Information Integration Part 2: Information Integration Models

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Information Integration

Il has the aim to provide **uniform access** to data that are stored in **a number** of **autonomous and heterogeneous** sources:

- different *data models* (structured, semi-structured, text)
- different schemata
- differences in the representation of values (km vs. miles, USD vs. EUR) and entities (addresses, dates, etc.)
- inconsistencies among the data

Il is a basic problem in

- Data Warehousing, Data Re-engineering
- Integration of data from scientific experiments
- E-commerce: Harvesting data on the Web



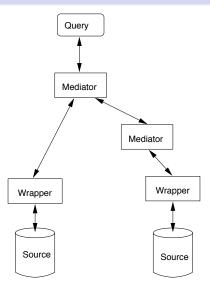
Architecture of a Mediator-based II System

The system generates an integrated, uniform view of a collection of sources

- Queries are formulated over a global schema domain model, domain schema, "mediated schema", ontology, enterprise model, ...
- Wrappers (= cover, envelop, encase) make sources accessible
- Mediators translate queries, combine answers of wrappers and mediators, resolve contradictions



Information Integration: Scenario



Movie Info: Global Schema [Idea by A. Halevy]

```
Movie(title, director, year, genre, rating)
```

```
Starring(title, actor)
```

```
Artist(name, yob, country)
```

```
Plays(title, language, cinema, startTime)
```

```
Cinema(cinema, location)
```

```
Review(title, rating, description)
```



Movie Info: Queries Over the Global Schema

• "Which films with Johnny Depp are shown in Bolzano at which time?"

Q(t, st) := Starring(t, 'Johnny Depp'), Plays(t, c, st),Cinema(c, 'Bolzano')

• "Which thrillers by an Italian director are shown in Bolzano at which time?"

Q(t, st) := Movie(t, d, y, 'Thriller'), Artist(d, 'Italy'),Plays(t, c, st), Cinema(c, 'Bolzano')



Movie Info: Sources

• Website Cineplexx Cinema, Bozen

CineplexxShowing(title, language, startTime) CineplexxDetails(title, director, genre) CineplexxCast(title, actor)

• Website Filmclub Cinema, Bozen

Filmclub(title, language, director, startTime)

Website Kinoliste

Kinoliste(city, cinema)

• Internet Movie Database

ImdbActor(name, yob)
ImdbStarring(name, title)
ImdbFilm1(title, stars, genre, director, year)
ImdbFilm2(title, actor)
ImdbReview(title, stars, description)

Website Kino München

KinoMuenchen(cinema, title, startTime)

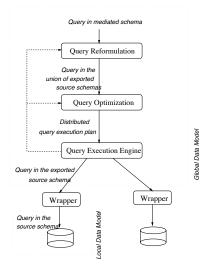


Approaches to II

- What does the II system contain?
 - \Rightarrow virtual vs. materialized integration
- Which operations are allowed on the global schema?
 ⇒ Read vs. Read and Write
- How is the II system *specified*?
 - \Rightarrow procedurally vs. **declaratively**
- How do we model the *connection* between sources and global schema?
 ⇒ global schema in terms of the sources
 vs. sources in terms of the global schema



Architecture of a Virtual Integration System



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Questions about II [M. Lenzerini]

- How to construct the global schema
- (Automatic) source wrapping
- How to express mappings between sources and global schema
- How to discover mappings between sources and global schema
- How to deal with limitations in mechanisms for accessing sources
- Data extraction, cleaning, and reconciliation
- How to model the global schema, the sources, and the mappings
- How to answer queries expressed on the global schema
- How to exchange data according to the mappings
- How to optimize query answering
- How to process updates expressed on the global schema and/or the sources (read/write vs. read-only data integration)



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The Mediator (1)

The mediator

- provides an integrated access to the information sources
- hides the sources
- creates the illusion to query a unique database
- \rightsquigarrow the mediator presents to the user a *virtual db*
- → the virtual db is presented by a schema: the global or mediated schema

Depending on the application, several data models are possible:

relational, XML, description logics

Here: the global schema is a relational schema



The Mediator (2)

Function

- accepts a query over the global schema
- reformulates the query into queries over the sources
- determines an *execution plan*: in which *order* will the queries be posed over the sources?

(information flow size of the expected answers,

expected speed of the answer)

- sends queries to the sources (= wrappers)
- collects and combines the answers
- changes the plan during run time



Modeling the Information Content of Sources

2 approaches of mapping source schemas and global schema

Relations in the global schema are views of the sources:
 "global as view" (GAV)

traditional concept of a view

- Views are virtual relations the global schema describes a virtual DB
- Relations in the *sources* are *views of the global schema:* **"local as view**" (LAV)

apparently nonsensical

• sources are materialized views of a db, which is not accessible itself

There is also a combination of the two, called GLAV



Logical Query Planning

In a standard database setting (centralized or distributed):

- Given: a declarative query over the logical schema
- Wanted: a sequence of operations for retrieving data, operating on the physical schema:

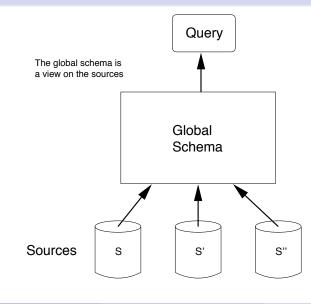
the execution plan

In information integration:

- Given: a declarative query over the global schema
- Wanted: an "equivalent" declarative query over the local schemas: the logical plan
- The logical plan can be transformed into an execution plan with (more or less) standard techniques



Global as View: Idea



Global as View: Example (1) [J. Ullman]

Sources: S_1 , S_2 , S_3 contain info on *employees* e, *phone numbers* p, *managers* m, *offices* o, *departments* d. Thus, the source schema is:

 $S_1(e, p, m)$ $S_2(e, o, d)$ $S_3(e, p),$

where variable names indicate the meaning of the positions.

Global Schema: We combine the three sources into a global schema with the two relations EPO and EDM:

$$\begin{split} & \texttt{EPO}(e, p, o) \coloneqq \texttt{S}_1(e, p, m), \, \texttt{S}_2(e, o, d) \\ & \texttt{EPO}(e, p, o) \coloneqq \texttt{S}_3(e, p), \, \texttt{S}_2(e, o, d) \\ & \texttt{EDM}(e, d, m) \coloneqq \texttt{S}_1(e, p, m), \, \texttt{S}_2(e, o, d) \end{split}$$

EPO und EDM are described by views on the sources



Global as View: Example (2)

Query 1: "What are Sally's phone and office?"

 $Q_1(p, o) := EPO('Sally', p, o)$

We obtain a plan P_1 for Q_1 if we expand the body of Q_1 , by unfolding the predicate EPO:

$$\begin{split} P_1(p,o) &:= \mathtt{S}_1(\textit{'Sally'}, p, m), \, \mathtt{S}_2(\textit{'Sally'}, o, d) \\ P_1(p,o) &:= \mathtt{S}_3(\textit{'Sally'}, p), \, \mathtt{S}_2(\textit{'Sally'}, o, d) \end{split}$$



Global as View: Example (3)

Query 2: "What are Sally's office and department?"

 $Q_2(o,d) := \text{EPO}('Sally', p, o), \text{EDM}('Sally', d, m)$

Again, if we expand the body of Q_2 unfolding the definitions of EPO and EDM, we obtain a plan P_2 for Q_2 :

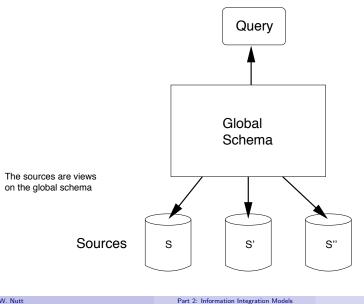
$$\begin{split} P_2(o,d) &:= \mathtt{S}_1(\textit{'Sally'}, p1, m1), \, \mathtt{S}_2(\textit{'Sally'}, o, d), \\ & \mathtt{S}_1(\textit{'Sally'}, p2, m2), \, \mathtt{S}_2(\textit{'Sally'}, o, d) \\ P_2(o,d) &:= \mathtt{S}_3(\textit{'Sally'}, p1), \, \mathtt{S}_2(\textit{'Sally'}, o, d), \\ & \mathtt{S}_1(\textit{'Sally'}, p2, m), \, \mathtt{S}_2(\textit{'Sally'}, o, d) \end{split}$$

But: Wouldn't a single plan be sufficient

$$P'_2(o,d) := S_2('Sally',o,d)?$$



Local as View: Idea



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Local as View: Example (1)

Sources: Again, we have the same three sources S_1 , S_2 , S_3 :

$$S_1(e, p, m)$$
 $S_2(e, o, d)$ $S_3(e, p)$

Global Schema: We model the application domain by five relations:

- Emp(e): e is an employee
- Phone(e, p): e has phone number p
- Office(e, o): e has office o
- Mgr(e, m): m is e's manager
- Dept(e, d): d is e's department



Local as View: Example (2)

Source Descriptions: We describe the sources as being included in views on the global schema:

$$\mathbf{S}_1 \subseteq V_1$$
 $\mathbf{S}_2 \subseteq V_2$ $\mathbf{S}_3 \subseteq V_3$.

