

# Search Based Software Engineering and Evolutionary Testing

---

Barbara Russo

SwSE - Software and Systems Engineering research group

---

# References

- Phil McMinn Search-Based Software Testing: Past, Present and Future, 2009
- Joachim Wegener, Oliver Bühler Evaluation of Different Fitness Functions for the Evolutionary Testing of an Autonomous Parking System, 2004

- Finding the optimal inputs for testing is a key issue that can be NP-hard
- Search based techniques can be leverage to find good inputs

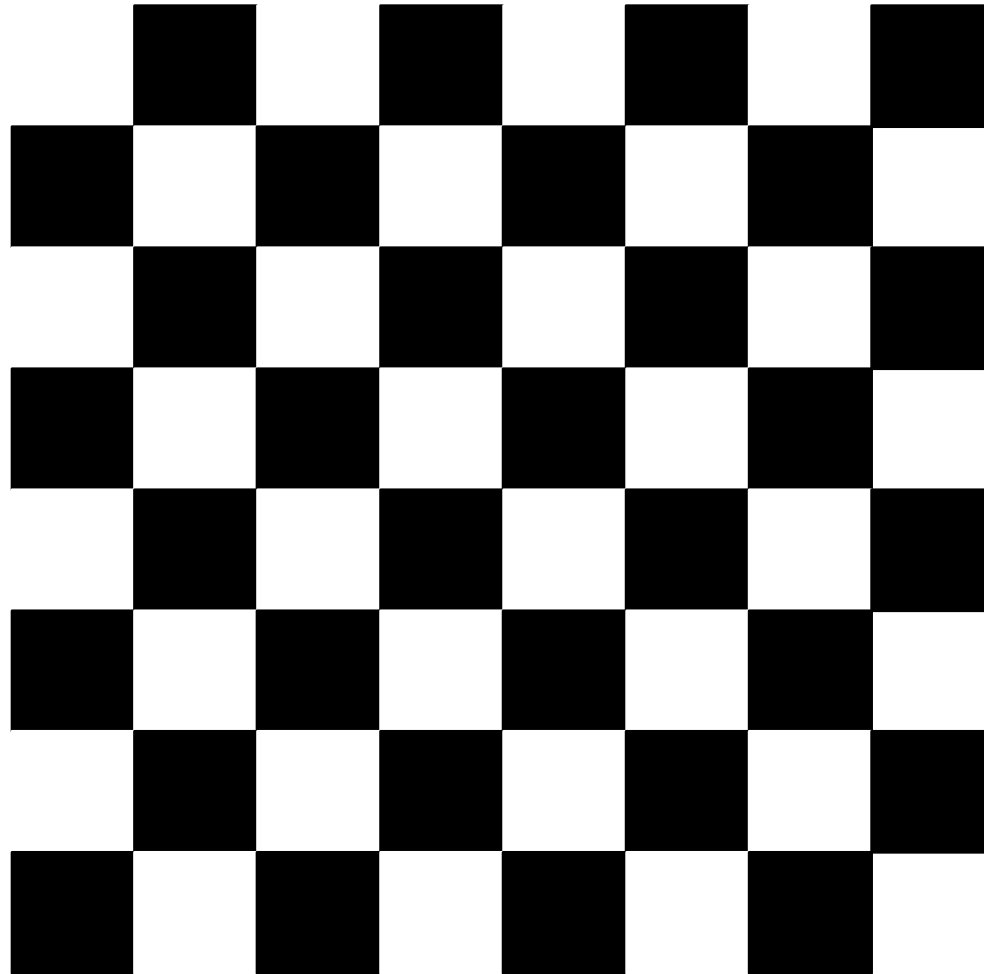
# What is SBSE

**Techniques to search large spaces** guided by a **fitness function** that captures **properties** of the software artefacts we seek for

