

3)

~~Strong Connectivity (slides)~~

LAB 2

~~Write a Pseudo-Code~~

Bipartite Graph / 2-Colorability

+ write a Pseudo-Code using BFS (ASSUMING THAT THE GRAPH IS CONNECTED)

We run BFS with an extra array, COLOR[n]

s.t. ~~if (v, v') ∈ edge~~

~~if v' is added to L[i+1] then~~

$$Color[v'] = \begin{cases} \text{blue} & \text{if } i+1 \text{ is ODD} \\ \text{white} & \text{otherwise} \end{cases}$$

~~After and we check all edges~~

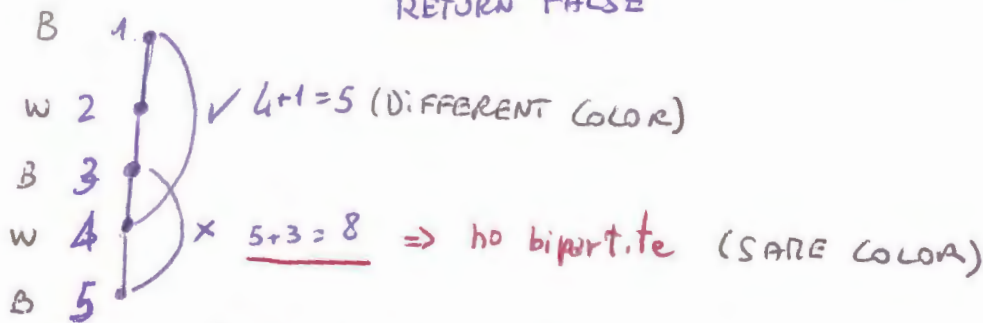
else ~~if~~ if Layer[v] = Layer[v'] then return FALSE

+ Write a PseudoCode using DFS-RECURSIVE

- We use the index associated by DFS to each node

- if (v, v') ∈ G and Explored(v) AND v' ∈ Stack  
v.index + v'.index is EVEN =>

RETURN FALSE



BIPARTITE-DFS(G)

For each v ∈ G do v.index = 0 /\* node is not explored  
index = 1

2COLOR(v), for some v ∈ G

2COLOR(v)

IF ODD index then

COLOR[v] = BLUE

ELSE

COLOR[v] = WHITE

v.index = index  
index = index + 1; S.push(v)

For each (v, v') ∈ G

IF v'.index = 0

2COLOR(v')

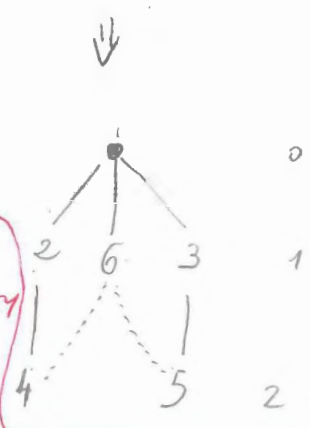
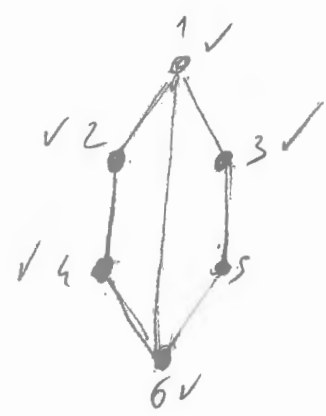
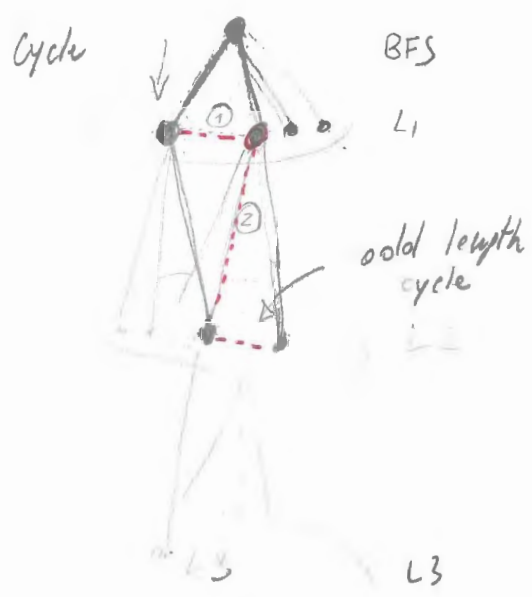
S.pop(v)