The views have the following definitions:

$$V_1(e, p, m) := \operatorname{Emp}(e), \operatorname{Phone}(e, p), \operatorname{Mgr}(e, m)$$

 $V_2(e, o, d) := \operatorname{Emp}(e), \operatorname{Office}(e, o), \operatorname{Dept}(e, d)$
 $V_3(e, p) := \operatorname{Emp}(e), \operatorname{Phone}(e, p)$



Local as View: Example (3)

Query 3: "What are Sally's phone and office?"

```
Q_3(p,o) := \text{Phone}('Sally', p), \text{Office}('Sally', p)
```

Problem: No source contains complete information about phone numbers and offices. Moreover, the information we are looking for is always combined with other information.

Idea: Use the views to construct queries that are equivalent or more specific than Q_3 :

$$P_{3}(p, o) := V_{1}('Sally', p, m), V_{2}('Sally', o, d)$$

$$P_{3}(p, o) := V_{3}('Sally', p), V_{2}('Sally', o, d).$$

How can we test that P_3 is equivalent to or more specific than Q_3 ? \sim Unfold the views!



Local as View: Example (4)

Unfolding: We use the superscript .^{unf} to indicate unfolding using definitions:

$$\begin{split} P_3^{unf}(p,o) &:= \texttt{Emp}(\textit{'Sally'}), \texttt{Phone}(\textit{'Sally'},p), \texttt{Mgr}(\textit{'Sally'},d), \\ & \texttt{Emp}(\textit{'Sally'}), \texttt{Office}(\textit{'Sally'},o), \texttt{Dept}(\textit{'Sally'},d) \end{split}$$

$$\begin{split} P_3^{unf}(p,o) &:= \operatorname{Emp}(\,\, 'Sally'), \, \operatorname{Phone}(\,\, 'Sally',p), \\ & \qquad \operatorname{Emp}(\,\, 'Sally'), \, \operatorname{Office}(\,\, 'Sally',o), \, \operatorname{Dept}(\,\, 'Sally',d) \end{split}$$

Each rule of P_3^{unf} has "more" (in the sense of " \supseteq ") conditions than Q_3 :

- $\Rightarrow Q_3$ contains each rule of P_3^{unf}
- $\Rightarrow Q_3 \text{ contains } P_3^{unf}$



Local as View: Example (5)

Query 4: "What are Sally's office and department?"

 $Q_4(o,d) := \text{Office}('Sally', o), \text{Dept}('Sally', d)$

Office and departments are only mentioned in V_2 . Hence:

$$P_4(o,d) := V_2($$
'Sally', o,d)

Unfolding:

$$P_{4}^{unf}(o,d) := \text{Emp}('Sally'), \, \texttt{Office}('Sally',o), \, \texttt{Dept}('Sally',d)$$

Again, the plan is contained in the query, thus okay



Global as View vs. Local as View

Global as View:

- + query reformulation is simple: unfold (... and simplify!)
- + **abstracts** from *irrelevant information* in the sources

(e.g., can forget attributes)

- changes in the sources affect the global schema
- connections between the sources
 need to be taken into account when setting up the schema ("query reformulation at design time")

Local as View:

+ modularity and reusability:

when a source changes, only its description needs to be changed

- + connections between the sources can be inferred
- query processing is difficult: "query reformulation at run time"



Questions

We started with queries Q over the global schema and transformed them to queries Q^\prime over the sources

Are these transformations

• correct?

that is, are all answers to Q' also answers to Q?

• complete?

that is, will Q' retrieve all (sensible) answers for Q?

generally computable?

 \rightsquigarrow What at all are answers for Q?



Information Integration Systems

Here: formal framework for

- defining the problems of II (= information integration)
- developing and comparing techniques
- comparing approaches

Ideas:

- sources are accessed by means of a **global schema** *G*, which describes a virtual db
- $\bullet\,$ the instance ${\bf J}$ of the virtual db is unknown
- the source instance I *restricts* the possible global instances J \rightsquigarrow how can one model the connection between sources and virtual db?
- $\rightsquigarrow\,$ Queries over ${\cal G}$ must be answered with incomplete information



Incomplete Information

Schema

```
Person(fname, surname, city, street)
City(cname, population)
```

We know

- Mair lives in Bozen (but we don't know first name and street)
- Carlo Rossi lives in Bozen (but we don't know the street)
- Mair and Carlo Rossi live in the same street (but we don't know which)
- Maria Pichler lives in Brixen
- Bozen has a population of 100,500
- Brixen has a population < 100,000 (but we don't known the number)

Queries

- Return first name and surname of people living in Bozen!
- In the surnames of people living in Bozen!
- Who (surname) is living in the same street as Mair?
- Which people are living in a city with less than 100,000 inhabitants?



Incomplete Information: Questions

How can we represent this info?

- What does the representation look like?
- What is its meaning?
- What answers should the queries return?
- How can we define the semantics of queries?



Modeling Incomplete Information: SQL Nulls

Person

fname	surname	city	street
NULL	Mair	Bozen	NULL
Carlo	Rossi	Bozen	NULL
Maria	Pichler	Brixen	NULL

City

cname	population	
Bozen	100,500	
Brixen	NULL	

Intuitive meaning of NULL: one of

- (i) does not exist
- (ii) exists, but is unknown
- (iii) unknown whether (i) or (ii)



Databases and Queries

SQL Nulls: Formal Semantics

- dom (or, equivalenty, every type) is extended by a new value: NULL
- built-in predicates are evaluated according to a 3-valued logic with truth values *false < unknown < true*
- atoms with NULL evaluate to unknown
- Boolean operations:
 - AND/OR correspond to min/max on truth values
 - NOT extends the classical definition by NOT(unknown) = unknown
- additional operation $ISNULL(\cdot)$ with ISNULL(v) = true iff v is NULL
- a query returns those tuples for which query conditions evaluate to true



SQL Nulls: Example Queries

- Query 1 returns (NULL, Mair) and (Carlo, Rossi)
- Query 2 returns Mair and Rossi
- Queries 3 and 4 return nothing



Representation Systems [Imieliński/Lipski, 1984]

Distinguish between

- semantic instances, which are the ones we know
- syntactic instances, which contain tuples with variables (written \perp_1, \perp_2, \ldots)

A syntactic instance represents many semantic instances

Syntactic instances are called multi-tables (i.e., several tables).

There are three kinds of (multi-)tables: Codd Tables: a variable occurs no more than once Naive or Variable Tables: a variable can occur several times Conditional Tables: variable table where each tuple \bar{t} is tagged with a boolean combination $cond(\bar{t})$ of built-in atoms

Short names: table, v-table, c-table



Semantics of Tables

Let **T** be a multi-table with variables $var(\mathbf{T})$. For an assignment $\alpha: var(\mathbf{T}) \rightarrow \mathbf{dom}$ we define

```
\alpha \mathbf{T} = \{ \alpha \, \overline{t} \mid \overline{t} \in \mathbf{T}, \ \alpha \models cond(\overline{t}) \}
```

Then **T** represents the infinite sets of instances

$$rep(\mathbf{T}) = \{ \alpha \mathbf{T} \mid \alpha : var(\mathbf{T}) \rightarrow \mathbf{dom} \}$$
$$Rep(\mathbf{T}) = \{ \mathbf{J} \mid \mathbf{I} \subseteq \mathbf{J} \text{ for some } \mathbf{I} \in rep(\mathbf{T}) \}$$

where

rep(T) is the *closed-world* interpretation of T Rep(T) is the *open-world* interpretation of T

(Many results hold for both, the closed-world and the open-world interpretation. We assume open-world interpretation if not said otherwise.)