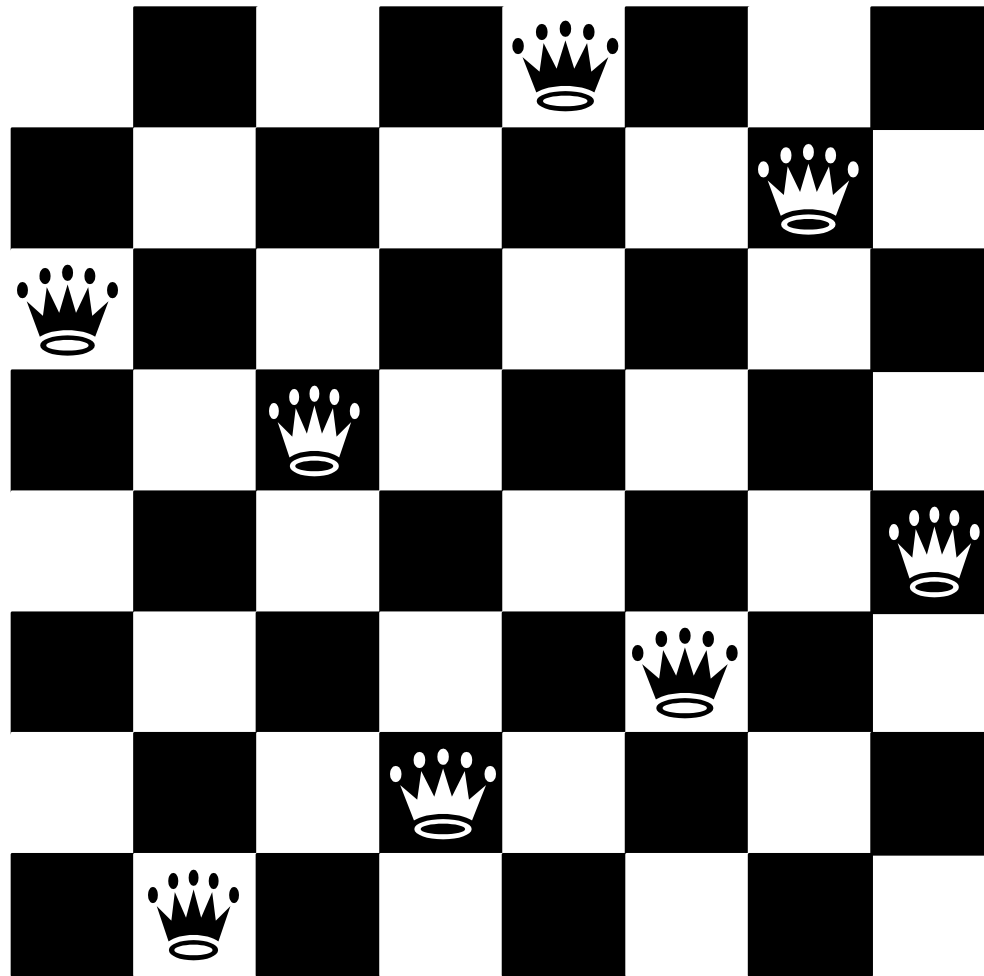
# Example - the search

Place  $n$  queens on a board so that there is no attack

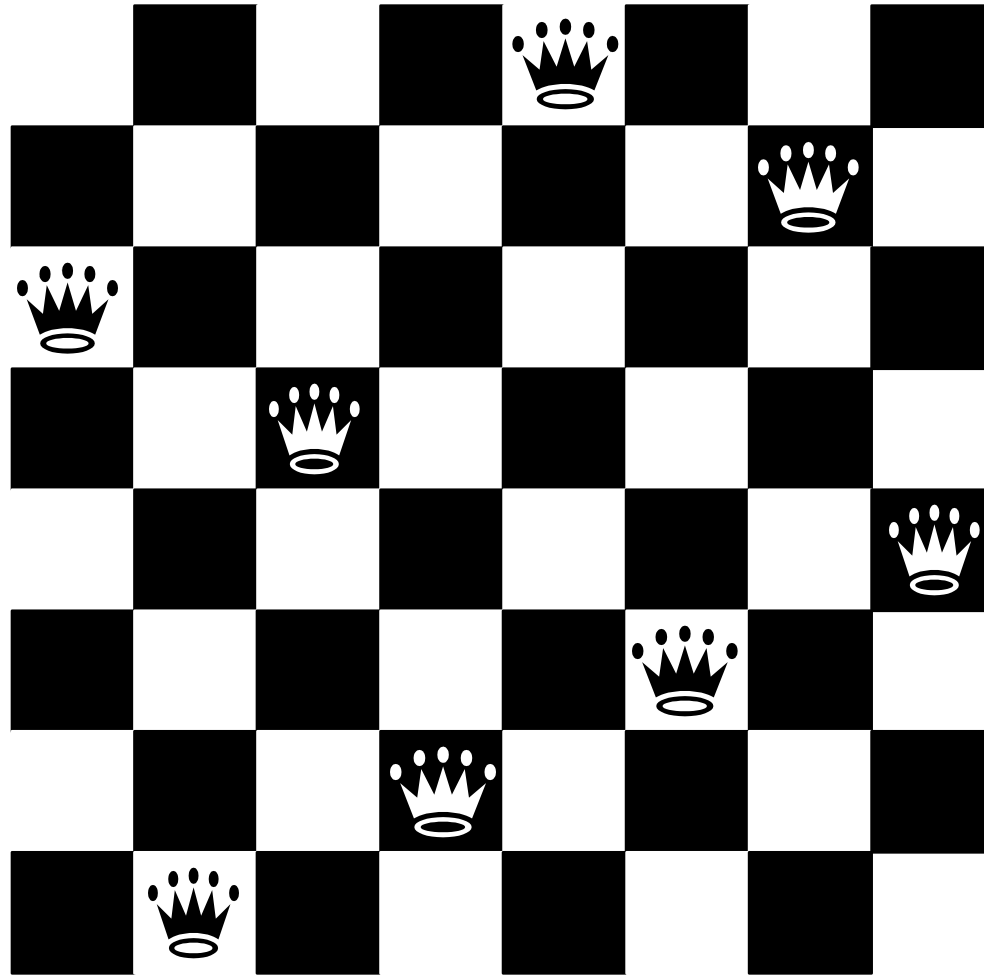
# The Eight Queens Problem



# The Eight Queens Problem



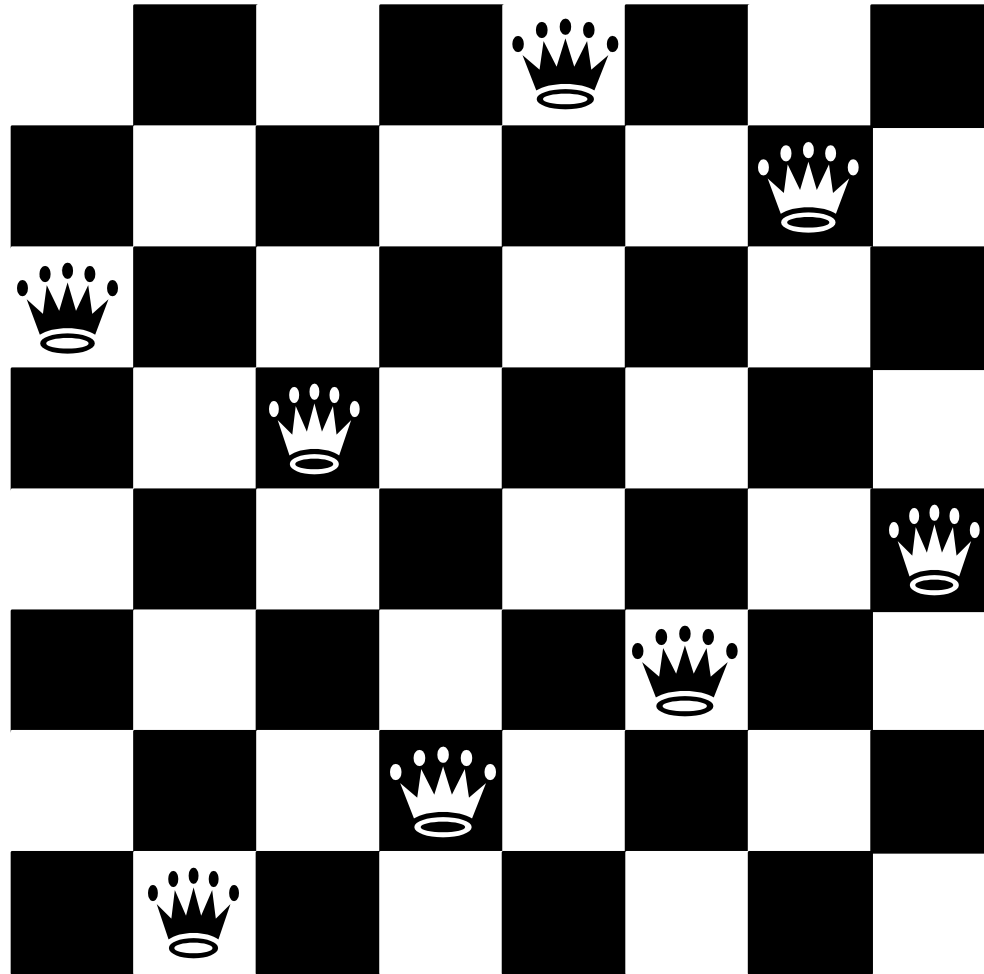
