t} \cdot \lambda x^e \cdot \alpha(\lambda y^e \cdot comesFrom(x, y)) : ((e \to \mathbb{N}) \to t) \to t$  $(e \rightarrow t)$  and Ns such as "student", to entries such as  $\tau$ (student):= $\lambda x^e$ .Student(x): $e \rightarrow \mathbb{N}$ . Consider now the following controlled Wh-questions:

Which course is heavier than (strictly heavier than, as heavy as) some course? (Q1)

- Who is a student who does not come from Italy? (Q2)
- Who is a student or comes from some country? (Q3)
- Which student studies only courses held in universities? (Q4)

They can now be successfully parsed. ATQ-English can now express simple queries with  $\forall, \neg, \lor$  and  $\theta \in \{\leq, \geq, \approx, <, >\}$ .

#### **Data Complexity of QA** 4

In this section we show that adding  $\forall, \leq$  and  $\neg$  to conditions make query answering hard. The  $\lor$  operator alone, however, need not [6, 1]. Modulo  $\tau(\cdot)$ , reasoning over CLs is polynomially equivalent (in data complexity) to reasoning over their MRs [14]. In what follows, we identify CLs with their MRs (i.e., with constraints and/or formal queries) and reason solely on these MRs.

To check whether a tuple (c, n) is a certain answer for ATQ  $q(x, \alpha(y)) \leftarrow \Phi$  to an OBDAS  $(\mathcal{O}, D)$ , in general, we (i) check whether x is instantiated to c by a certain assignment and then (ii) loop over the (finitely many) certain assignments for y, updating at each step the value of  $\alpha$  on the group  $H_c$ , until  $\alpha$  returns n. Otherwise, our procedure will return a negative answer. In other words the data complexity of answering an ATQ depends, ultimately, on that of computing  $Sat_D^{\mathcal{O}}(\Phi)$  and coincides, for this reason, with the data complexity of answering its core (i.e., with that of answering CQs over OBDASs), whenever this data complexity is known.

**Theorem 2.** Answering ATQs (and unions thereof) w.r.t. Lite-English and COP declarations is in LogSpace in data complexity.

*Proof.* Lite-English expresses the *DL-Lite* ontology language [4]. It moreover, contains COP. The result follows immediately from the data complexity of answering CQs over *DL-Lite* OBDASs [6].  $\Box$ 

**Theorem 3.** Answering ATQs is **coNP**-complete for COP+Rel and DL-English.

*Proof.* (Sketch) It can be shown that QA for ATQs and COP+Rel is **coNP**-hard in data complexity. On the other hand, DL-English contains COP+Rel and is contained in the two-variable fragment of FO. The same holds for the cores of ATQs. Hence, data complexity is in **coNP** [13].  $\Box$ 

**Theorem 4.** Answering  $\forall$ -ATQs (and unions thereof) over OBDASs ( $\mathcal{O}$ , D) where  $\mathcal{O}$  is a COP ontology is **coNP**-hard in data complexity. It is in **coNP** for DL-English, COP+TV, Lite-English and COP.

*Proof.* (Hardness.) By reduction from the **NP**-complete satisfiability problem for 2+2 clauses (2+2-SAT), where, given a conjunction  $\phi := \psi_1 \wedge ... \wedge \psi_k$  of k propositional clauses of the form  $\psi_i := p_{i1} \vee p_{i2} \vee \neg n_{i1} \vee \neg n_{i2}$ , we ask whether there exists a truth assignment (ta)  $\delta(\cdot)$  s.t.  $\delta(\phi) = 1$ . 2+2-SAT was shown to be **NP**-complete by [15], whose prove we adapt.

Encode  $\phi$  into a DB  $D_{\phi}$  as follows. Consider the predicates  $P_1$ ,  $P_2$ ,  $N_1$  and  $N_2$ , and for each  $\psi_i$ , set:  $\{(i, p_{i1})\} \subseteq P_1^{D_{\phi}}$ ,  $\{(i, p_{i2})\} \subseteq P_2^{D_{\phi}}$ ,  $\{(i, n_{i1})\} \subseteq N_1^{D_{\phi}}$  and  $\{(i, n_{i2})\} \subseteq N_2^{D_{\phi}}$ . Next, consider three predicates  $A_f$  and  $A_t$  (unary), and Val (binary). Set  $\mathcal{O} := \{\forall x (A_f(x) \Rightarrow \neg A_t(x))\}$  and put  $\top \in A_t^{D_{\phi}}$ . Finally, consider the following (boolean)  $\forall$ -ATQ  $q() \leftarrow \Phi$  whose body is defined as follows,  $\Phi := \exists x \exists y_1 \exists y_2 \exists y_3 \exists y_4 (P_1(x, y_1) \land \forall z_1 (Val(y_1, z_1) \Rightarrow A_f(z_1)) \land P_2(x, y_2) \land \forall z_2 (Val(y_2, z_2) \Rightarrow A_f(z_2)) \land N_1(x, y_3) \land \exists z_2 (Val(y_3, z_3) \land A_t(z_3)) \land N_2(x, y_3) \land \exists z_3 (Val(y_4, z_4) \land A_t(z_4)))$ . We claim that

()  $\notin cert(q, \mathcal{O}, D_{\phi})$  iff  $\phi$  is satisfiable.

