

Multifarious Uncertainty in Ontologies

Where we are and where we might go

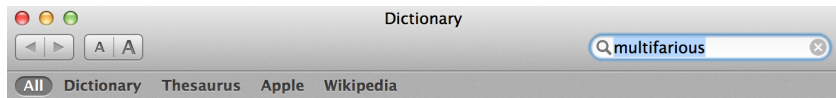
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▼ ————— *Dictionary* —————

multifarious | ,mʌlt(ə)'fe(ə)rēəs |

adjective

many and of various types: *multifarious activities*.

- having many varied parts or aspects: *a vast multifarious organization*.

DERIVATIVES

multifariously adverb .

multifariousness noun

ORIGIN late 16th cent.: from Latin *multifarius* + *-ous*.

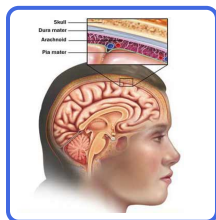
▼ ————— *Thesaurus* —————

multifarious

adjective

our multifarious ethnic traditions: DIVERSE, many, numerous, various, varied, diversified, multiple, multitudinous, multiplex, manifold, multifaceted, different, heterogeneous, miscellaneous, assorted; literary myriad, divers. ANTONYMS homogeneous.

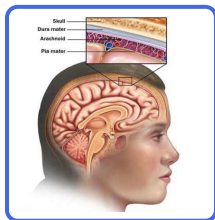
Motivation



Medical terminology

- ▶ Viral meningitis is a type of meningitis
- ▶ Bacterial meningitis is a type of meningitis
- ▶ Meningitis is either viral or bacterial

Motivation



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- ▶ *Meningitis is usually not fatal*
- ▶ *Meningitis and caused by bacteria is usually fatal*
- ▶ *Meningitis affects most of skull, Dura mater is mostly made of fibre*
- ▶ *B. menin. is similar to v. menin., Pia mater is analogous to dura mater*
- ▶ *Cases of B. meningitis can be treated with antibiotics*
- ▶ **But** *Mary has meningitis and is pregnant*

Uncertainty in Ontologies

Several nuances

- ▶ **Exceptions:** special cases, overriding of properties
meningitis, bact. meningitis
- ▶ **Similarity** or **analogy:** focus on relevant aspects, tolerance
pia mater, dura mater
- ▶ **Vagueness:** notions of 'generally', 'rarely', 'most'
meningitis rarely kills
- ▶ **Incomplete information:** take chances, be venturous
give antibiotics to cases of meningitis
- ▶ **Dynamicity:** incorporate new information, backtracking
not during pregnancy
- ▶ **Others**

Uncertainty in Ontologies

Various takes

- ▶ **Quantitative:** probabilistic, statistical
- ▶ **Qualitative:** logical
- ▶ **Combinations thereof**

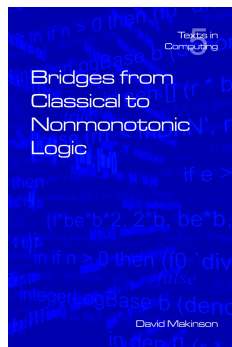
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Logical approaches

- ▶ Qualitative analysis of uncertainty in reasoning
- ▶ a.k.a. **nonmonotonic reasoning**
- ▶ Broader than the usual understanding of NMR



Outline

Overview

Where Are We?

Where To?

Conclusion

Outline

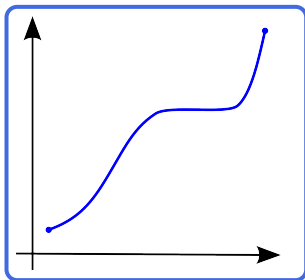
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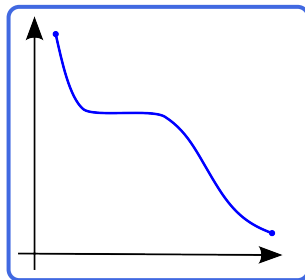
Where To?

Conclusion

Monotonicity



$$Cn(\alpha) \subseteq Cn(\alpha \wedge \beta)$$

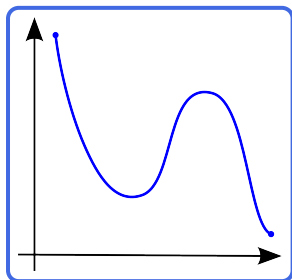


$$Mod(\alpha \wedge \beta) \subseteq Mod(\alpha)$$

In reasoning

- ▶ It means knowledge is always *incremental*
- ▶ **Not suitable** when facing uncertainty

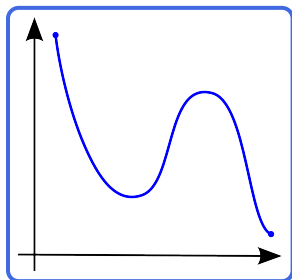
Reasoning under Uncertainty



In the logic landscape

- ▶ Shares aims of **non-classical** logics
- ▶ But does **not** reject classical reasoning
- ▶ Builds on classical logic, **extending** it