# The Eight Queens Problem



**Perfect !**



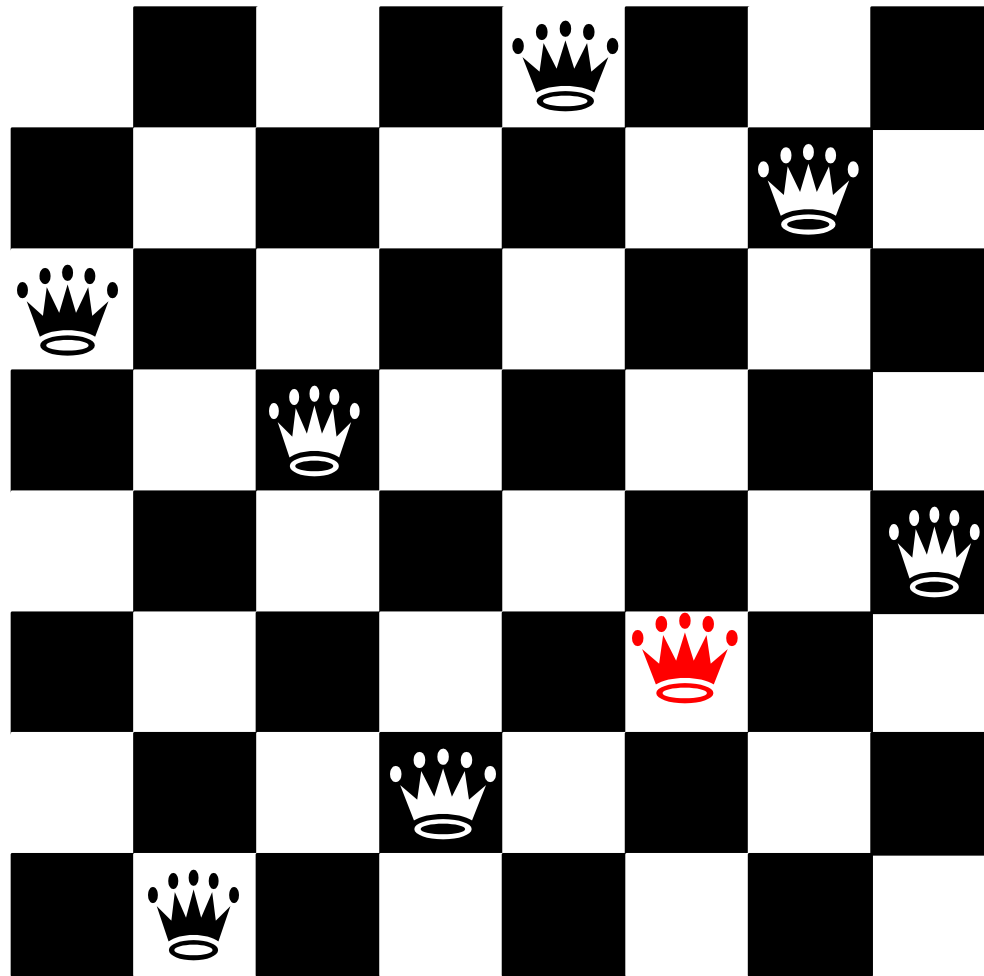
# The Eight Queens Problem



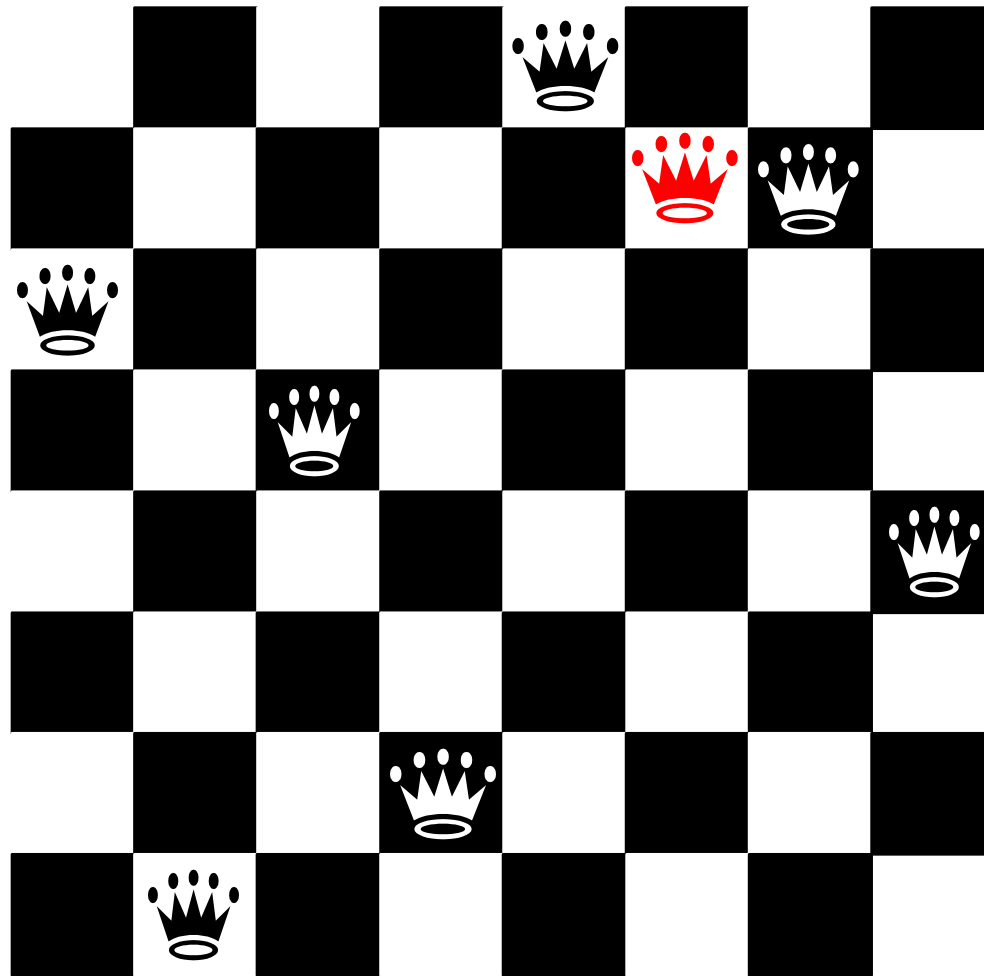
**Perfect !**

**Score 0**

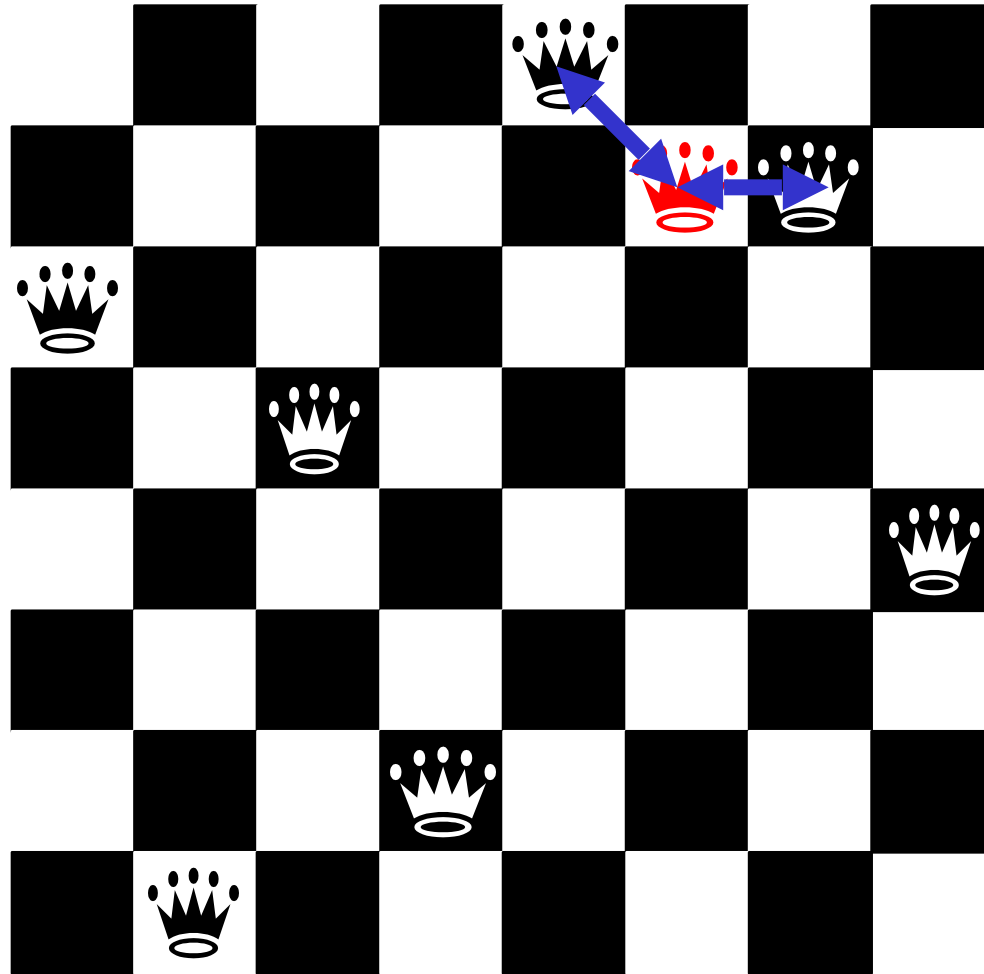