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Certain and Possible Answers

Given **T** and a query Q, the tuple \overline{c} is

• a certain answer (for Q over T) if

 \bar{c} is returned by Q over all instances represented by ${\bf T}$

• a possible answer if

 \bar{c} is returned by Q over some instance represented by ${\bf T}$

We denote the set of all certain answers as $cert_{T}(Q)$.

We have

$$cert_{\mathsf{T}}(Q) = \bigcap_{\mathbf{J} \in Rep(\mathsf{T})} Q(\mathbf{J})$$



Modeling Incomplete Information: Codd-Tables

Person

fname	surname	city	street
\perp_1	Mair	Bozen	\perp_2
Carlo	Rossi	Bozen	\perp_3
Maria	Pichler	Brixen	⊥₄

City

cname	population
Bozen	100,500
Brixen	\perp_5

Certain answers for our example queries:

- Query 1 returns (Carlo, Rossi)
- Query 2 returns Mair and Rossi
- Query 3 returns Mair
- Query 4 returns nothing



Modeling Incomplete Information: v-Tables

Person

fname	surname	city	street
\perp_1	Mair	Bozen	\perp_2
Carlo	Rossi	Bozen	\perp_2
Maria	Pichler	Brixen	\perp_4

City

cname	population
Bozen	100,500
Brixen	\perp_5

Certain answers for our example queries:

- Query 1 returns (Carlo, Rossi)
- Query 2 returns Mair and Rossi
- Query 3 returns Mair and Rossi
- Query 4 returns nothing



Modeling Incomplete Information: v-Tables

Person

fname	surname	city	street
\perp_1	Mair	Bozen	\perp_2
Carlo	Rossi	Bozen	\perp_2
Maria	Pichler	Brixen	\perp_4

City

cname	population	cond
Bozen	100,500	true
Brixen	\perp_5	$\perp_5 < 100,000$

Certain answers for our example queries:

- Query 1 returns (Carlo, Rossi)
- Query 2 returns Mair and Rossi
- Query 3 returns Mair and Rossi
- Query 4 returns Pichler



Strong Representation Systems

Definition

Let Q be a query and \mathbf{T} be a table. Then

$$Q(\mathbf{T}) := \{Q(\mathbf{I}) \mid \mathbf{I} \in rep(\mathbf{T})\}$$

That is, $Q(\mathbf{T})$ contains the relation instances obtained by applying Q individually to each instance represented by \mathbf{T} .

Note: $Q(\mathbf{T})$ is a set of sets of tuples, not a set of tuples!



Strong Representation Systems (cont)

Theorem (Imieliński/Lipski)

For every relational algebra query Q and every c-table ${\bf T}$ one can compute a c-table $\widetilde{{\bf T}}$ such that

$$rep(\widetilde{\mathbf{T}}) = Q(\mathbf{T})$$

That is,

- $\widetilde{\mathbf{T}}$ can be considered the answer of Q over \mathbf{T}
- the result of querying a c-table can be represented by a c-table
 → c-tables are a strong representation system

The downside:

• handling of c-tables is intractable:

the membership problem " $I \in rep(T)$ "? is NP-hard

• the c-tables $\widetilde{\mathbf{T}}$ may be very large



Weak Representation Systems: Motivation

Let $\boldsymbol{T}_{\rm v}$ be our example v-table and consider

$$\begin{aligned} Q_0 &= \sigma_{\texttt{city}=\texttt{'Bozen'}}(\texttt{Person}), \\ Q_1 &= \pi_{\texttt{sname}}(\sigma_{\texttt{city}=\texttt{'Bozen'}}(\texttt{Person})) \end{aligned}$$

Then: $cert_{T_v}(Q_0) = \{Mair\}$ and $cert_{T_v}(Q_1) = \{Mair, Rossi\}$

Observation: $Q_0 = \pi_{\text{sname}}(Q_1)$, but $cert_{T_v}(Q_0)$ cannot be computed from $cert_{T_v}(Q_1)$

Compositionality is violated! Better keep the nulls!

Idea: Try to keep enough information for representing certain answers!



Incomplete Databases: Definition

Definition (Incomplete Database)

An **incomplete database** is a set of instances $(\mathcal{I}, \mathcal{J})$.

For a query Q and an incomplete db $\mathcal I,$ the set of certain answers for Q over $\mathcal I$ is

$$cert_{\mathcal{I}}(Q) := \bigcap_{\mathbf{I} \in \mathcal{I}} Q(\mathbf{I}).$$



Weak Representation Systems

Let ${\cal L}$ be a query language (e.g., conjunctive queries, positive queries, positive relational algebra)

Definition (*L*-Equivalence)

Two incomplete databases \mathcal{I} , \mathcal{J} are \mathcal{L} -equivalent, denoted $\mathcal{I} \equiv_{\mathcal{L}} \mathcal{J}$, if for each $Q \in \mathcal{L}$ we have

 $cert_{\mathcal{I}}(Q) = cert_{\mathcal{J}}(Q)$

That is, $\mathcal L\text{-equivalent}$ incomplete dbs give rise to the same certain answers for all queries in $\mathcal L.$

Goal: For Q and **T**, find a **T**' such that **T**' is \mathcal{L} -equivalent to $Q(rep(\mathbf{T}))$, for a suitable \mathcal{L}



Weak Representation Systems (cntd)

 $\mathcal{L}_{\mathsf{calc}}^+$ language of positive relational calculus queries

Theorem (Imielinski/Lipski)

For every positive query Q and v-table ${\bf T},$ one can compute a v-table ${\bf T}'$ such that

$${\sf Rep}({f T}')\equiv_{{\cal L}^+_{\sf calc}}Q({\sf Rep}({f T}))$$

Proof.

Apply Q to **T**, treating variables like constants.

That is, **T**'

- contains enough information to compute certain answers to positive queries on Q(Rep(T))
- can be considered the answer of Q over **T**, in the context of positive queries



Source Descriptions in GLAV

GLAV combines the approaches "global as view" and "local as view"

The components are two schemas

- \mathcal{G} , the domain or global schema $(R \in \Sigma_{\mathcal{G}}, \text{ or } R \in \mathcal{G} \text{ (by abuse of notation)})$
- \mathcal{L} , the source or local schema $(S \in \Sigma_{\mathcal{L}}, \text{ or } S \in \mathcal{L} (\dots))$

and two sets of views (= relations defined by queries)

- \mathcal{W} , the domain or global views ($W \in \mathcal{W}$)
- \mathcal{V} , the source or local views $(V \in \mathcal{V})$

Here: no assumptions about the query languages of the views Later: Investigate the effects of the choice of language



Information Integration System (formally ...)

 An information integration system (IIS) I = (G, L, M) is given by two schemas G and L and a set M of mappings

$$V \subseteq W$$
 or $V = W$

involving source views V and domain views W

- A domain instance J interprets symbols $R \in \mathcal{G}$ and domain views $W \in \mathcal{W}$ as relations J(R) and J(W), resp.
- A source instance I interprets symbols $S \in \mathcal{L}$ und source views $V \in \mathcal{V}$ as relations I(S) and I(V), resp.
- \bullet A domain instance ${\bf J}$ is compatible with a source instance ${\bf I}$ if

$$\mathbf{I}(V) \subseteq \mathbf{J}(W)$$
 or $\mathbf{I}(V) = \mathbf{J}(W)$,

for every constraint $V \subseteq W$ or V = W, resp.