( $\Leftarrow$ ) If  $\phi$  is satisfiable, then there exists a ta  $\delta(\cdot)$  s.t.  $\delta(\phi) = 1$ . Define a DB D extending  $D_{\phi}$  and that is a model of  $\mathcal{O}$  as follows. Pick a  $v \in \Delta$  and put, for all p,  $(p, v) \in hasValue^{D}$  and  $v \in A_{t}^{D}$  iff  $\delta(p) = 1$ . Clearly, D is as desired and, for all  $\gamma$ ,  $D, \gamma \not\models \Phi$ , i.e.,  $Sat_{D}(\Phi)$  is empty. Thus,  $Sat_{D_{\phi}}^{\mathcal{O}}(\Phi)$  is empty and the result follows.

(⇒) If the certain answers are empty, then there exists a DB *D* s.t., for all  $\gamma$ , D,  $\gamma \not\models \Phi$ . Define now a tvd  $\delta(\cdot)$  from the  $p_{ij}$ s and the  $n_{ij}$ s, to  $\{0, 1\}$ , by putting, for all such propositional atoms p,  $\delta(p) = 1$  iff there exists a v s.t.  $(p, v) \in hasValue^D$  and  $v \in A_t^D$ . Clearly,  $\delta(\phi) = 1$ .

(Membership.) For the upper bound, we remind the reader that the core  $\breve{q}$  (and body  $\varPhi$ ) of an ATQ q are formulas from the two variable fragment of FO, for which data complexity is in **coNP** [13].

**Theorem 5.** Answering  $\neg$ -ATQs (and unions thereof) over OBDASs ( $\mathcal{O}$ , D) where  $\mathcal{O}$  is an empty ontology is **coNP**-hard in data complexity. It is in **coNP** for DL-English, COP+TV, Lite-English and COP.

*Proof.* (Sketch) By reduction, again from 2+2-SAT. The proof is also a variation of the previous two. We put  $\mathcal{O} := \emptyset$ , leave  $D_{\phi}$  unchanged and consider the boolean query with body  $\Phi := \exists x \exists y_1 \exists y_2 \exists y_3 \exists y_4 (P_1(x, y_1) \land \neg A_t(y_1) \land P_2(x, y_2) \land \neg A_t(y_2) \land N_1(x, y_3) \land A_t(y_3) \land N_2(x, y_3) \land A_t(y_4)$ ). The intuition is that a 2+2 clause propositional atom p is true under tvd  $\delta(\cdot)$  iff  $p \in A_t^D$  holds in DB D.

For the upper bound we reason as previously, by observing that the cores  $\breve{q}$  (and bodies  $\Phi$ ) of a  $\neg$ -ATQs q are also contained in the two-variable fragment of FO.

**Theorem 6.** Answering  $\leq$ -ATQs (and unions thereof) over OBDASs ( $\mathcal{O}$ , D) where  $\mathcal{O}$  is an empty ontology is **coNP**-hard in data complexity.

*Proof.* (Sketch) The lower bound is obtained by reduction, again, from 2+2-SAT. The proof is a slight variation of the previous one. Notice that  $\leq$  can be used to simulate negation.  $\mathcal{O}$  and  $D_{\phi}$  stay unchanged, and we consider the boolean CQ of (boolean tree-shaped body)  $\Phi := \exists x \exists y_1 \exists y_2 \exists y_3 \exists y_4 (P_1(x, y_1) \land y_1 \leq 0 \land P_2(x, y_2) \land y_2 \leq 0 \land N_1(x, y_3) \land y_3 > 0 \land N_2(x, y_3) \land y_4 > 0$ ). The intuition is that a 2+2 clause literal p is true under this encoding iff the (ground FO) fact p > 0 is true.

|              | ∨-ATQs        | ≤-ATQs    | ∀-ATQs        | <b>¬-ATQ</b> s |
|--------------|---------------|-----------|---------------|----------------|
| Lite-English | in LogSpace   | coNP-hard | coNP-complete | coNP-complete  |
| СОР          | in LogSpace   | coNP-hard | coNP-complete | coNP-complete  |
| COP+TV       | (unknown)     | coNP-hard | coNP-hard     | coNP-hard      |
| COP+TV+DTV   | (unknown)     | coNP-hard | coNP-hard     | coNP-hard      |
|              | coNP-complete |           |               |                |
| COP+Rel      | coNP-complete | coNP-hard | coNP-complete | coNP-complete  |

#### 5 Conclusions

We have proposed a class of aggregate queries, viz., tree-shaped aggregate queries (ATQs), equipped with a certain answers semantics. ATQs can be considered a subclass of the so-called epistemic aggregate queries defined in [7].

We have shown how to express ATQs in controlled English by means of the CL ATQ-English. We analyse GROUP BY clauses as modifiers of the question's subject (i.e., its subject **N** constituent). By using higher order logic (HOL) and, hence, (bag) typed, intermediate semantic representations, we ensure that the translation  $\tau(\cdot)$  is compositional and that query answering (QA) with ATQ-English questions reduces (w.r.t. data complexity) to QA with ATQs.

We have shown that answering ATQ-English controlled aggregate questions over declarative CLs such as ACE-OWL and other declarative languages that overlap in expressiveness with ACE-OWL reduces to conjunctive query answering. Therefore, computing aggregates does not have any significant impact on data complexity. Aggregates by themselves are constructs that any CL interface to OBDASs can support. What does have an impact are query conditions, alone or in combination with expressive ontology languages.

We have also shown that (*i*) allowing for full boolean operations in the declarative CL/ontology language and/or (*ii*) full boolean operations  $(\forall, \neg)$  and/or  $\leq$  in the interrogative CL/query language, yields immediately intractability.

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