# The Eight Queens Problem



# The Eight Queens Problem



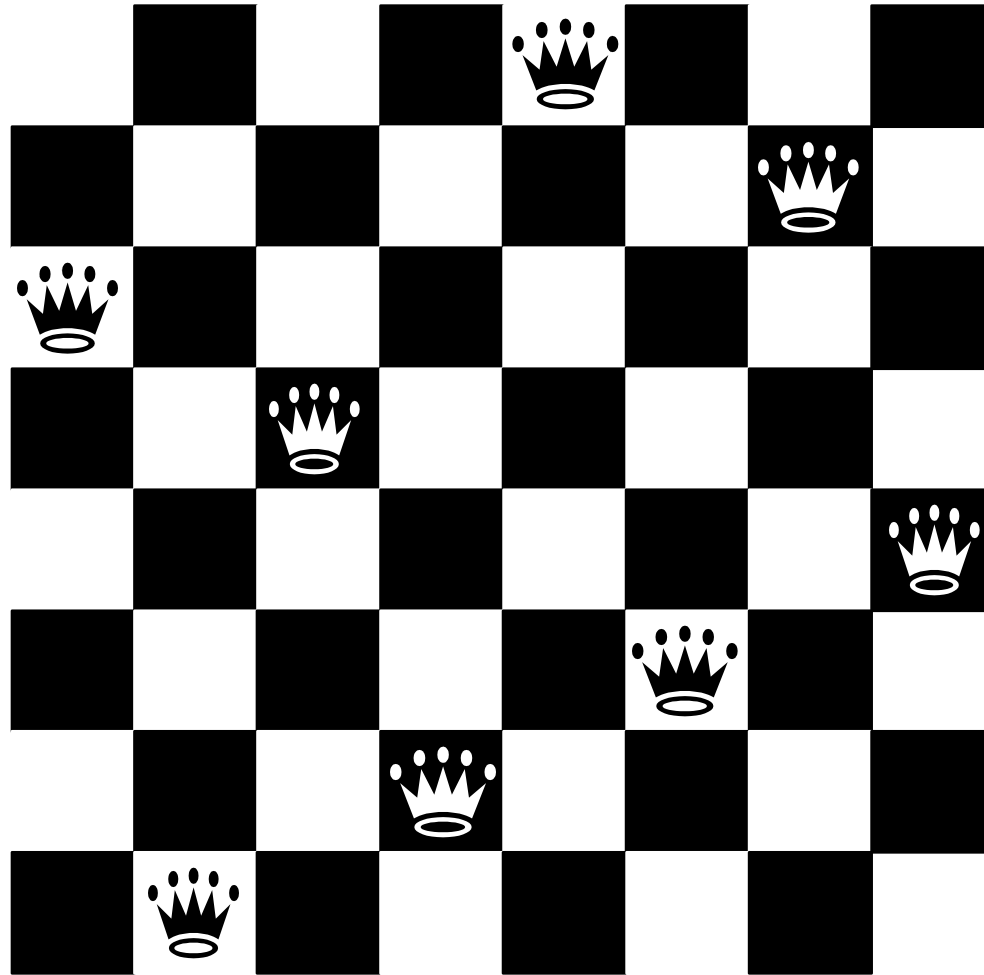
# The Eight Queens Problem



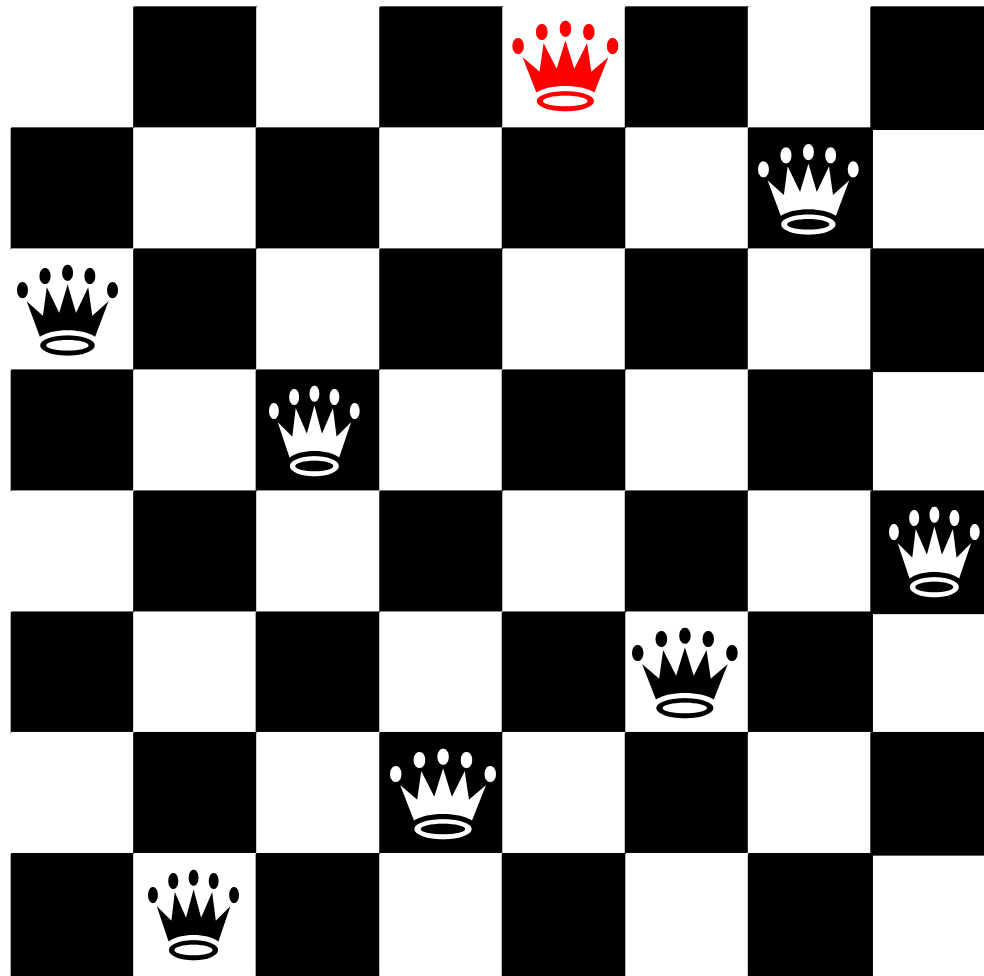
**Two  
Attacks**

**Score -2**

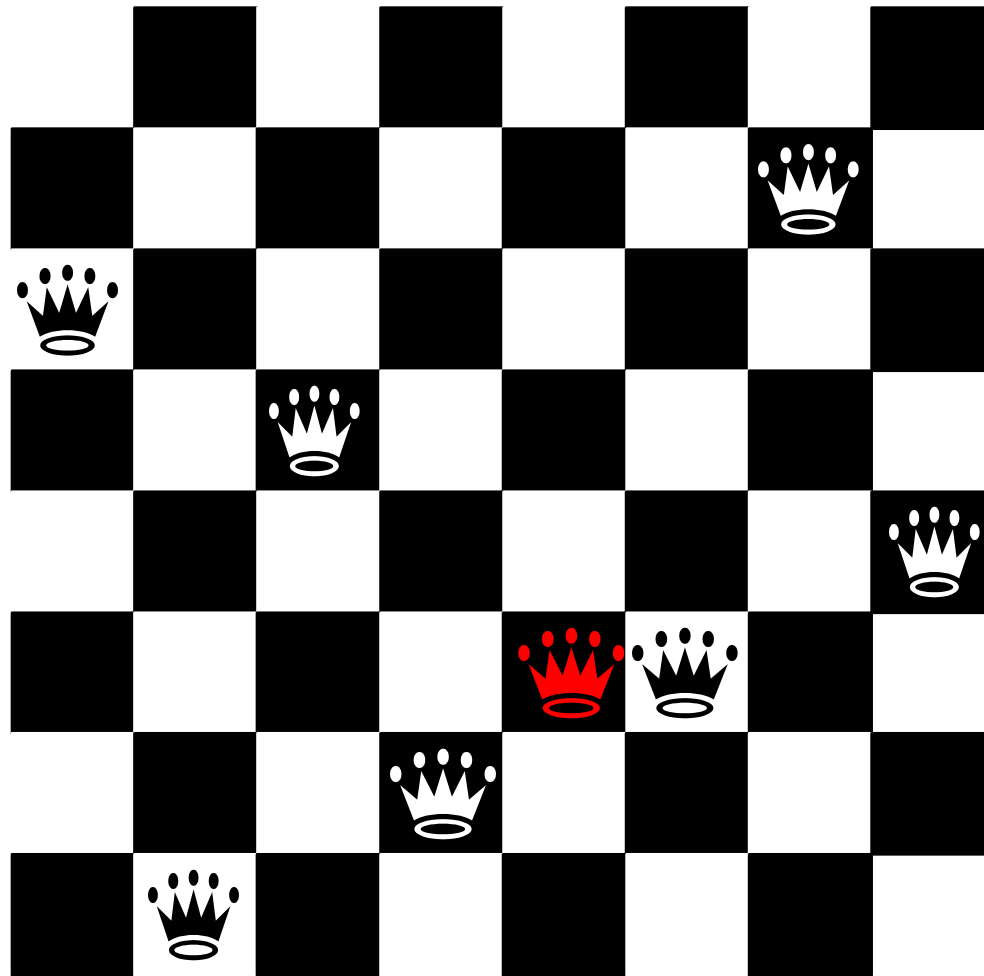