Reasoning under Uncertainty



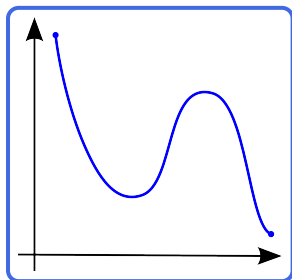
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Two fundamental aspects

- ▶ *Ampliativeness* and *defeasibility*

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Two fundamental aspects

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Happens at three levels (at least)

- ▶ *Object*, *entailment* and *meta-reasoning* levels

Ampliative Aspect of Uncertainty

Allowing **more conclusions** by **venturing** beyond what is known

Default reasoning

- ▶ **Jumping** to conclusions: $\mathcal{T} \not\models \neg\alpha$, $\therefore \mathcal{T} \cup \{\alpha\}$ OK
- ▶ E.g.: **negation as failure**, **closed-world assumption**

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Abductive reasoning

- ▶ Finding **tentative** explanations: $\mathcal{T} \not\models \alpha$, $\mathcal{T} \cup ? \models \alpha$
- ▶ E.g.: **diagnosis**, **forensics**

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Inductive reasoning

- ▶ Making generalizations: $P(a), P(b), P(c), \dots, \therefore \forall x.P(x)$ OK
- ▶ E.g.: physical laws, stereotypes

Defeasible Aspect of Uncertainty

Allowing **less conclusions** by **disregarding** or **blocking** some of them

Retractive reasoning

- ▶ **Withdrawing** conclusions **already** derived

$$\alpha \in Cn(\mathcal{T}) \quad \Rightarrow \quad \alpha \notin Cn(\mathcal{T})$$

- ▶ Ex.: **ontology change**, **dialectics**

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Preemptive reasoning

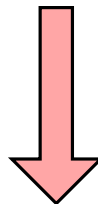
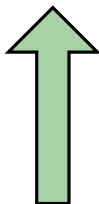
- ▶ **Preventing** the **derivation** of some conclusion

$$\gamma \rightarrow \alpha, \quad \alpha \rightarrow \beta, \quad \text{not } (\gamma \rightarrow \beta)$$

- ▶ Ex.: **special cases** in taxonomies, **exceptions** in regulations

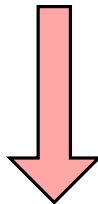
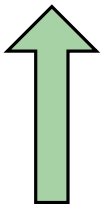
Central Research Question in Uncertainty

How to sanction **more** conclusions and how to sanction **fewer** of them



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Uncertainty at the Object Level

Logical symbols of the language

- ▶ Connectives can behave nonmonotonically

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Nonmonotonic version of material implication ' \rightsquigarrow '

- ▶ Ampliative aspect: $\alpha \rightsquigarrow \beta$ holds even if $\alpha \rightarrow \beta$ doesn't

meningitis \rightsquigarrow \neg *fatal*

- ▶ Defeasible (preemptive) aspect: $\alpha \rightsquigarrow \beta$ is the case but $\alpha \wedge \gamma \rightsquigarrow \beta$ not

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Negation in logic programming

- ▶ Ampliative and retractive

Uncertainty at the Entailment Level

Sanctioned inferences or reasoning

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Sanctioned inferences or reasoning

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Nonmonotonic version of \models

- ▶ Historically the **most extensively studied**
- ▶ Ampliative aspect: we may have $\{\alpha\} \approx \beta$ even if $\{\alpha\} \not\models \beta$

$\{hasMeningitis(mary)\} \approx AntiBioOK$

- ▶ Defeasible (retractive) aspect: $\{\alpha\} \approx \beta$ is the case but $\{\alpha, \gamma\} \not\approx \beta$

$\{hasMeningitis(mary), pregnant(mary)\} \not\approx AntiBioOK$

Uncertainty at the Meta-reasoning Level

Reasoning about sanctioned inferences

- ▶ Nonmonotonicity happens 'outside' the logic

Theory change

- ▶ Theory **expansion**: make sure $\alpha \in Cn(\mathcal{T})$
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Ampliative aspect

- ▶ Usually more '**conservative**': **primacy of new information**
- ▶ Even when not conservative, **not venturous enough**: **minimal change**
- ▶ New information must follow **classically** from the new theory

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Standard Logical Frameworks for Uncertainty

- ▶ Conditional logics
- ▶ Default logic
- ▶ Circumscription
- ▶ Autoepistemic logic
- ▶ AGM belief revision
- ▶ Ontology evolution
- ▶ Abstract argumentation frameworks
- ▶ Dynamic epistemic logic
- ▶ Adaptive logics
- ▶ Preferential logics
- ▶ ...