Special Case "Global as View"

- Domain views = global relations, that is, $W_{\!R}(ar{x}) \coloneqq R(ar{x})$
- per domain relation, there is exactly one source view, that is,

 $\mathcal{M} = \{ V_R \ \rho_R \ R \mid R \in \mathcal{G} \} \qquad \text{where } \rho_R \in \{ \subseteq, = \}$

" $V_R \subseteq R$ ": the mapping of R is sound

" $V_R = R$ ": the mapping of R is **exact**

Notation: Given a source instance I, we define

$$\mathcal{V}(\mathbf{I}) := \{ R(\overline{t}) \mid t \in V_R(\mathbf{I}), \ R \in \mathcal{G} \},\$$

the tuples mapped from ${\bf I}$ by the local views ${\mathcal V}$ to the global schema ${\mathcal G}$

Observation: J is compatible with I iff

- $\mathcal{V}(\mathbf{I}) \subseteq \mathbf{J}$ if all mappings are *sound*
- $\mathcal{V}(\mathbf{I}) = \mathbf{J}$ if all mappings are *exact*



Special Case "Local as View"

- Source views = local relations, that is, $V_S(\bar{x}) := S(\bar{x})$
- per source relation, there is exactly one domain view, that is,

 $\mathcal{M} = \{ S \ \rho_S \ W_S \mid S \in \mathcal{L} \} \qquad \text{where} \ \rho_S \in \{ \subseteq, = \}$

" $S \subseteq W_S$ ": the mapping of R is sound

" $S = W_S$ ": the mapping of R is **exact**

Notation: Given a domain instance J, we define

$$\mathcal{W}(\mathbf{J}) := \{ S(\overline{t}) \mid t \in W_S(\mathbf{J}), \ S \in \mathcal{L} \},\$$

the tuples mapped from ${\bf J}$ by the global views ${\mathcal W}$ to the local schema ${\mathcal L}$

Observation: J is compatible with I iff

- $\mathbf{I} \subseteq \mathcal{W}(\mathbf{J}) \qquad \text{if all mappings are } \textit{sound}$
- $\mathbf{I} = \mathcal{W}(\mathbf{J}) \qquad \text{ if all mappings are } \textit{exact}$



Certain Answers

Let $\mathcal{M} = \{V_i \ \rho_i \ W_i \mid i = 1, \dots, n\}$ be the set of mappings of an IIS

I a source instance

Q a query over \mathcal{G} (= the global schema)

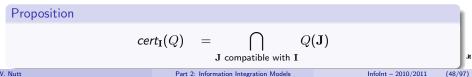
Definition (Certain Answers)

A tuple \overline{d} ist a **certain answer** for Q w.r.t. I if

 $d \in Q(\mathbf{J})$ for alle \mathbf{J} compatible with \mathbf{I} .

The set of all certain answers for Q w.r.t. I is denoted as

 $cert_{\mathbf{I}}(Q)$



Certain Answers under GAV

Let
$$\mathcal{M} = \{V_R \subseteq /= R \mid R \in \mathcal{G}\}$$
 be a set of GAV mappings

I a source instance

Q a query over \mathcal{G} (= the global schema)

 \rightsquigarrow When is a global instance ${\bf J}$ compatible with ${\bf I}?$

Exact Mappings: $\mathcal{V}(\mathbf{I}) = \mathbf{J}$

 \Rightarrow only one instance is compatible!

$$\Rightarrow cert_{\mathbf{I}}(Q) = Q(\mathcal{V}(\mathbf{I}))$$

Sound Mappings: $\mathcal{V}(\mathcal{I}) \subseteq \mathbf{J}$

 \Rightarrow supersets of $\mathcal{V}(\mathbf{J})$ are compatible

 \rightsquigarrow do we still have $cert_{\mathbf{I}}(Q) = Q(\mathcal{V}(\mathbf{I}))$?

GAV with sound mappings: \mathbf{J} compatible with \mathbf{I} iff $\mathcal{V}(\mathbf{I}) \subseteq \mathbf{J}$



GAV with Exact Mappings

Definition (Monotonic Query)

A query Q is monotonic if for all instances I_1 , I_2 we have

 $\mathbf{I}_1 \subseteq \mathbf{I}_2 \quad \Rightarrow \quad Q(\mathbf{I}_1) \subseteq Q(\mathbf{I}_2)$

- Datalog (= Horn clauses w/o function symbols) queries are monontonic
- Queries with negation are in general not monotonic

Proposition

Consider an IIS with exact GAV mappings and let ${\it Q}$ be a query. Then:

 $Q \text{ monotonic} \Rightarrow cert_{\mathbf{I}}(Q) = Q(\mathcal{V}(\mathbf{I}))$

If $cert_{\mathbf{I}}(Q) = Q(\mathcal{V}(\mathbf{I}))$, then we can compute the certain answers for Q by evaluating $Q' = Q \circ \mathcal{V}$ on the source instance \mathbf{I}

$$\rightsquigarrow \quad Q'$$
 is a "query plan" for Q

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How Difficult is Finding Certain Answers under Exact LAV?

Example: LAV with exact mappings (Abiteboul/Duschka)

1. Global relations model a coloured graph:

Edge(X, Y): there is an edge from vertex X to vertex Y Colour(X, Z): vertex X has colour Z

2. Source relations S_1 , S_2 , S_3 are mapped exactly by domain views W_1 , W_2 , W_3

$$\mathcal{M} = \{ S_1 = W_1, \ S_2 = W_2, \ S_3 = W_3 \},\$$

where

$$W_1(X) := \operatorname{Colour}(X, Y)$$
$$W_2(Y) := \operatorname{Colour}(X, Y)$$
$$W_3(X, Y) := \operatorname{Edge}(X, Y).$$

Thus, we have the vertices in S_1 , the colours in S_2 , the edges in S_3



Certain Answers under LAV? (Cont)

3. Source Instances.

Graph G = (V, E) (V are the vertices, E the edges)

Define the source instance \mathbf{I}_{G} by

$$\begin{split} \mathbf{I}_G(S_1) &:= V\\ \mathbf{I}_G(S_2) &:= \{\texttt{red}, \texttt{green}, \texttt{blue}\}\\ \mathbf{I}_G(S_3) &:= E. \end{split}$$

4. Compatible Instances.

A global instance ${\bf J}$ is compatible with ${\bf I}_{\it G}$ if

- J(Edge) contains exactly the edges in E
- J(Colour) assigns to the vertices of G the colours red, green, blue



Certain Answers under LAV? (Cont)

5. Query.

$$Q() \coloneqq \texttt{Edge}(X,Y), \texttt{Colour}(X,Z), \texttt{Colour}(Y,Z)$$

Q returns the answer () over ${f J}$ if and only if

 ${\bf J}$ contains neighbouring vertices $X,\,Y$ with the same colour

6. Certain Answers.

Observe, "()" is a certain answer for Q wrt I_G iff every colouring of G with three colours assigns the some colour to two neighbouring vertices

Thus: G is not 3-colourable iff $cert_{I_G}(Q) = \{()\}$



Certain Answers under LAV? (Cont)

3-Colorability is NP-complete

7. Conclusion.

To decide whether a tuple is a certain answer under LAV is coNP-hard, if sources are mapped **exactly**.

This holds already for

- relational conjunctive queries and
- views defined by relational conjunctive queries.

And what if the sources are not mapped exactly?



Computing Certain Answers under LAV

GAV:

- $\bullet\,$ certain answers for Q can in general be computed
 - by evaluating a query Q^\prime over the sources
- Q' results from Q by a simple transformation

 \rightsquigarrow is that also possible for LAV?

Problem with LAV and *exact* mappings:

If: $cert_{\mathbf{I}}(Q)$ can be computed by evaluating a query Q' over the sources Then: the problem " $\overline{d} \in cert_{\mathbf{I}}(Q)$ " is tractable (for a fixed Q)

(Evaluation of Datalog or PL1 queries is polynomial)

But: there is a conjunctive set of mappings \mathcal{M} und a conjunctive query Q, such that " $\overline{d} \in cert_{\mathbf{I}}(Q)$ " is coNP-hard



GAV and LAV

The approach for GAV was:

- $\bullet\,$ find prototypical database instance ${\bf J}_0$
- evaluate Q over $\mathbf{J}_0 \quad \rightsquigarrow \quad cert_{\mathbf{I}}(Q)$

To LAV, this can only be applied if mappings are sound, but not exact:

•
$$\mathcal{M} = \{S_i \subseteq W_i \mid S_i \in \mathcal{S}\}$$

 $\rightsquigarrow \mathbf{J} \text{ compatible with } \mathbf{I} \quad \text{ iff } \quad \mathbf{I} \subseteq \mathcal{W}(\mathbf{J})$

• Can we invert \mathcal{W} to \mathcal{W}^{-1} ?

