

Semantic Web Technologies

F-Logic Semantics

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1/18

Outline

F-Logic Semantics

Reducing F-Logic Programming to standard LP

2/18

F-Structures (I)

- ▶ Interpretations in F-Logic are called **F-structures**.

F-Structure

An **F-structure** is a tuple $\mathbf{I} = \langle U, \prec_U, \in_U, \mathbf{I}_F, \mathbf{I}_{\rightarrow}, \mathbf{I}_{\rightarrow\rightarrow} \rangle$.

- ▶ U is the domain,
- ▶ \prec_U is an irreflexive partial order on U ,
 - ▶ $a \preceq_U b$ when $a \prec_U b$ or $a = b$
- ▶ \in_U is a binary relation over $U \times U$, and
- ▶ $a \in_U b$ and $b \preceq_U c$ then $a \in_U c$.

4/18

Interpreting Symbols with \mathbf{I}_F

- ▶ \mathcal{F} is the set of function symbols of some F-Logic language

Interpretation of function symbols

\mathbf{I}_F interprets every n -ary function symbol $f \in F$ as an n -ary function over the domain U : $\mathbf{I}_F(f) : U^n \rightarrow U$

- ▶ Thus, constants are interpreted as elements of the domain

5/18

Interpreting Attributes with \mathbf{I}_{\rightarrow}

Interpretation of single-valued attributes

\mathbf{I}_{\rightarrow} interprets every **element of the domain** $u \in U$ as a partial function from U to U : $\mathbf{I}_{\rightarrow}(u) : U \rightarrow U$.

- ▶ Thus, \mathbf{I}_{\rightarrow} associates with **elements of the domain**,
- ▶ pairs $\langle u_0, u_1 \rangle$.

6/18

Interpreting Attributes with $\mathbf{I}_{\rightarrow\rightarrow}$

Interpretation of set-valued attributes

$\mathbf{I}_{\rightarrow\rightarrow}$ interprets every **element of the domain** $u \in U$ as a partial function from U to 2^U : $\mathbf{I}_{\rightarrow\rightarrow}(u) : U \rightarrow 2^U$.

- ▶ Thus, $\mathbf{I}_{\rightarrow\rightarrow}$ associates with **elements of the domain**,
- ▶ pairs $\langle u_0, \{u_1, \dots, u_n\} \rangle$.

7/18

Interpreting Variables

- ▶ Same as in FOL

Interpreting Variables

Given interpretation \mathbf{I} , a variable assignment B , and a term t , $t^{\mathbf{I},B}$ is defined as:

- ▶ $x^{\mathbf{I},B} = x^B$ for variable symbol x and
- ▶ $t^{\mathbf{I},B} = \mathbf{I}_F(f)(t_1^{\mathbf{I},B}, \dots, t_n^{\mathbf{I},B})$ for t is $f(t_1, \dots, t_n)$.

8/18

Satisfaction in F-Structures

Satisfaction of atomic formulas

Given $\mathbf{I} = \langle U, \prec_U, \in_U, \mathbf{I}_F, \mathbf{I}_P, \mathbf{I}_{\rightarrow}, \mathbf{I}_{\leftrightarrow} \rangle$, B a variable assignment, and ϕ a formula. $\mathbf{I}, B \models \phi$ if:

- ▶ $\mathbf{I}, B \models t_1 : t_2$ iff $t_1^{\mathbf{I},B} \in_U t_2^{\mathbf{I},B}$
- ▶ $\mathbf{I}, B \models t_1 :: t_2$ iff $t_1^{\mathbf{I},B} \preceq_U t_2^{\mathbf{I},B}$
- ▶ $\mathbf{I}, B \models t_1[t_2 \rightarrow t_3]$ iff $t_3^{\mathbf{I},B} = \mathbf{I}_{\rightarrow}(t_2^{\mathbf{I},B})(t_1^{\mathbf{I},B})$.
- ▶ $\mathbf{I}, B \models t_1[t_2 \leftrightarrow t_3]$ iff $\mathbf{I}_{\leftrightarrow}(t_2^{\mathbf{I},B})(t_1^{\mathbf{I},B})$ is defined and $t_3^{\mathbf{I},B} \in \mathbf{I}_{\leftrightarrow}(t_2^{\mathbf{I},B})(t_1^{\mathbf{I},B})$.

