

# ***XML Data Management***

## **6. XPath 1.0 Principles**

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# XPath Expressions and the XPath Document Model

- XPath expressions are evaluated over documents
- XPath operates on an *abstract document* structure  
(essentially the same as DOM)
- Documents are *trees* with several *types of nodes*,  
the most important of which are
  - **element** nodes
  - **attribute** nodes
  - **text** nodes

*There are other node types (namespaces, comments, etc.),  
which we ignore in this lecture*

# The Recipes Example (DTD)

```
<!ELEMENT recipes      (recipe*)>
<!ELEMENT recipe      (title, ingredient+, preparation, nutrition)>
<!ELEMENT title       (#PCDATA)>
<!ELEMENT ingredient  (ingredient*, preparation?)>
<!ATTLIST ingredient
    name  CDATA #REQUIRED
    amount CDATA #IMPLIED
    unit  CDATA #IMPLIED>
<!ELEMENT preparation (step+)>
<!ELEMENT step        (#PCDATA)>
<!ELEMENT nutrition   EMPTY>
<!ATTLIST nutrition
    calories CDATA #REQUIRED
    fat      CDATA #REQUIRED>
```

## A Recipe Document

```
<recipes>
  <recipe>
    <title>Zuppa Inglese</title>
    <ingredient name="egg yolks" amount="4"/>
    <ingredient name="milk" amount="2.5" unit="cup"/>
    <ingredient name="Savoiard biscuits" amount="21"/>
    <preparation>
      <step>Warm up the milk in a sauce pan.</step>
      <step>In a large bowl beat the egg yolks with the sugar.</step>
    </preparation>
    <comment>Refrigerate for at least 4 hours.</comment>
    <nutrition calories="612" fat="49"/>
  </recipe>
</recipes>
```

# Document Nodes Are Ordered

## *Document order*

- *Element* e1 is “before” e2 if the opening tag of e1 occurs before the opening tag of e2
- *Element* e is “before” its *attributes*  
*(order on attributes is implementation dependent, but most often attributes are ordered according to their occurrence)*
- The *attributes* of e are “before” the *child* elements of e
- If e1 is “before” e2, then all attributes of e1 are “before” all attributes of e2

*Reverse document order* is document order backwards

# Expressions

There are *two kinds* of expressions, returning either

- a *set of nodes* (= “node sets”), or
- a *value* (i.e., number, string, boolean)

**Mechanism:**

- specify node sets
- compute values from node sets
- use values in conditions that further constrain a node set

**Example:** `//recipe/nutrition[@calories > 1000]`

# The Basic Mechanism for Specifying Node Sets: Location Steps

## A **location step**

- goes in some *direction* (i.e., along some “axis”)
- leads to a node with a certain *property*

Properties can be specified by *node tests* and zero or more *predicates*.

Node tests test for

- *node types*: e.g., element (“\*”), text (“**text()**”),
- element or attribute *names*

Syntax: **<axis>::<test> [<pred1>] . . . [<predN>]**

# Location Steps: Examples

- **descendant::\***

all descendant elements

- **following-sibling::ingredient**

all “ingredient” siblings following in document order

- **following::text()**

all following text nodes

- **@\***

all attributes



# Location Steps: Examples (cntd.)

- **@amount**  
all “amount” attributes
- **descendant::ingredient[@amount=1.5]**  
all descendant elements with name “ingredient”  
where the attribute “amount” has the value 1.5
- **descendant::ingredient[position()=2]**  
the second descendant element with name “ingredient”
- **descendant::\*[self::ingredient][2]**  
same as above

# Steps Can be Combined to Paths

A path has a *starting point*, which can be

- the *root* of the document tree: "/"
- a "*current node*"

Example: `/descendant::recipe[1]`

`/child::ingredient[@unit="tablespoon"]`

`/@name`

“ / “ has *two meanings*:

- “*the root*” at the beginning of a path
- step *concatenation*

# Semantics of Steps and Paths (1)

- A step leads from a *node* (the “context node”) to a *set of nodes* (which may be empty)
- For any node  $n$ , and axis  $\alpha$ , there is the set of *nodes reachable from  $n$  via  $\alpha$* ,

denoted as  $R_\alpha(n)$

*(The definition of reachable nodes for an axis  $\alpha$  is more or less as one would expect. More later on.)*

# Semantics of Steps and Paths (2)

Consider a step  $S = \alpha :: \langle \text{test} \rangle [ \langle \text{pred} \rangle ]$

- If  $S$  starts from a node  $n$ , then it returns the set  $S(n)$  of all nodes in  $R_\alpha(n)$  that satisfy
  - the test and
  - the predicate
- The set  $S(n)$  is the *context* for each node in the set.