# The Eight Queens Problem



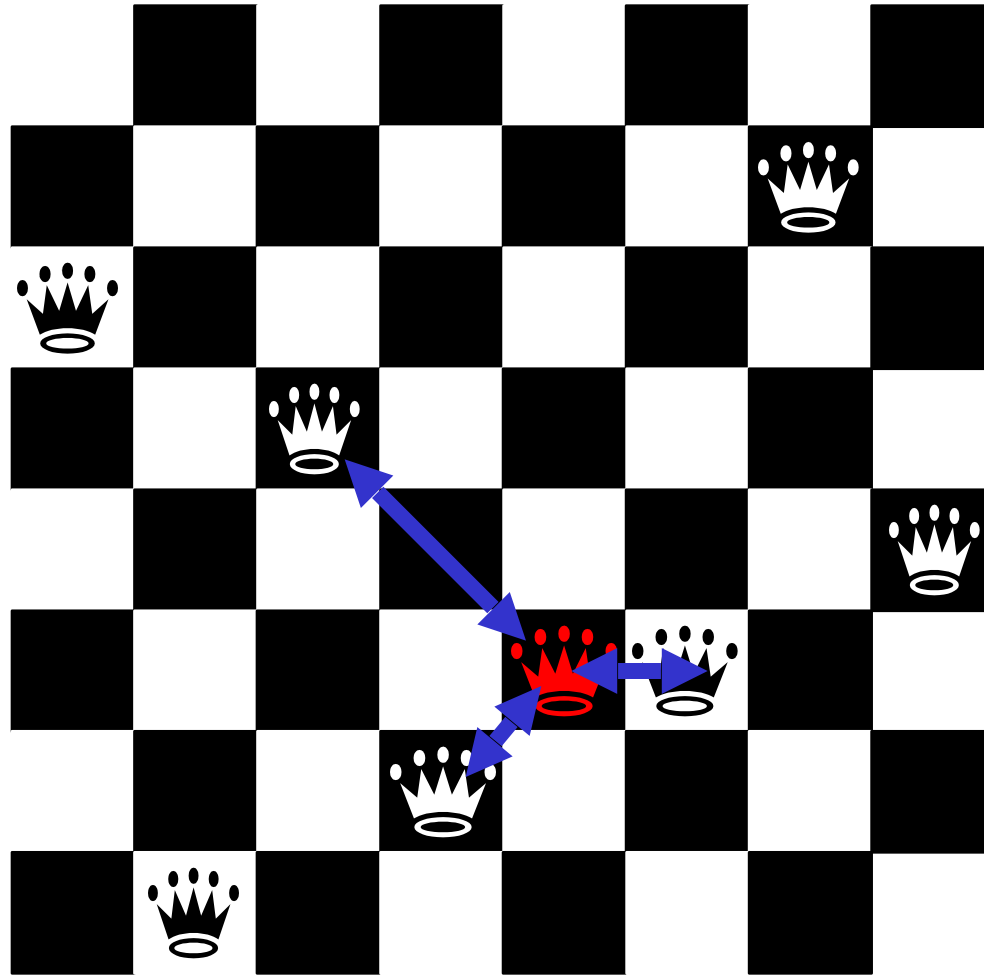
# The Eight Queens Problem



# The Eight Queens Problem



# The Eight Queens Problem

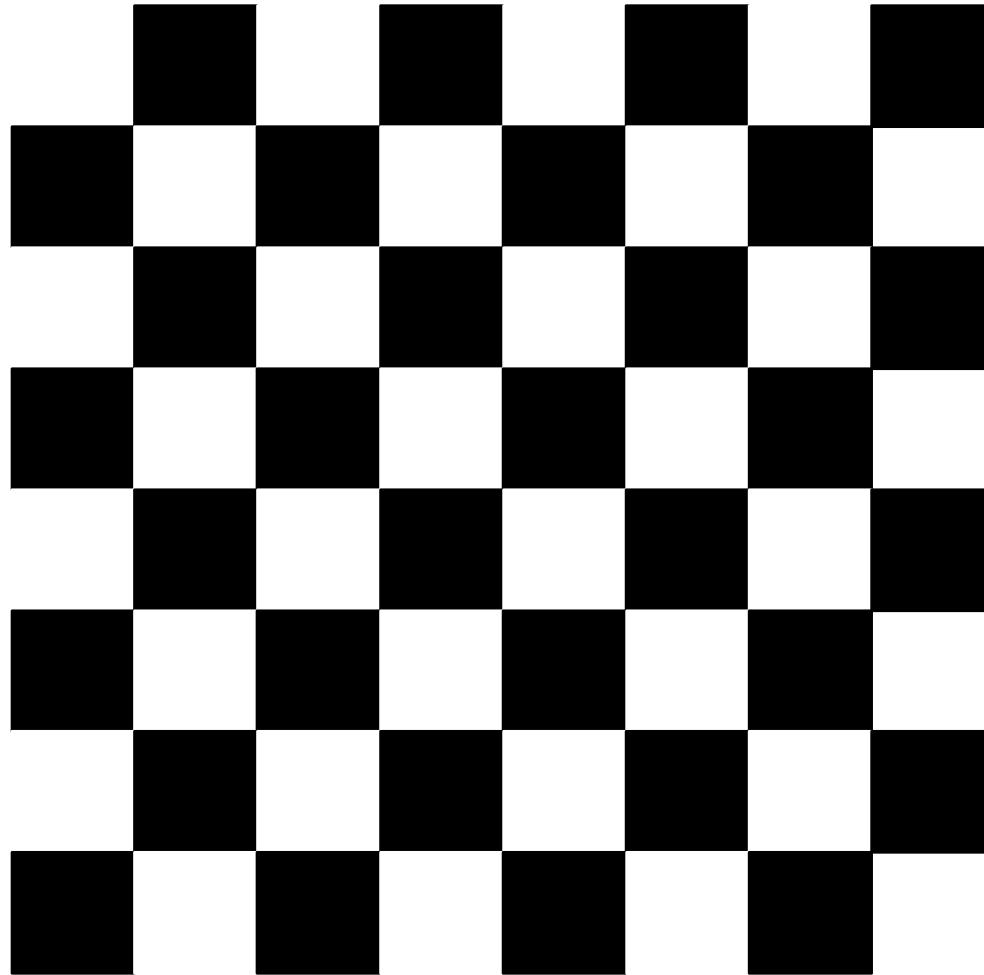


**Three  
Attacks**

**Score -3**



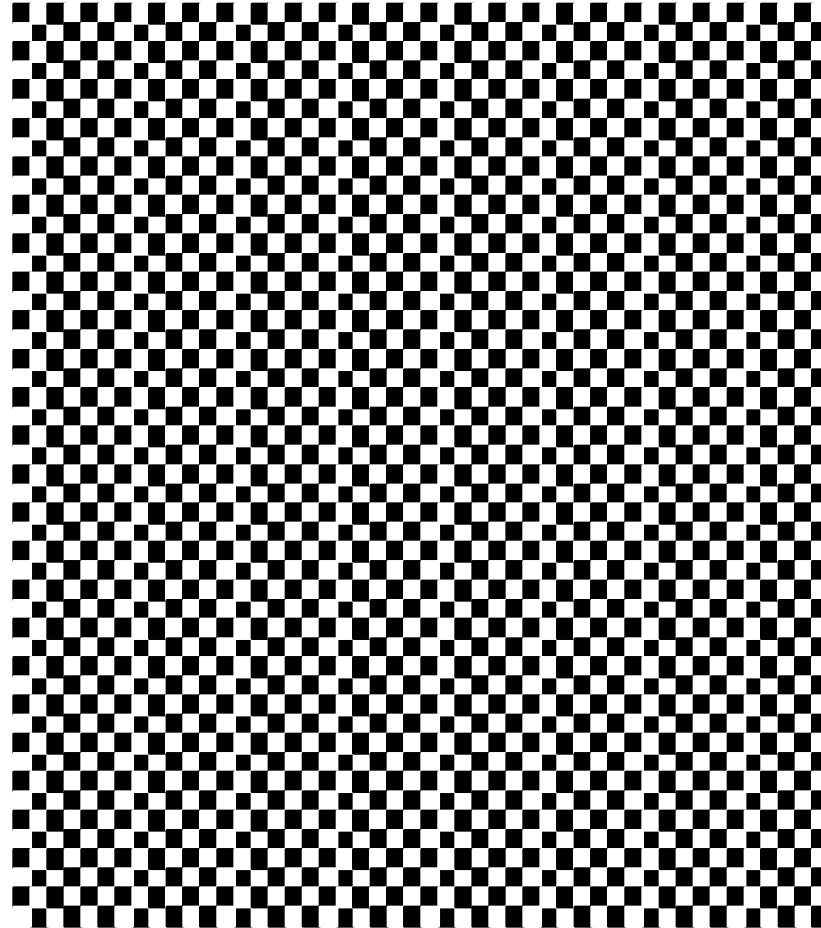