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Default Logic

Motivation

- ▶ Account of conclusions **by default** (based on absence of knowledge)
- ▶ Default **rules** of the form

$$\frac{\alpha : \beta, \neg\gamma}{\beta} \quad \frac{\textit{hasMeningitis}(\textit{mary}) : \textit{AntiBioOK}, \neg\textit{pregnant}(\textit{mary})}{\textit{AntiBioOK}}$$

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- ▶ Related to **negation as failure**

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Semantic intuition

- ▶ Minimize the **extension** of predicates (different **policies**)
- ▶ Look at **some** models of the premises
- ▶ $\alpha \models_{\text{Circ}(\gamma)} \beta$ if the **γ -minimized** α -models are β -models
- ▶ E.g. minimize extension of ***pregnant*** to infer ***AntiBioOK***

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- ▶ Additions and removals of **theorems**
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Approaches and construction methods

- ▶ *Belief bases* and *belief sets*
- ▶ *Partial-meet*, *kernels*, *system of spheres*, etc.

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Example

$\mathcal{K} = \{\dots, \exists \text{hasDisease.Menin}(\text{mary}), \dots\} \models \exists \text{hasDisease.}\neg \text{Fatal}(\text{mary})$

Revise \mathcal{K} with $\exists \text{hasDisease.BacMenin}(\text{mary})$

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Ontology Evolution

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- ▶ Essentially the **same** as AGM ...
- ▶ ...but from a **different angle** (more 'operational')

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[hasDisease.BacMenin(mary)!]

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- ▶ Epistemic possibilities held by multiple agents
- ▶ Model transformations: $\mathcal{M}_E \otimes \mathcal{M}_A \Rightarrow \mathcal{M}'_E$

$$\mathcal{M}_E^{\text{hasDisease.Menin(mary)}} \otimes \mathcal{M}_A^{\text{hasDisease.BacMenin(mary)}} \Rightarrow \mathcal{M}'_E^{\text{hasDisease.Fatal(mary)}}$$

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Aspects and levels

- ▶ Only **defeasible** (retractive): $\neg K\alpha \rightarrow [\alpha!]\neg K\alpha$ **not** valid
- ▶ Only at the **object level**

Preferential Logics and Rational Closure (KLM)

Motivation

- ▶ Nonmonotonic conditional \rightsquigarrow satisfying **rationality properties**:

$$\text{(Ref)} \quad \alpha \rightsquigarrow \alpha$$

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- ▶ Extra structure: *preference relation* on worlds
- ▶ Notion of *minimal entailment à la* circumscription
- ▶ Different *strategies*: *prototypical* and *presumptive* reasoning

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Preferential DLs

Defeasible subsumption

- ▶ E.g. $\text{Menin} \sqsubseteq \neg\text{Fatal}$, $\text{BacMenin} \sqsubseteq \text{Fatal}$
- ▶ Properties

$$\text{(Cons)} \top \not\sqsubseteq \perp$$

$$\text{(Ref)} C \sqsubseteq C$$

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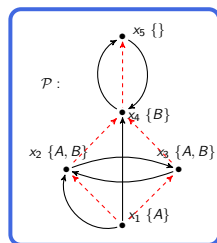
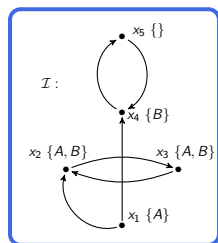
Typicality operator

- ▶ E.g. $\mathbf{T}(\text{Menin}) \sqsubseteq \neg\text{Fatal}$, $\mathbf{T}(\text{BacMenin}) \sqsubseteq \text{Fatal}$

Preferential DLs

Semantics

- ▶ Enriched DL Interpretations $\mathcal{P} := \langle \Delta^{\mathcal{I}}, \cdot^{\mathcal{I}}, \prec \rangle$
- ▶ $\Delta^{\mathcal{I}}$ and $\cdot^{\mathcal{I}}$ as before
- ▶ \prec is a *preference (or normality) relation*



$\mathcal{P} \models C \sqsubseteq D$ iff $\min_{\prec} C^{\mathcal{P}} \subseteq D^{\mathcal{P}}$

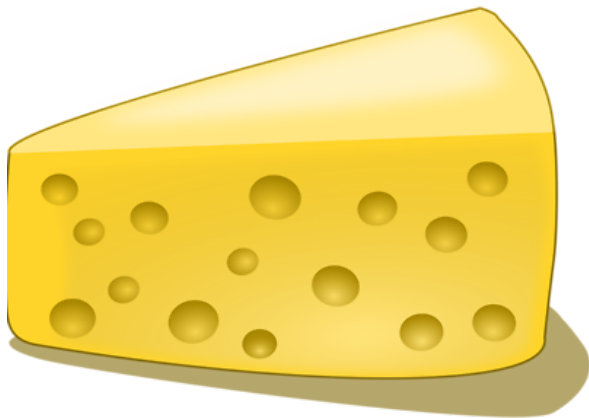
$(\mathbf{T}(C))^{\mathcal{P}} = \min_{\prec} C^{\mathcal{P}}$