# Semantics of Steps and Paths (3)

A path  $P$  is a *sequence of steps*

$$P = S_1/S_2/\dots/S_n$$

A path defines a *set of nodes*  $P(n)$  as follows:

- If  $P$  consists of a *single step*  $S$ , then  $P(n) = S(n)$
- If  $P$  is a combined path  $P = P_0/S$ , then
$$P(n) = \text{Union of all } S(n_0) \text{ where } n_0 \text{ in } P_0(n)$$
- The *context* of a result node is determined by the *last step*

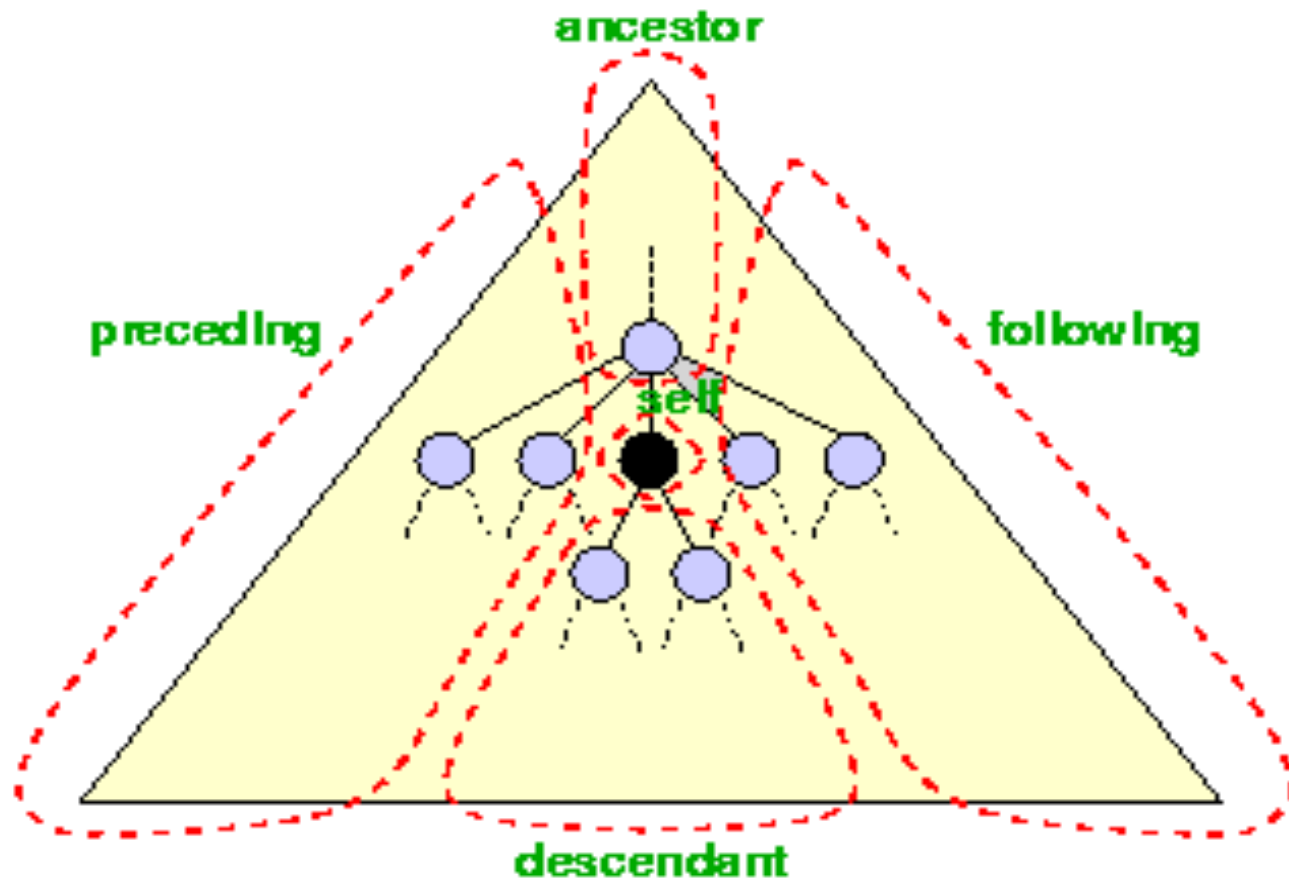
# Axes in XPath

- **child** the *children* of the context node
- **descendant** all *descendants* (children, children's children, ...)
- **parent** the *parent* (empty if at the root)
- **ancestor** all *ancestors* from the parent to the root
- **self** the *context node* itself
- **following-sibling** siblings to the *right*
- **preceding-sibling** siblings to the *left*