# Generate a solution



Place  
8 queens  
on the  
Board ...

... so that  
there are  
no  
attacks

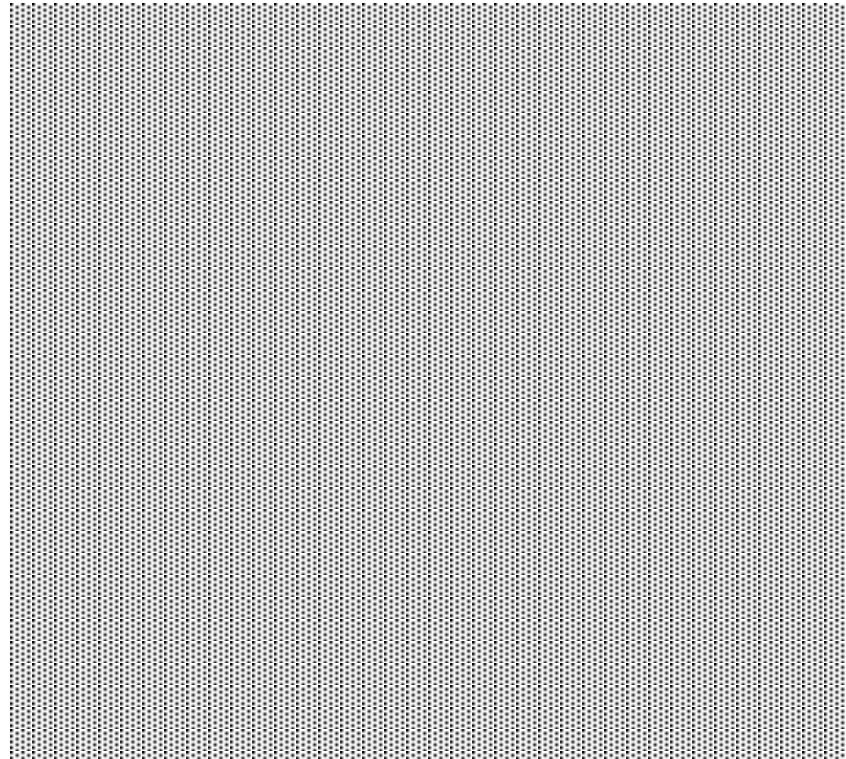
# Scale up: Generate a solution



Place  
44 queens  
on the  
Board ...