 \rightsquigarrow If so, a compatible ${f J}$ would have to satisfy ${\mathcal W}^{-1}({f I})\subseteq {f J}$



Inverse Rules: Idea (1)

Example: global relation Edge, sources $S_1 \subseteq W_1$, $S_2 \subseteq W_2$ where

$$W_1(X) := \operatorname{Edge}(X, Z)$$

 $W_2(X, Y) := \operatorname{Edge}(X, Z) \wedge \operatorname{Edge}(Z, Y)$

Let ${\bf J}$ be defined as

$$\mathbf{J}(\texttt{Edge}) = \{ \langle a, b \rangle, \ \langle b, c \rangle, \ \langle c, d \rangle, \ \langle d, e \rangle \}$$

Let $\mathbf{I} := \mathcal{W}(\mathbf{J})$, that is,

$$\mathbf{I}(S_1) = \{a, b, c, d\}$$

$$\mathbf{I}(S_2) = \{\langle a, c \rangle, \langle b, d \rangle, \langle c, e \rangle\}$$

How far can we reconstruct ${\bf J}$ from ${\bf I}?$

Inverse Rules: Idea (2)

In W_1 , W_2 , there are existential variables

 $\Rightarrow~$ a compatible ${\bf J}$ must contain elements for these

Idea: Generate lost elements by Skolem functions

$$W_1(X) := \operatorname{Edge}(X, Z)$$

 $W_2(X, Y) := \operatorname{Edge}(X, Z) \wedge \operatorname{Edge}(Z, Y)$

 \rightarrow Inverse rules \mathcal{W}^{-1} for Edge:

$$\begin{split} & \texttt{Edge}(X, f(X)) \coloneqq S_1(X) \\ & \texttt{Edge}(X, g(X, Y)) \coloneqq S_2(X, Y) \\ & \texttt{Edge}(g(X, Y), Y) \coloneqq S_2(X, Y) \end{split}$$



Inverse Rules: Definition

Let the conjunctive domain view in the mapping $S\subseteq W$ be defined by

$$W(\bar{x}) := R_1(\bar{s}_1), \ldots, R_n(\bar{s}_n)$$

The inverse rules for W are

$$R_j(ar t_j)\coloneqq S(ar x), \qquad j=1,\ldots,n$$

where \bar{t}_j originates from \bar{x}_j as follows:

- ullet constants und distinguished variables from $ar{x}$ stay unchanged
- if $x \in \overline{s}_j$ is the *i*-th existential variable, say z_i ,

then x is replaced by Skolem term $f_i^S(\bar{x})$

Observation: for a collection of *conjunctive* views \mathcal{W} the set of rules \mathcal{W}^{-1} is *not* recursive



Inverse Rules: Example

For $\mathbf{J}_0:=\mathcal{W}^{-1}(\mathbf{I})$ we have

$$\begin{split} \mathbf{J}_{\mathbf{0}}(\mathsf{Edge}) &= \{ \langle a, f(a) \rangle, \ \langle b, f(b) \rangle, \ \langle c, f(c) \rangle, \ \langle d, f(d) \rangle, \\ \langle a, g(a, c) \rangle, \ \langle b, g(b, d) \rangle, \ \langle c, g(c, e) \rangle, \\ \langle g(a, c), c \rangle, \ \langle g(b, d), d \rangle, \ \langle g(c, e), e \rangle \} \end{split}$$

$$\begin{array}{ll} \text{Query:} & Q(X,Y) \coloneqq \text{Edge}(X,Z_1), \, \text{Edge}(Z_1,Y), \, \text{Edge}(Y,Z_2) \\ \text{Result:} & Q(\mathbf{J}_0) = \{ \langle a,c \rangle, \, \langle b,d \rangle, \, \langle c,e \rangle, \\ & \langle g(a,c), \, g(c,e) \rangle \} \end{array}$$

What happens for

$$\begin{array}{l} Q_1(X,Y) := {\tt Edge}(X,Z), \, {\tt Edge}(Z,Y) \\ Q_2(X,Y) := {\tt Edge}(X,Y), \, {\tt Edge}(Y,Z) \\ Q_3(X,Y) := {\tt Edge}(X,Y) \\ Q_3(X,Y) := {\tt Edge}(X,Z), \, Q_3(Z,Y) \end{array} ?$$



Inverse Rules: Idea (3)

Observation: In the examples, $Q(\mathcal{W}^{-1}(\mathbf{I}))$ returned certain answers ... and more

Idea: compute $Q(\mathcal{W}^{-1}(\mathbf{I}))$ — and remove the tuples with Skolem terms

Definition (Cutting out Skolem Terms)

 $(Q \circ \mathcal{W}^{-1})^{\downarrow}(\mathbf{I}) = \{ \overline{t} \in Q(\mathcal{W}^{-1}(\mathbf{I})) \mid \overline{t} \text{ contains no Skolem term} \}$

 $Q \circ \mathcal{W}^{-1}$ can itself be seen as a query:

Rules for $Q \circ \mathcal{W}^{-1}$ = Rules for $Q \cup$ inverse rules

Question (to be addressed later on):

Can we express $(Q \circ \mathcal{W}^{-1})^{\downarrow}$ as a conjunctive query?



Inverse Rules and Certain Answers

Proposition

 $\mathcal{W}^{-1}(\mathbf{I})$ is compatible with \mathbf{I}

Proof.

Let $\mathbf{J}_0 := \mathcal{W}^{-1}(\mathbf{I})$. We show that $\mathbf{I} \subseteq \mathcal{W}(\mathbf{J}_0)$. Let S be a source relation and $\overline{d} \in \mathbf{I}(S)$. Suppose the domain view W_S in the mapping " $S \subseteq W_S$ " $\in \mathcal{M}$ is defined as $W_S(\overline{x}) := R_1(\overline{s}_1), \ldots, R_n(\overline{s}_n)$. The inverse rules are $R_i(\overline{t}_i) := S(\overline{x})$. For \overline{d} the inverse rules generate the tuples $\overline{t}'_i := [\overline{x}/\overline{d}]\overline{t}_i \in \mathbf{J}_0(R_i)$, which originate from the \overline{t}_i , by replacing the x_j with d_j . For the assignment $\alpha = [x_1/d_1, \ldots, x_n/d_k, z_1/f_1^S(\overline{d}), \ldots, z_m/f_m^S(\overline{d})]$, we have $\mathbf{J}_0 \models \alpha(R_i(\overline{s}_i))$.

Thus, application of the rule for W_S gives $\overline{d} \in W_S(\mathbf{J}_0)$.

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Inverse Rules and Certain Answers

Corollary (Completeness)

Let $\ensuremath{\mathcal{W}}$ be the set of domain views describing the sources in a set of sound LAV mappings. Then

cert
$$_{\mathbf{I}}(Q) \subseteq (Q \circ \mathcal{W}^{-1})^{\downarrow}(\mathbf{I})$$

for all queries Q.

Proof.

 $\mathcal{W}^{-1}(\mathbf{I})$ compatible with $\mathbf{I} \Rightarrow cert_{\mathbf{I}}(Q) \subseteq Q(\mathcal{W}^{-1}(\mathbf{I}))$ No certain answer contains Skolem terms $\Rightarrow cert_{\mathbf{I}}(Q) \subseteq (Q \circ \mathcal{W}^{-1})^{\downarrow}(\mathbf{I})$



Inverse Rules and Certain Answers/2

Theorem (Soundness)

Let $\ensuremath{\mathcal{W}}$ be the set of domain views describing the sources in a set of sound LAV mappings. Then

$$(Q \circ \mathcal{W}^{-1})^{\downarrow}(\mathbf{I}) \subseteq cert_{\mathbf{I}}(Q)$$

for all relational conjunctive queries Q.

Proof will be added later. Uses the Universal Model Lemma below.



Inverse Rules and Certain Answers/3

 W^{-1} contains in its domain elements (Skolem terms) that are not in **dom** Let **sko** be the set of all Skolem terms.

Let J be a "normal" instance and J' an instance over $dom \cup sko.$

A homomorphism from \mathbf{J}' to \mathbf{J} is a mapping $\eta : \mathbf{sko} \to \mathbf{dom}$ such that $\eta A \in \mathbf{J}$ for every atom $A \in \mathbf{J}'$, that is $\eta R(\overline{t}) = R(\eta \overline{t}) \in \mathbf{J}$, whenever $R(\overline{t}) \in \mathbf{J}'$.

Remark

If we view Skolem terms as variables, then \mathbf{J}' is a v-(multi-)table.

In this perspective, there is a homomorphism from J' to J iff $J \in Rep(J)$.