# Axes in XPath (cntd.)

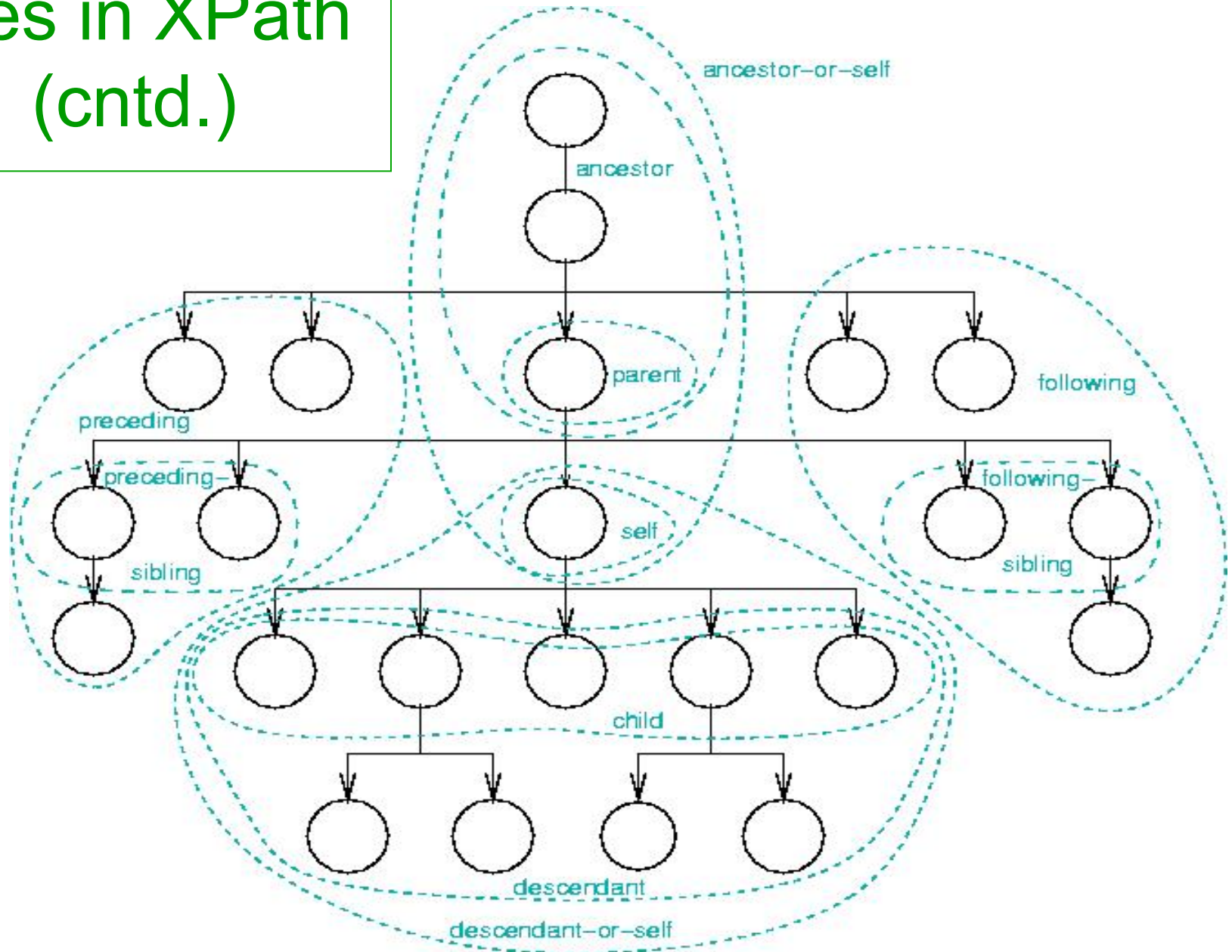
- **following** all *following* nodes in the document, excluding descendants
- **preceding** all *preceding* nodes in the document, excluding ancestors
- **attribute** the *attributes* of the context node
- **namespace** *namespace declarations* in the context node
- **descendant-or-self** the *union* of descendant and self
- **ancestor-or-self** the *union* of ancestor and self

# Axes in XPath (cntd.)





# Axes in XPath (cntd.)



# Ordering of Axes

What should be the meaning of

`/descendant::recipe[last()]`

`/preceding::recipe[2]` ?