Representation results: soundness and completeness of postulates

Existing Frameworks: Summary

	Amp.	Def.	Obj.	Ent.	Meta.
Conditional logics	✓	✓	✓		
Default logics	✓	✓		✓	
Circumscription	✓	✓		✓	
Autoepistemic logic	✓	✓		✓	
AGM belief change		✓			✓
Ontology evolution		✓			✓
Argumentation		✓			✓
DEL		✓	✓		
Adaptive logics	✓	✓		✓	✓
Preferential	✓	✓	✓	✓	

Existing Frameworks: Summary



Not all **levels** and **aspects** have been dealt with!

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The Need for Multifarious Uncertainty

Other nonmonotonic logical symbols

- ▶ Nonmonotonic **connectives**
- ▶ Nonmonotonic **modalities** and **quantifiers**

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- ▶ Links with **abduction**, **induction** and other forms of reasoning

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New and more general theories of uncertainty are called for

Uncertainty in Concept Constructors

Defeasible disjointness

- ▶ Normally mutually exclusive

BacMenin $\sqsubseteq \neg$ ViralMen 'OR' ViralMen $\sqsubseteq \neg$ BacMenin

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Other layers of typicality

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Typicality for roles

- ▶ Some relations are more normal than others

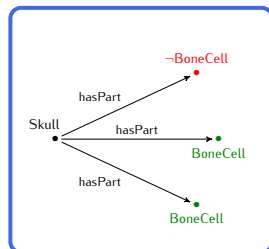
$T(\text{infectedBy}), T(\text{marriedTo})$

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Nonmonotonic role restrictions

- ▶ Normal role fillers

$\text{Skull} \equiv \forall \text{madeOf}.\text{Bone}$

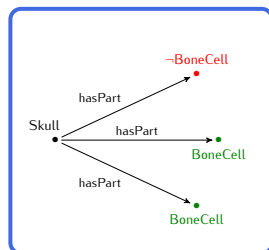


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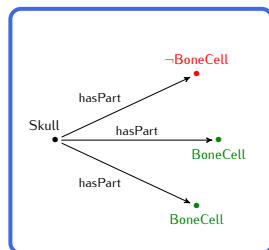
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Defeasible role properties

- ▶ Holding in the most normal cases

marriedTo : usually functional, partOf : usually transitive

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- ▶ Further semantic **constraints**
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$$\frac{C \sqsubseteq D}{\exists r.C \sqsubseteq \exists r.D}$$

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► Rational Existential Monotonicity

$$(REM) \frac{\exists r.C \sqsubseteq \exists r.D, \exists r.C \not\sqsubseteq \neg \mathbf{T}(\exists r.E)}{\exists r.(C \sqcap E) \sqsubseteq \exists r.D}$$

► Rational Value Monotonicity

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Different levels of ‘venturousness’

- ▶ **Skeptical**, **credulous**, and **in between**

Uncertainty in Entailment

Standard constructions

- ▶ Usually: **Strengthening** the premises or **relaxing** the conclusions

$$\mathcal{K} \models \alpha \text{ iff } \downarrow \text{Mod}(\mathcal{K}) \subseteq \text{Mod}(\alpha)$$

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Beyond standard constructions

- ▶ Go beyond the **dichotomy** “preferred v. non-preferred”
- ▶ Look for other notions of **preferences** and **minimality**
- ▶ New **forms of reasoning** beyond induction and abduction?

Enhanced Theory Change

Beyond propositional languages

- ▶ Modal logics, description logics, ...

$$\mathcal{T} \star \Box \alpha \text{ ?}, \quad \mathcal{T} \star (C \sqsubseteq D) \text{ ?}, \quad \mathcal{T} - r(a, b) \text{ ?}$$

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Beyond classical constructors

- ▶ Makes sense for languages with **nonmonotonic connectives**
- ▶ A whole family of AGM-like **new postulates**
- ▶ Links with various \approx

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Remember

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Principle

- ▶ Not to diverge from existing approaches, rather **build on** them

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Several frameworks available

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Why?

- ▶ Provides a general **proof-theoretic** characterization of \rightsquigarrow (and \sqsubseteq)
- ▶ Basis for nonmonotonic entailment \models , e.g. *rational closure*
- ▶ Links with **AGM** belief revision (inter-definability)
- ▶ **Simple** and **elegant** (cf. our desiderata)
- ▶ Recently extended to **modal** and **description logics**

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What we have seen

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- ▶ It happens at **three levels**: object, entailment, and meta-reasoning
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Thank you!