Inverse Rules and Certain Answers/4

Lemma (Universal Model)

Let $\mathcal{I} = (\mathcal{G}, \mathcal{L}, \mathcal{M})$ be with sound LAV mappings and conjunctive views \mathcal{W} . Let I be a source instance and J be a global instance. Then the following are equivalent:

- $\textcircled{\textbf{0}} \ \textbf{J} \text{ is compatible with } \textbf{I} \ (\mathsf{wrt} \ \mathcal{I})$
- 2 there is a homomorphism from $\mathcal{W}^{-1}(\mathbf{I})$ to \mathbf{J}

Proof will be added later.



Query Plans: Definition

It would be nice to compute the certain answers for Q (or as many as possible) by running a (simple) query P on the sources.

Such a P could be considered a *logical plan* for answering Q

Definition

A query P over the source schema \mathcal{L} is a logical query plan for Q if

 $P(\mathbf{I}) \subseteq cert_{\mathbf{I}}(Q)$

for all source instances I.

How can one recognize that P is a query plan for Q?

 \rightsquigarrow Theory of query equivalence and containment

(67/97)

Containment and Equivalence Modulo a set of Views

 ${\mathcal G}$ global schema, ${\mathcal W}$ set of views over ${\mathcal G}$

P query over $\mathcal L$, Q query over $\mathcal G$

Definition

P is **contained in** Q **modulo** \mathcal{W} , denoted $P \subseteq_{\mathcal{W}} Q$, iff

 $P(\mathcal{W}(\mathbf{J})) \subseteq Q(\mathbf{J})$

for all instances ${\bf J}$ of ${\cal G}$

This means:

- We extend all J, using W, so that the source relations $S \in \mathcal{L}$ are interpreted, too Call the extensions J_W
- Then check " $P(\mathbf{J}_{\mathcal{W}}) \subseteq Q(\mathbf{J}_{\mathcal{W}})$ " for all \mathbf{J}

Analogously: P is equivalent to Q modulo \mathcal{W} , denoted $P \equiv_{\mathcal{W}} Q$



Query Plans and Containment Modulo a set of Views

Proposition (Plans are Contained)

If P is a plan for Q, then $P \subseteq_{\mathcal{W}} Q$.

Proof.

If **J** is a global instance, then $\mathcal{W}(\mathbf{J})$ is a source instance and **J** is compatible with $\mathcal{W}(\mathbf{J})$.

Thus: $P(W(\mathbf{J})) \subseteq cert_{W(\mathbf{J})}(Q) \subseteq Q(\mathbf{J}).$



Query Plans and Containment Modulo a Set of Views

Proposition (Monotonic Containees are Plans)

Let P be monotonic. Then

$$P \subseteq_{\mathcal{W}} Q \quad \Rightarrow \quad P \text{ is a plan for } Q$$

Proof.

Let I be a source instance. We show that $P(I) \subseteq cert_I(Q)$.

Let **J** be compatible with $\mathbf{I} \Rightarrow \mathcal{W}(\mathbf{J})$ is a source instance with $\mathbf{I} \subseteq \mathcal{W}(\mathbf{J})$. P monotonic $\Rightarrow P(\mathbf{I}) \subseteq P(\mathcal{W}(\mathbf{J}))$.

 $P \subseteq_{\mathcal{W}} Q \Rightarrow P(\mathcal{W}(\mathbf{J})) \subseteq Q(\mathbf{J}).$ Hence: $P(\mathbf{I}) \subseteq Q(\mathbf{J})$

 $\mathbf{J} \text{ was arbitrary } \Rightarrow P(\mathbf{I}) \subseteq \bigcap_{\mathbf{J} \text{ compatible with } \mathbf{I}} Q(\mathbf{J}) = cert_{\mathbf{I}}(Q)$

Query Plans and Containment Modulo a Set of Views/2

Proposition (Exact Mappings)

Suppose all LAV mappings in ${\mathcal W}$ are exact, Q is a query over the global schema, and P is a query over the sources. Then

 $P \subseteq_{\mathcal{W}} Q \quad \Rightarrow \quad P \text{ is a plan for } Q$

Proof.

Let I be a source instance. We show that $P(\mathbf{I}) \subseteq cert_{\mathbf{I}}(Q)$ J is a global instance compatible with $\mathbf{I} \Rightarrow \mathcal{W}(\mathbf{J}) = \mathbf{I}$ $P \subseteq_{\mathcal{W}} Q \Rightarrow P(\mathbf{I}) = P(\mathcal{W}(\mathbf{J})) \subseteq Q(\mathbf{J}).$ As before, this shows $P(\mathbf{J}) \subseteq cert_{\mathbf{I}}(Q)$

Thus: in the case of *monotonic plans* or *exact mappings*, logical query plans are characterized by "containment module W" \rightarrow how can we recognize "containment modulo W"? \rightarrow how can we generate plans for Q?



Reduction " $\subseteq_{\mathcal{W}}$ " \rightarrow " \subseteq "

Let P be a plan for Q

If the views in ${\mathcal W}$ are not recursive, we can **unfold** the relation symbols of the views occurring in P, that is, we can replace them by their definitions

Notation: P^{unf} is the unfolding of P

Clearly: $P \equiv_{\mathcal{W}} P^{unf}$

Consequence: $P \subseteq_{\mathcal{W}} Q$ iff $P^{unf} \subseteq Q$

What can we say about the



Unfolding Example (A. Halevy)

Global Relations

 $\begin{aligned} \mathtt{Cites}(x,y) & \text{ if } x \text{ cites } y \\ \mathtt{SameTopic}(x,y) & \text{ if } x \text{ and } y \text{ work on the same topic} \end{aligned}$

Query

Q(x,y) := SameTopic(x,y), Cites(x,y), Cites(y,x)

Global Views, describing two sources $W_1(u, v) := \text{Cites}(u, v), \text{Cites}(v, u)$ $W_2(u, v) := \text{SameTopic}(u, v), \text{Cites}(u, u'), \text{Cites}(v, v')$

Suggested Plan

 $P(x,y) := W_1(x,y), W_2(x,y)$



More Questions About Plans

- Can all certain answers be computed by plans?
- How many plans do we need?
- How can we compare plans?
- Is there a best set of plans?
- If so, how can we find it?



In LAV, the Certain Answer Function is Monotonic

We not that for sound LAV mappings, the function

 $\mathbf{I} \mapsto \mathit{cert}_{\mathbf{I}}(Q)$

is always monotonic

Proposition

Consider an IIS with sound LAV mappings and let Q be any query. Then

$$\mathbf{I} \subseteq \mathbf{I}' \qquad \Rightarrow \qquad \operatorname{cert}_{\mathbf{I}}(Q) \subseteq \operatorname{cert}_{\mathbf{I}'}(Q)$$

The same holds for GLAV systems where the source views are monotonic



Logical Plans and Certain Answers

Proposition

Let \mathcal{W} and Q be arbitrary. For every I and $d \in cert_{I}(Q)$ there exists a conjunctive plan P for Q such that

 $\bar{d} \in P(\mathbf{I})$

Proof.

Suppose
$$\mathbf{I}(S_i) = \{\overline{d}_{i,1}, \ldots, \overline{d}_{i,n_i}\}$$
 for $i \in [1,k]$

As on an earlier occasion, define \boldsymbol{P} as

$$P(\bar{d}) := W_1(\bar{d}_{1,1}), \dots, W_1(\bar{d}_{1,n_1}), \dots, W_k(\bar{d}_{k,1}), \dots, W_k(\bar{d}_{k,n_k})$$

Since $\bar{d} \in P(\mathbf{I})$, we only need to show that P is a plan for Q, that is, $P \subseteq_{\mathcal{W}} Q$. Let \mathbf{J} be a global instance.

 $\begin{array}{lll} \mathsf{Case 1:} & \mathbf{I} \subseteq \mathcal{W}(\mathbf{J}) \ \Rightarrow \ P(\mathcal{W}(\mathbf{J})) = \{\bar{d}\} \subseteq Q(\mathbf{J}), \ \text{since } \bar{d} \text{ is a certain answer} \\ \mathsf{Case 2:} & \mathbf{I} \not\subseteq \mathcal{W}(\mathbf{J}) \ \Rightarrow \ P(\mathcal{W}(\mathbf{J})) = \emptyset \subseteq Q(\mathbf{J}) \end{array}$

(76/97)

Complete Sets of Plans

Let ${\mathcal W}$ be a set of global views and Q be a query.