**Forward axes:** child, descendant, following-sibling, following

**Reverse axes:** ancestor, preceding-sibling, preceding

- By *default*, the ordering of a node set is *document order*.
- If a node set has been obtained by a step along a **reverse axis**, it is in **reverse** document order.

# Node Tests

Testing by node type:

- `text()` character data nodes
- `comment()` comment nodes
- `processing-instruction()`  
processing instruction nodes
- `node()` all nodes (not including attributes and namespace declarations)

Testing by node name (for elements and attributes):

- `recipe` nodes with the name “recipe”
- `*` any element (\*) or attribute node (@\*)

# Node Tests (Exercises)

What is the meaning of

- `/descendant::text()` ?
- `/descendant::*` ?
- `/descendant::node()` ?
- `/descendant::*/@amount` ?
- `/descendant::*/@*` ?

# Shorthands

There are shorthands for moving along the descendant and the child axis

- `//` means `/descendant-or-self::node()/`
- `/recipes` means `/child::recipes`
- `/*` means `/child::*`
- `/node()` means `/child::node()`
- `.` means `self::node()`
- `..` means `parent::*`

# Shorthands: Exercises

- What is the difference between `//*` and `//.` ?
- What is the result of

`//*[2]` ?

`//self::*[2]` ?

`//*[2]/self::*` ?

- `//*` means `/descendant-or-self::node()/child::*`

Is this different from `/descendant::*` !

*Why?*

# Predicates

- Predicates are **expressions** of type **boolean**,  
*although they do not always look like that ...*
- A predicate **filters a node-set** by evaluating the predicate expression on each node in the set with
  - that **node** as the **context node**,
  - the **size** of the node-set as the **context size**, and
  - the **position** of the node in the node-set wrt. the axis ordering as the **context position**.
- Predicates can be **combined** with and, or, and not()  
*Expressions that are not boolean are **cast** to boolean*

# Casting of Node Sets (1)

- Casting of **node sets** to **boolean**
  - true, if the set is nonempty
  - false otherwise

- Example:

**/descendant::ingredient[@unit]**

means:

*ingredients having a unit attribute*



# Casting of Node Sets (2)

## Casting of *nodes* to *string*

- Every *text node* has a string as its *content*
- Every *element node* has a *string content*:
  - the strings occurring in the node and its descendants,
  - concatenated in document order
- Every *attribute node* has a string value  
(which may be empty)

# Casting of Node Sets (3)

Casting of **nodes** to **number**

- Interpret the string value as a number
- If not possible, value is NaN (= "*not a number*")

Casting of **node sets** to **string**, **number**, or **boolean**

- Take the value of the *first node*

wrt to document order

# Casting Between Values

- XPath has explicit **casting functions** for the value types boolean, string, and number
- Essentially, they work as one would expect.
  - Note: an **integer** in a predicate is interpreted as referring to the **position** of the context node
- Examples:
  - `string(true) = "true"`,     `string(0) = "0"`
  - `number(false) = 0`,     `number(true) = 1`,
  - `number("123") = 123`, `number("sugar") = NaN`

# Casting Between Values (cntd.)

- `boolean(0) = false`,      `boolean(2) = true`,  
    `boolean(NaN) = false`
- `boolean("") = false`,      `boolean("false") = true`

What is the meaning of

- `/descendant::recipe/title["Ricotta Pie"]` ?

And what about

- `/descendant::recipe/title[self::*="Ricotta Pie"]` ?

# Equalities

- Things become more complicated if a node set is involved in an equality:

$$\langle \text{node set} \rangle = \langle \text{value} \rangle$$

means:

*“The  $\langle \text{node set} \rangle$  contains some node that has the value  $\langle \text{value} \rangle$  after casting.”*

- Similarly, the test

$$\langle \text{node set 1} \rangle = \langle \text{node set 2} \rangle$$

succeeds if

*“There is a  $\text{node1}$  in  $\langle \text{node set 1} \rangle$ ,  $\text{node2}$  in  $\langle \text{node set 2} \rangle$  s.t. the string content of  $\text{node1}$  and  $\text{node2}$  is equal”*

# Examples

- “Recipes where sugar is *one* of the ingredients”

`/descendant::recipe[ingredient/@name = "sugar"]`

- “Recipes with *some* ingredient *other than* sugar”

`/descendant::recipe[ingredient/@name != "sugar"]`

- “Recipes where sugar is *the only* ingredient”