ELSE IF (v' ∈ Stack ∧

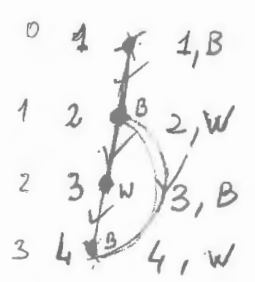
v'.index + v.index is EVEN)

Then return false

Cycles



check odd-length cycles using DFS  $\Rightarrow$  2-COLORABILITY



2COLOR(1)

2COLOR(2)

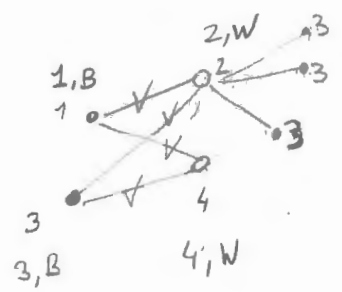
2COLOR(3)

2COLOR(4)

FAIL

INDEX = 1, 2, 3, 4, 5

4
3
2
1



2COLOR(1)

2COLOR(2)

2COLOR(3)

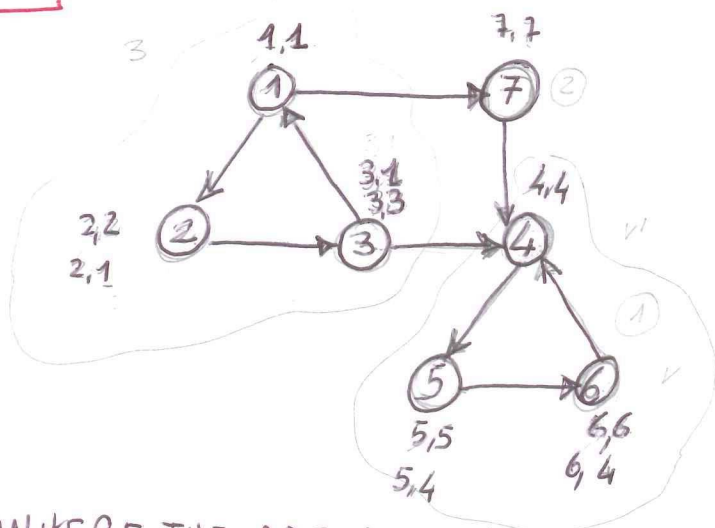
2COLOR(4)