Then $|PLANS_{\mathcal{W}}(Q)|$ denotes the set of all conjunctive query plans for Q in the IIS with sound mappings defined by \mathcal{W} .

Definition

- A subset $\mathcal{P} \subseteq \operatorname{PLANS}_{\mathcal{W}}(Q)$ is complete if for every source instance I and every certain answer $\overline{d} \in \operatorname{cert}_{\mathbf{I}}(Q)$, there is a $P \in \mathcal{P}$ such that $\overline{d} \in P(\mathbf{I})$
- A complete set \mathcal{P} is **minimal** if no proper subset is complete.

Let ${\mathcal P}$ be a complete set of plans. Then for every Q and ${\mathbf I}$ we have

$$cert_{\mathbf{I}}(Q) = \bigcup_{P \in \mathcal{P}} P(\mathbf{I})$$

Do miminal complete sets of plans exist? What is their size?



Covering Sets of Plans

Definition

- $\mathcal{P} \subseteq \text{PLANS}_{\mathcal{W}}(Q)$ is covering if for every plan P'there are plans $P_1, \ldots, P_n \in \mathcal{P}$ such that $P' \subseteq P_1 \cup \cdots \cup P_n$
- $\mathcal{P} \subseteq \text{PLANS}_{\mathcal{W}}(Q)$ is dominating if for every plan P'there is a plan $P \in \mathcal{P}$ such that $P' \subseteq P$
- A covering (dominating) set is **minimal** if no proper subset is covering (dominating)
- Plan P is maximal if for every plan P' we have $P \subseteq P' \Rightarrow P' \subseteq P$

Proposition

Let \mathcal{P} be dominating set of plans and P be a maximal plan. Then \mathcal{P} contains a plan P' such that $P \equiv P'$.

How are complete, covering, and dominating sets of plans related?



Plans in the Relational Case

On this and the next slide, we assume that ${\mathcal W}$ and Q are relational and we consider only relational plans.

Theorem (Covering by Maximal Plans)

A covering set of plans is dominating.

A minimal covering set contains only maximal plans.

Proof.

Claim 1 holds because for relational conjunctive queries we have that $Q \subseteq Q_1 \cup \cdots \cup Q_n$ iff $Q \subseteq Q_i$ for some $i \in [1, n]$.

Claim 2 holds for all dominating sets in preorders.

Note that Claim 1 would not hold for conjunctive queries with disequations or comparisons



Plans in the Relational Case/2

Theorem (Maximal Plans are Small and Simple)

Let $P \in PLANS_{\mathcal{W}}(Q)$ be maximal. Then

- O P has at most as many atoms as Q
- $\ensuremath{\textcircled{0}}\ P \mbox{ contains only constants occurring in } Q \mbox{ or in } \mathcal{W} \label{eq:product}$

Proof.

Both claims follow from that fact that P is a plan iff $P^{unf} \subseteq Q$ iff there is a homomorphism from Q to P^{unf} .

The last two theorems tells us how we can compute, in principle, a minimal dominating (= covering) set of plans.

I am note aware that anyone has shown how difficult it is do decide whether a query over the sources is a maximal plan.



Questions about Logical Plans

- Given a set of views \mathcal{W} , how many maximal plans for Q are there? At most? At least?
- Is it also possible in an exact LAV setting to compute all certain answers by plans?
- What is the data complexity of deciding certain answers
 - in a sound LAV setting?
 - in an exact LAV setting?
- What can we say about the difficulty of computing certain answers in a sound LAV setting if
- the query can contain comparisons?
- the views can contain comparisons?



Plans and Rewriting Queries Using Views

The problem of computing logical query plans in a sound LAV setting is the same as the one to compute *rewritings* of a query Qusing views $W = \{W_1, \dots, W_n\}$.

A query R over the relations in \mathcal{W} is a (contained) rewriting of Q if

$$R^{unf} \subseteq Q.$$

It is an **exact** rewriting if

$$R^{unf} \equiv Q.$$

All results about covering, domininating, maximal plans etc.

can be rephrased as results about rewritings.



The "Bucket" Algorithm

The Bucket Algorithm was developed to generate query plans for the *Information Manifold* system, the first LAV integration system [Levy/Rajaraman/Ordille 1996].

Goal: Given a conjunctive query Q, compute a set $\mathcal{P} = \{P_1, \dots, P_n\}$ of plans for Q

> If Q is relational, we want \mathcal{P} to be covering wrt. " \subseteq " (*i.e.*, for every plan P for Q there is a P_i with $P \subseteq P_i$)



The "Bucket"-Algorithm in an Example

Global schema:

Registered(student, course, year) Course(course, number) Enrolled(student, department)

Sources S_1 , S_2 , S_3 , S_4 described by the views:

$$\begin{split} W_1(s,n,y) &\coloneqq \texttt{Registered}(s,c,y), \,\texttt{Course}(c,n), \, n \geq 500, \, y \geq 2007 \\ W_2(s,d,c) &\coloneqq \texttt{Enrolled}(s,d), \,\texttt{Registered}(s,c,y) \\ W_3(s,c,y) &\coloneqq \texttt{Registered}(s,c,y), \, y \leq 2005 \\ W_4(s,c,n) &\coloneqq \texttt{Enrolled}(s,\texttt{cs}), \,\texttt{Registered}(s,c,y), \\ &\quad \texttt{Course}(c,n), \, n \leq 100 \end{split}$$



The "Bucket"-Algorithm: 1st Step

Idea:

- for each atom in Q, collect the views that possibly can appear in a plan
- exploit: unfolded plans are homomorphic images of the query

For each relational atom $r(\bar{y})$ in the query, create a "bucket":

For atom $\left| \begin{array}{c} r(ar{y}) \end{array} \right|$ collect all instantiated views $W_i(\phi_i ar{x}_i)$ such that

- $\phi_i r(\bar{z})$ occurs in the body of $W_i(\phi_i \bar{x})$
- ullet there is a substitution heta with $heta r(ar y)=\phi_i r(ar z)$

i.e., $r(\bar{y})$ and $r(\bar{z})$ are unifiable, without instantiating existential variables in W_i

- ϕ_i and θ are as general as possible
- the comparisons on the variables of the two atoms are consistent



The "Bucket"-Algorithm: the Buckets

In our example: 3 buckets

Enrolled(s, cs)	Registered(s, c, 2010)	Course(c,n)
$W_2(s, \mathtt{cs}, C')$	$W_1(s, n', 2010)$	$W_1(s',n,y')$
$W_4(s,c',n')$		

The following views do not fit into the buckets:

 $W_2, W_4 \notin \text{BUCKET}(\text{Registered}(s, c, 2010)): Y \text{ cannot be instantiated}$ $W_3 \notin \text{BUCKET}(\text{Registered}(s, c, 2010)): \text{ comparisons for } n \text{ are inconsistent}$ $W_4 \notin \text{BUCKET}(\text{Course}(c, n)): \text{ comparisons for } n \text{ are inconsistent}$



The "Bucket"-Algorithm: 2nd Step

Combine the views in the buckets, 1st possibility:

$$P_1(S) := W_2(s, \mathtt{cs}, c'), W_1(s, n', 2010), W_1(s', n, y')$$

$$\begin{array}{lll} \mathsf{Unfold:} & P_1^{\mathit{unf}}(S) \coloneqq \fbox{Enrolled}(s, \mathsf{cs}) \\ & & & \\ \hline & & \\ & &$$

Clearly: there is a hom from Q to $P_1^{unf} \Rightarrow P_1$ is a plan for QMoreover: P_1 is equivalent to P'_1 :

$$P_1'(S) := W_2(s, \mathtt{cs}, c'), W_1(s, n', 2010)$$



The "Bucket"-Algorithm: 2nd Step (cont)

Combine the views in the buckets, 2^{nd} possibility:

 $P_2(S) := W_4(s, c', n'), W_1(s, n'', 2010), W_1(s', n, y')$

Unfold: $P_2^{unf}(S) := \overline{\text{Enrolled}(s, cs)}$, Registered (s, c', y_1) , Course(c', n'), n' < 100Registered $(s, c_2, 2010)$, Course (c_2, n'') , $n'' > 500, 2010 \ge 2007,$ Registered (s', c_3, y') , Course (c_3, n) , n > 500, u' > 2007Query: Q(S) := |Enrolled(s, cs) |, Registered(s, c, 2010) |, $\boxed{\texttt{Course}(c,n)}, n \geq 300$ Clearly: there is a hom from Q to $P_2^{unf} \Rightarrow P_2$ is a plan for Q P_2 can be optimized analogously to P_1



Observation

The Bucket Algorithm may find exponentially many plans

Example

 $Q(x_1,\ldots,x_n) := r_1(x_1),\ldots,r_n(x_n)$

With 2n Sources S_i , S'_i , $i = 1, \ldots, n$, where

 $W_i(x_i)$:- $r_i(x_i)$ and $W'_i(x_i)$:- $r_i(\bar{x}_i)$,

it finds 2^n plans

 $P(x_1,\ldots,x_n)$:- $ilde W_1(x_1),\ldots, ilde W_n(x_n),$ where $ilde W_i=W_i$ or $ilde W_i=W_i'.$

Note: for each plan P we have $P^{unf} = Q$

 \Rightarrow all plans are equivalent wrt. " $\equiv_{\mathcal{W}}$ ".