`/descendant::recipe[not(ingredient/@name != "sugar")]`

# Exercise

What is the meaning of

```
/descendant-or-self::*
```

```
[descendant-or-self::node() = "Zuppa Inglese"] ?
```

What of

```
/descendant-or-self::*
```

```
[descendant-or-self::* = "Zuppa Inglese"] ?
```

And what about

```
/descendant-or-self::node()
```

```
[descendant-or-self::node() = "Zuppa Inglese"] ?
```

# Arithmetic Expressions

- XPath has *built-in functions* returning numbers, e.g.
  - position()** the position of the context node in the current node set
  - last()** the number of elements in the current node set
- With numbers and numeric functions one can build up *arithmetic expressions*
  - 2, 2 \* 2, last() div 2, last() - 1, last() - position()**



# Arithmetic Expressions

- A predicate that contains only a **numeric expression**, e.g.,  
`[last() -1]` ,  
is a *shorthand* for a **position predicate**, e.g.,  
`[position() = last() -1]` .
- Otherwise, numbers are cast to **boolean**.

**Exercise:** What is the meaning of

`//*[2 and ingredient]` ?

# Aggregation Functions

- The aggregation functions **count** and **sum** are applied to **node sets** and return **numbers**.
  - The count result is *always* a number.
  - The sum result is *only* a number *if every* node in the argument set can be *cast as a number*.
- Aggregation functions in a predicate refer to the current node set.
- Functions min, max, and avg do not exist in XPath  
(but in XQuery)

# Examples

What is the meaning of

- `sum(/descendant::ingredient  
[@unit="cup" and @amount]/@amount) ?`
- `//recipe[count(ingredient) > 5] ?`
- `//recipe[count(./ingredient) > 5] ?`

# XPath Expressions: Summary

An expression can be:

- a **constant**, e.g. "..."
- a **function call**: *function(arguments)*
- a **boolean expression**: **or, and, =, !=, <, >, <=, >=**  
(standard precedence, all left associative)
- a **numerical expression**: **+, -, \*, div, mod**
- a **node-set expression**: using location paths  
and “|” (set union)

# XPath Expressions: Summary

- Expressions have a type: *node-set* (set of nodes), *boolean* (true or false), *number* (floating point), or *string* (text)
- **Coercion/casting** may occur at function arguments and when expressions are used as predicates.
- Functions are evaluated using the **context**.

# Core function library (1)

- Node-set functions:
  - `last()` returns the context size
  - `position()` returns the context position
  - `count(node-set)` number of nodes in node-set
  - `name(node-set)` string representation of first node in node-set
  - `id(ID)` returns element with id *ID*
- String functions:
  - `string(value)` type cast to string
  - `concat(string, string, ...)` string concatenation

# Core function library (2)

- Boolean functions:

- `boolean(value)` type cast to boolean
- `not(boolean)` boolean negation
- `contains(string, substring)` substring test
- `starts-with(string, prefix)` prefix test

- Number functions:

- `number(value)` type cast to number
- `sum(node-set)` sum of number value of each node in node-set

# The Family DTD

```
<!DOCTYPE family [  
  <!ELEMENT family (person) *>  
  <!ELEMENT person (name) >  
  <!ELEMENT name (#PCDATA) >  
  <!ATTLIST person  
    id ID #REQUIRED  
    mother IDREF #IMPLIED  
    father IDREF #IMPLIED  
    children IDREFS #IMPLIED>  
>
```



# A Family Document

```
<family>
  <person id="lisa" mother="marge" father="homer">
    <name> Lisa Simpson </name>
  </person>
  <person id="bart" mother="marge" father="homer">
    <name> Bart Simpson </name>
  </person>
  <person id="marge" children="bart lisa">
    <name> Marge Simpson </name>
  </person>
  <person id="homer" children="bart lisa">
    <name> Homer Simpson </name>
  </person>
</family>
```

# Family Exercise

- Return the children of Marge.
- Return the names of the children of Marge.
- Return the father of the children of Marge.

# Exercises

- Write XPath queries that ask for the following over the Recipes document:
  - The titles of all recipes, returned as strings.
  - The titles of all recipes that use olive oil.
  - The titles of all recipes that do not use olive oil.
  - The amount of sugar needed for Zuppa Inglese.
  - The recipes that have an ingredient in common with Zuppa Inglese.

# Exercises (cntd.)

- The number of recipes in the document.
- The last step in preparing Zuppa Inglese.
- The average fat content per recipe.
- The recipes with less than average fat content.
- The titles of recipes that have no compound ingredients.
- The titles of recipes where all top level ingredients are compound.
- The titles of recipes that have only non-compound ingredients.