INDEX = 1, 2, 3, 4

4
3
2
1

LAB 2

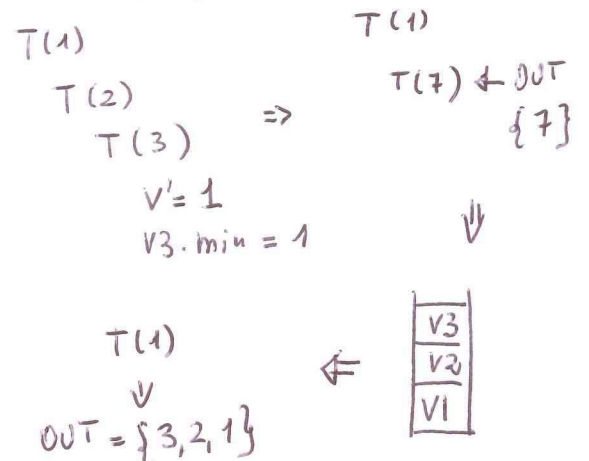
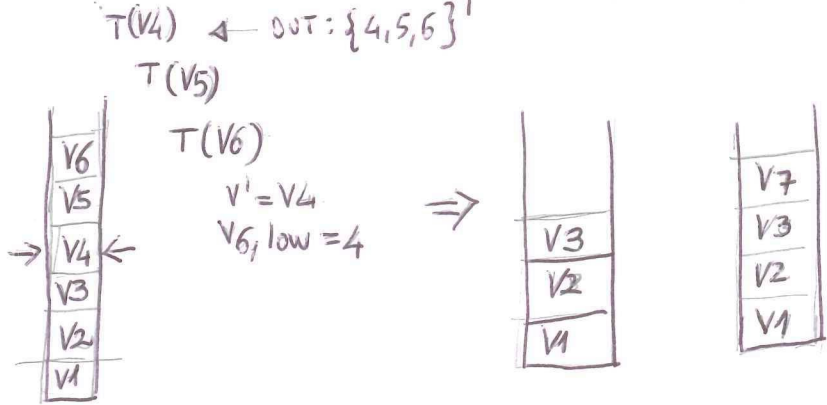
(4)



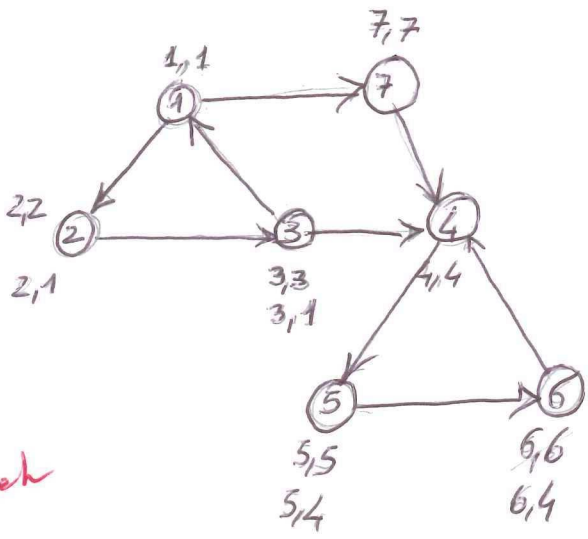
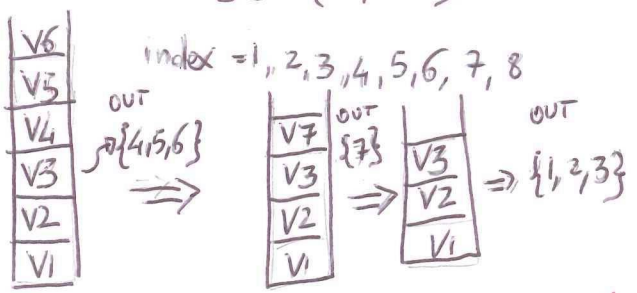
$i=0$   
 $i=1$   
 $i=2$   
 $i=3$

DIRECTED Graphs  
STRONG - COMPONENTS  
TARJAN - Algorithm

CASE WHERE THE ADJ for node 3 is :  $ADJ[3] = \{4, 1\}$



CASE WHERE  $ADJ[3] = \{1, 4\}$



- Show:
1. Nexting of recursive calls
  2. Value of the variables at each recursive call.
  3. Intermediate OUTPUT
  4. Stack.

Verove 2-SAT using TARJAN

see: <https://renzoggd.wordpress.com/2014/01/17/2-satisfiability/>

||

## LAB 3

### 1. TOPOLOGICAL ORDER

1.1. Modify the algorithm in the slides (3.1) ~~with~~ adding the array  $count[w]$  and a Stack  $S$  containing the nodes without incoming edges.

Assume we can check, given  $v$  vertices  $w$ ,  $\checkmark$ , whether  $(v, w) \in G$ .

1.2 Run the algorithm on the following DAG