... so that  
there are  
no  
attacks

# Scale up: Generate a solution

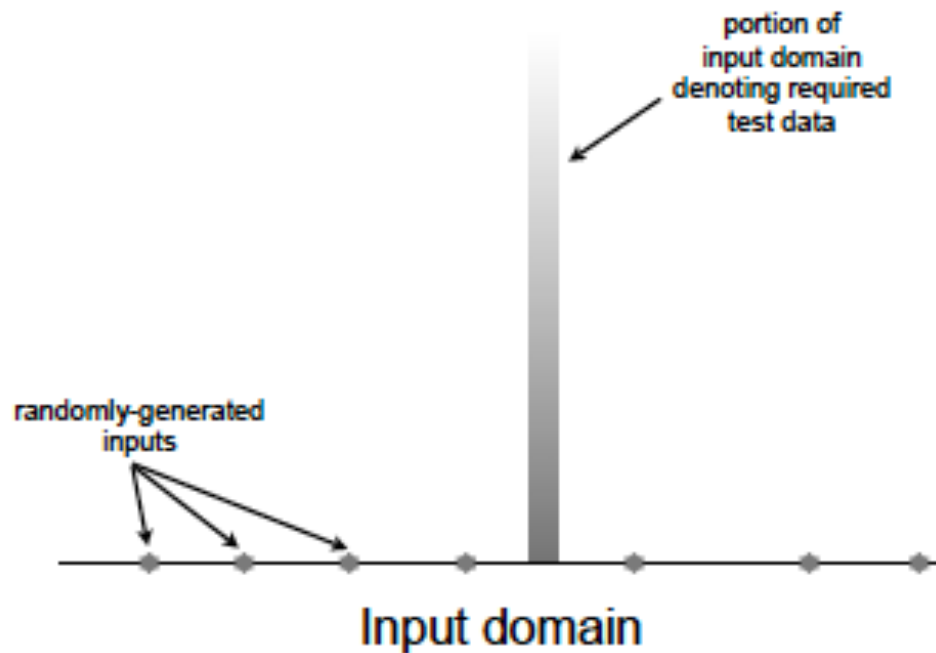


Place  
400 queens  
on the  
Board ...

... so that  
there are  
no  
attacks

# Random search

- Baseline for any search activity
- Inputs are generated at random until the goal of the test is fulfilled
- Random search is very poor at finding solutions when those solutions occupy a very small part of the overall search space



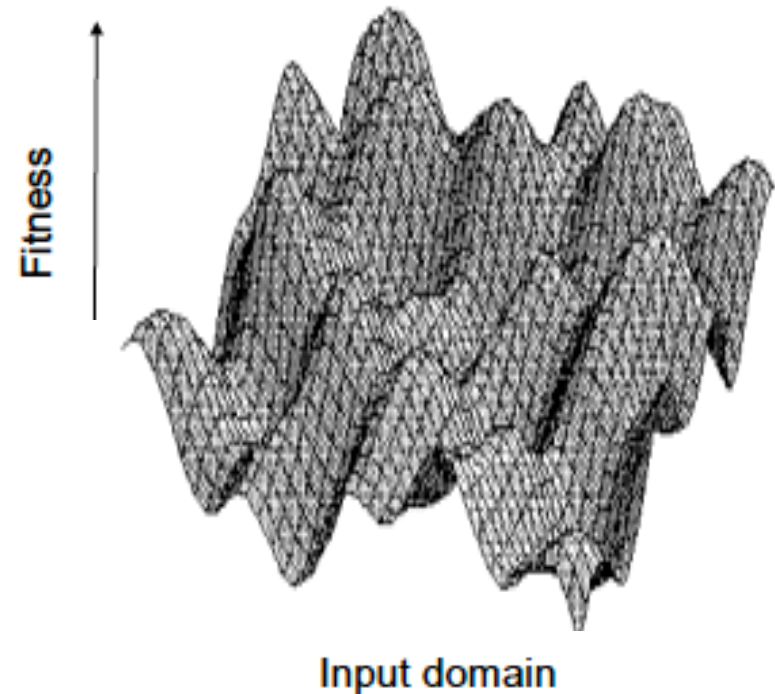
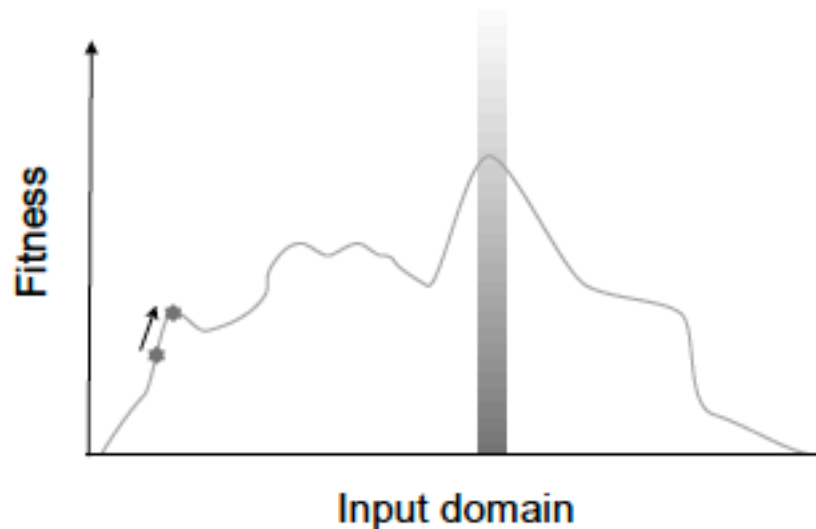
- Random search may fail to fulfil low-probability test goals

# Random search vs guided search

- Random search is not effective in finding test input when they are in small parts of the input space
- Test data may be found faster and more reliably if the search is given some guidance
- This guidance can be provided by a **fitness function**
  - *It scores different points in the search space with respect to their 'goodness' or their suitability for solving the problem*

# Fitness landscape

- A plot of a fitness function is referred to as the fitness landscape



# Checking vs Generating

## Task One:

- Write a method **to determine which is the better** of two placements of  $N$  queens

## Task Two:

- Write a method **to construct a board placement** with  $N$  non attacking queens



# Checking vs Generating

Task One:

- Write a method **to determine which is the better** of two placements of  $N$  queens

Which seems easier to you?