However: if we drop a plan, we lose certain answers

- \rightsquigarrow what is the meaning of " \equiv "?
- → what does the Bucket Algorithm compute?



What does the Bucket Algorithm Compute?

Clearly: Plans for Q (due to test $P^{unf} \subseteq Q$)

However: The original paper [Levy/Rajaraman/Ordille 1996] does not make statements about the semantics (in particular, not about completeness)

Theorem (Grahne/Mendelzon 1999)

For relational ${\mathcal W}$ and Q, the Bucket Algorithm returns a set of plans for Q that compute all certain answers.

- *Even:* Completeness holds as well if Q is *relational* and the views in \mathcal{W} contain *comparisons* over a dense order.
- **Open:** What does the Bucket Algorithm compute if Q contains comparisons? Under which conditions on Q is the set of plans complete?



Query Plans From Inverse Rules

Comparisons are conditions on the applicability of rules

(example only for W_1 and W_2)

$$egin{aligned} {
m Registered}(s, f_c(s, n, y), y) &:= W_1(s, n, y) \mid\mid y \geq 2007 \ {
m Course}(f_c(s, n, y), n) &:= W_1(s, n, y) \mid\mid n \geq 500 \ {
m Enrolled}(s, d) &:= W_2(s, d, c) \ {
m Registered}(s, c, f_y(s, d, c)) &:= W_2(s, d, c) \end{aligned}$$

Abduce the query plan from the query



Relational Query Languages: Overview

We consider the following classes of queries:

- CQ: relational conjunctive queries without built-ins
- CQ^{\leq} : conjunctive queries with comparisons
- CQ^{\neq} : conjunctive queries with disequations
- UCQ: **unions** of conjunctive queries, that is, disjunctions of conjunctive queries, or non-recursive Datalog queries
- datalog: Datalog queries, that is, queries defined by (possibly recursive) rules
 - FO: queries in **first-order logic**, that is, relational calculus queries



Certain Answers and Containment

Let \mathcal{Q}_1 , \mathcal{Q}_2 be query languages

Let CERT^{snd}(Q_1, Q_2) be the certain answer problem for sound source descriptions $W \subseteq Q_1$ und queries $Q \in Q_2$:

 $\begin{array}{ll} \mbox{Given:} & \mathcal{W} \subseteq \mathcal{Q}_1, \ Q \in \mathcal{Q}_2, \ \mbox{source instance I and tuple } \bar{d} \\ \mbox{Question:} & \bar{d} \in \textit{cert}_{\mathbf{I}}(Q) \ \ \mbox{w.r.t. } \mathcal{W}? \end{array}$

Let $CONT(Q_1, Q_2)$ be the **containment problem** for queries in Q_1 and Q_2 :

 $\begin{array}{ll} \mbox{Given:} & Q_1 \in \mathcal{Q}_1, \, Q_2 \in \mathcal{Q}_2 \\ \mbox{Question:} & Q_1 \subseteq Q_2? \end{array}$



Certain Answers and Containment (cntd)

Theorem (Abiteboul/Duschka 98)

- Let \mathcal{Q}_1 , $\mathcal{Q}_2 \in \{ CQ, CQ^{\neq}, PQ, datalog, FO \}$. Then
 - $\operatorname{CERT}^{snd}(\mathcal{Q}_1, \mathcal{Q}_2)$ and
 - CONT (Q_1, Q_2)

can be reduced to each other in polynomial time.



Complexity of the Containment Problem

"
$$Q \subseteq Q'$$
"

	Q'				
Q	CQ	CQ≤	UCQ	datalog	FO
CQ	NP	Π_2^P	NP	dec.	undec.
CQ≤	NP	Π_2^P	NP	dec.	undec.
UCQ	NP	Π_2^P	NP	dec.	undec.
datalog	dec.	undec.	dec.	undec.	undec.
FO	undec.	undec.	undec.	undec.	undec.

... and the certain answer problem



Reduction CERT^{*snd*}($\mathcal{L}_1, \mathcal{L}_2$) \rightarrow CONT($\mathcal{L}_1, \mathcal{L}_2$)

Given Q, W, I und \bar{d} with $I(S_i) = \{\bar{d}_{i,1}, \ldots, \bar{d}_{i,n_i}\}$ for $i \in [1, k]$ Define Q'' as

$$Q''(\bar{d}) := W_1(\bar{d}_{1,1}), \ldots, W_1(\bar{d}_{1,n_1}), \ldots, W_k(\bar{d}_{k,1}), \ldots, W_k(\bar{d}_{k,n_k})$$

Let $Q' := Q'' \cup W$. (If Q_1 is CQ, CQ^{\neq} or UCQ, then replace the view relations by their definitions.)

Show:
$$ar{d}\in {\it cert}_{f I}(Q)$$
 wrt. ${\cal W}$ iff $Q'\subseteq Q$

" \Rightarrow ": Let J be a global instance.

Case 1: $\mathbf{I} \not\subseteq \mathcal{W}(\mathbf{J}) \Rightarrow Q'(\mathbf{J}) = Q''(\mathcal{W}(\mathbf{J})) = \emptyset$ Case 2: $\mathbf{I} \subseteq \mathcal{W}(\mathbf{J}) \Rightarrow Q'(\mathbf{J}) = \{\overline{d}\} \subseteq Q(\mathbf{J})$, since \overline{d} is a certain answer Hence: $Q' \subseteq Q$

"\equiv: Let J be an instance with $\mathbf{I} \subseteq \mathcal{W}(\mathbf{J}) \Rightarrow \overline{d} \in Q''(\mathbf{I}) \subseteq Q''(\mathcal{W}(\mathbf{I})) = Q'(\mathbf{I})$ $Q' \subseteq Q \Rightarrow \overline{d} \in Q(\mathbf{J}).$ Hence: $\overline{d} \in cert_{\mathbf{I}}(Q)$



Reduction $CONT(Q_1, Q_2) \rightarrow CERT^{snd}(Q_1, Q_2)$

Let $Q_1 \in \mathcal{Q}_1, Q_2 \in \mathcal{Q}_2$ Let $\mathcal{W} := \{W\}$ be defined by Q_1 and $W(c) := Q_1(x), P(x), P(x)$ Define Q by Q_2 and $Q(c) := Q_2(x), P(x)$ After the unfolding: $W \in Q_1, Q \in Q_2$. Let I be an instance such that $I(W) := \{c\}$. **Show:** $Q_1 \subseteq Q_2$ iff $c \in cert_{\mathbf{I}}(Q)$ " \Rightarrow ": Let J be a global instance with $c \in \mathcal{W}(\mathbf{J}) \Rightarrow c \in Q(\mathbf{J})$ $\Rightarrow c \in cert_{I}(Q)$ " \Leftarrow ": $Q_1 \not\subseteq Q_2 \Rightarrow$ for a global **J** there is some d with $d \in Q_1(\mathbf{J}) \setminus Q_2(\mathbf{J})$ W.I.o.g., $\mathbf{J}(P) = \{d\} \Rightarrow \mathbf{I} \subseteq \mathcal{W}(\mathbf{J}) \text{ with } Q(\mathbf{J}) = \emptyset.$ Thus, $c \notin cert_{\mathbf{I}}(Q)$