9/18

Extension to complex formulas

Satisfaction of Complex formulas

- ▶ $\mathbf{I}, B \models t_1 = t_2$ iff $t_1^{\mathbf{I},B} = t_2^{\mathbf{I},B}$,
- ▶ $\mathbf{I}, B \models \phi_1 \wedge \phi_2$ iff $\mathbf{I}, B \models \phi_1$ and $\mathbf{I}, B \models \phi_2$,
- ▶ $\mathbf{I}, B \models \phi_1 \vee \phi_2$ iff $\mathbf{I}, B \models \phi_1$ or $\mathbf{I}, B \models \phi_2$,
- ▶ $\mathbf{I}, B \models \neg\phi_1$ iff $\mathbf{I}, B \not\models \phi_1$,
- ▶ $\mathbf{I}, B \models \forall x(\phi_1)$ iff for every B' which is an x -variant of B , $\mathbf{I}, B' \models \phi_1$, and
- ▶ $\mathbf{I}, B \models \exists x(\phi_1)$ iff for some B' which is an x -variant of B , $\mathbf{I}, B' \models \phi_1$.

10/18

Reducing F-Logic to LP

- ▶ F-Logic Programming can be reduced to Logic Programming
 - ▶ Thus, F-Logic is syntactic sugar; it does not add anything in expressiveness
 - ▶ Reducing terms:
 - ▶ Map object IDs to constants
 - ▶ Map constructed terms to functions
 - ▶ Map variables to variables
- Thus, terms look exactly the same!
- ▶ Map atoms to atoms

12/18

Reducing F-Logic to LP (2)

- ▶ Each type of molecule is mapped to an atom:
 - ▶ $A:B$ maps to `_member(A,B)`
 - ▶ $A::B$ maps to `_subclass(A,B)`
 - ▶ $A[B \rightarrow C]$ maps to `_svatt(A,B,C)`
 - ▶ $A[B \rightarrow\rightarrow C]$ maps to `_mvatt(A,B,C)`
 - ▶ $A[B \Rightarrow C]$ maps to `_svattsig(A,B,C)`
 - ▶ $A[B \Rightarrow\Rightarrow C]$ maps to `_mvattsig(A,B,C)`
- Note that the name of the predicates does not really matter.
- ▶ You obtain LP rules by simply replacing terms, atoms and molecules as specified.
 - ▶ Axiomatize the semantics of the F-Logic is-a molecules:
`_subclass(X,Z) :- _subclass(X,Y), _subclass(Y,Z).`
`_member(X,Z) :- _member(X,Y), _subclass(Y,Z).`

13/18

Reducing F-Logic to LP (2)

- ▶ Axiomatize the semantics of the F-Logic is-a molecules:
`_subclass(X,Z) :- _subclass(X,Y), _subclass(Y,Z).`
`_member(X,Z) :- _member(X,Y), _subclass(Y,Z).`
- ▶ Axiomatize the semantics of the F-Logic functions:
 - ▶ `X≐Y :- _svatt(V,W,X), _svatt(V,W,Y).`
 - ▶ `or :- _svatt(V,W,X), _svatt(V,W,Y), X≠Y.`

14/18

Reducing F-Logic to LP (4)

```
_member(bob, empl).
_svatt(bob,name,"Bob").
_svatt(bob,age,40).
_svatt(bob,affiliation,cs1).
_member(mary,faculty).
_svatt(mary,affiliation,cs1).
_member(cs1,dept).
_svatt(cs1,dname,"CS").
_svatt(cs1,mngr,bob).

bob:empl[name->"Bob";
         age->40;
         affiliation->cs1].
mary:faculty[affiliation->cs1].
cs1:dept[dname->"CS";
         mngr->bob]].
```

15/18

Class information:

```
_svattsig(person,name,string).
_mvattsig(person,friends,person).
_mvattsig(person,children,child(person)).
_subclass(empl,person).
_svattsig(empl,affiliation,department).
_svattsig(empl,boss,empl).
_subclass(faculty,empl).
_svattsig(faculty,boss,faculty).
_svattsig(faculty,boss,manager).
_svatt(faculty,avgSalary,50000).
_svattsig(dept,mngr,empl).

person[name=>string;
        friends=>person;
        children=>child(person)].
empl::person[affiliation=>department;
             boss=>empl].
faculty::empl[boss=>(faculty,manager);
             avgSalary->50000].
dept[mngr=>empl].
```

16/18

Rule

```
_svatt(E,boss,M) :- _member(E,empl),_member(D,dept),
_svatt(E,affiliation,D), _svatt(D,mngr,M),
_member(M,empl).

E[boss->M] :- E:empl, D:dept,
E[affiliation->D[mngr->M:empl]].
```

17/18

Summary

[F-Logic Semantics](#)

[Reducing F-Logic Programming to standard LP](#)

18/18