Task Two:

- Write a method **to construct a board placement** with  $N$  non attacking queens

# Checking vs Generating

## Search Based Software Engineering

- Write a method to determine which is the better of two solutions

## Conventional Software Engineering

- Write a method to construct a perfect solution

# Checking vs Generating

## Search Based Software Engineering

- Write a **method** to determine which is the better of two solutions

## Conventional Software Engineering

- Write a **method** to construct a perfect solution

# Checking vs Generating

## Search Based Software Engineering

- Write a **fitness function (also said cost function)** to determine which is the better of two solutions

## Conventional Software Engineering

- Write a method to construct a perfect solution

# Checking vs Generating

## Search Based Software Engineering

- Write a **fitness function** to guide a search of **a solution**

## Conventional Software Engineering

- Write a method to construct a perfect solution

# Checking vs Generating

## Search Based Software Engineering

- Write a **fitness function** to guide **automated search**

## Conventional Software Engineering

- Write a method to construct a perfect solution

# For the eight queens problem

## Search Based Software Engineering

- Write a **fitness function** to guide **automated search of placements of N queens**

## Conventional Software Engineering

- Write a method to **construct a board placement** with N non attacking queens

# The two SBSE ingredients

- **Representation should be easy:**
  - We always represent Software Engineering problems with data structures
- **Fitness function is often easy:**
  - We often define metrics



# Major issue

Uncertainty: identify a suitable fitness function

# We have plenty of search algorithm

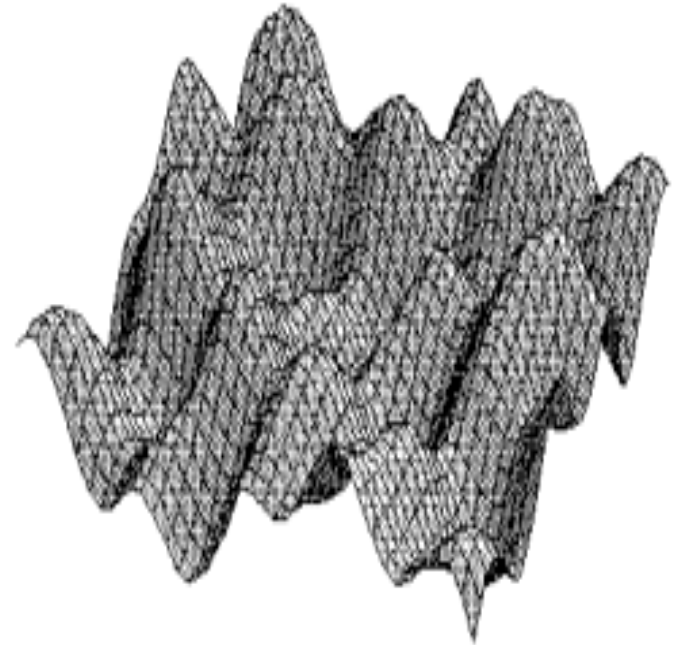
- Genetic Algorithms,
- Hill climbing,
- Simulated Annealing,
- Random,
- Tabu Search,
- Estimation of Distribution Algorithms,
- Particle Swarm Optimization,
- Ant Colonies,
- Greedy

# Hill Climbing - local search

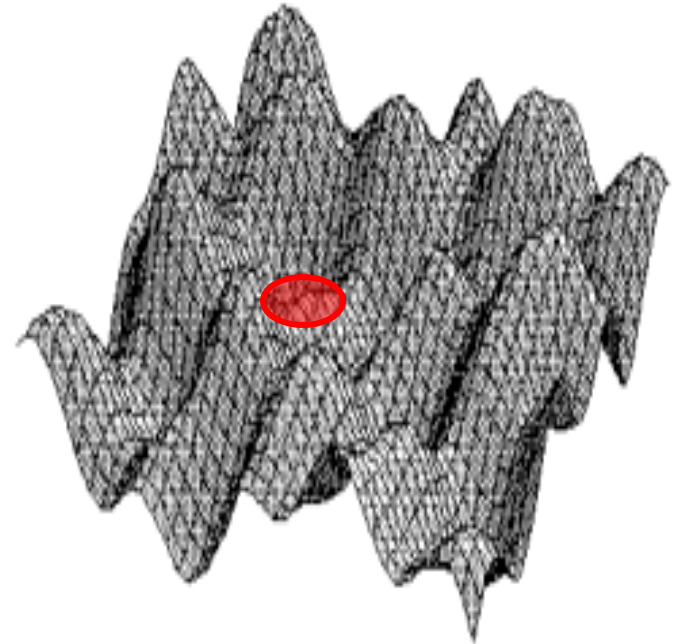


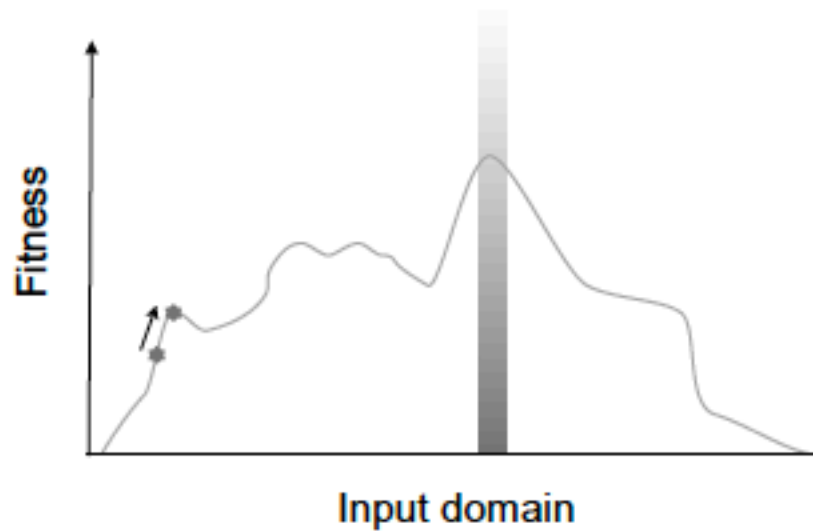
one solution at a time  
make moves only in the local  
neighborhood of those solutions

# Hill Climbing - local search

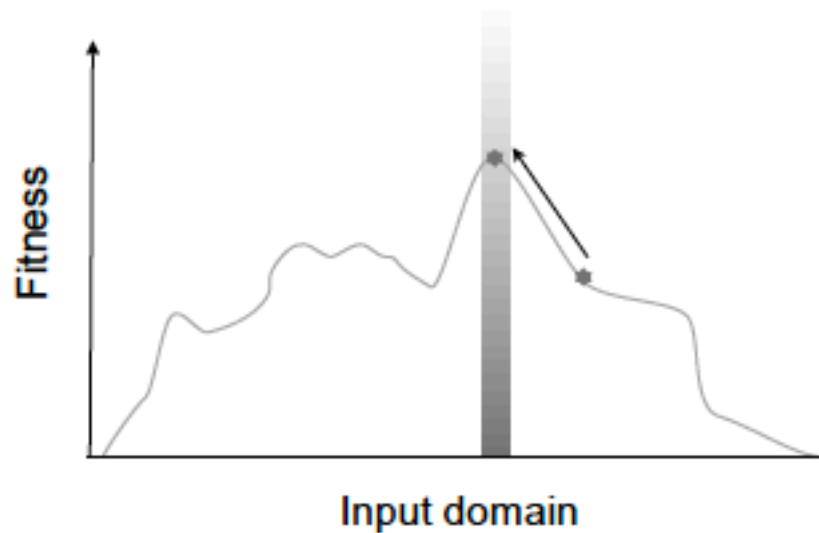


# Hill Climbing - local search





*(a) Climbing to a local optimum*



*(b) Restarting, on this occasion resulting in a climb to the global optimum*

# Bunch Hill Climbing Algorithm

```
bP = null;
```

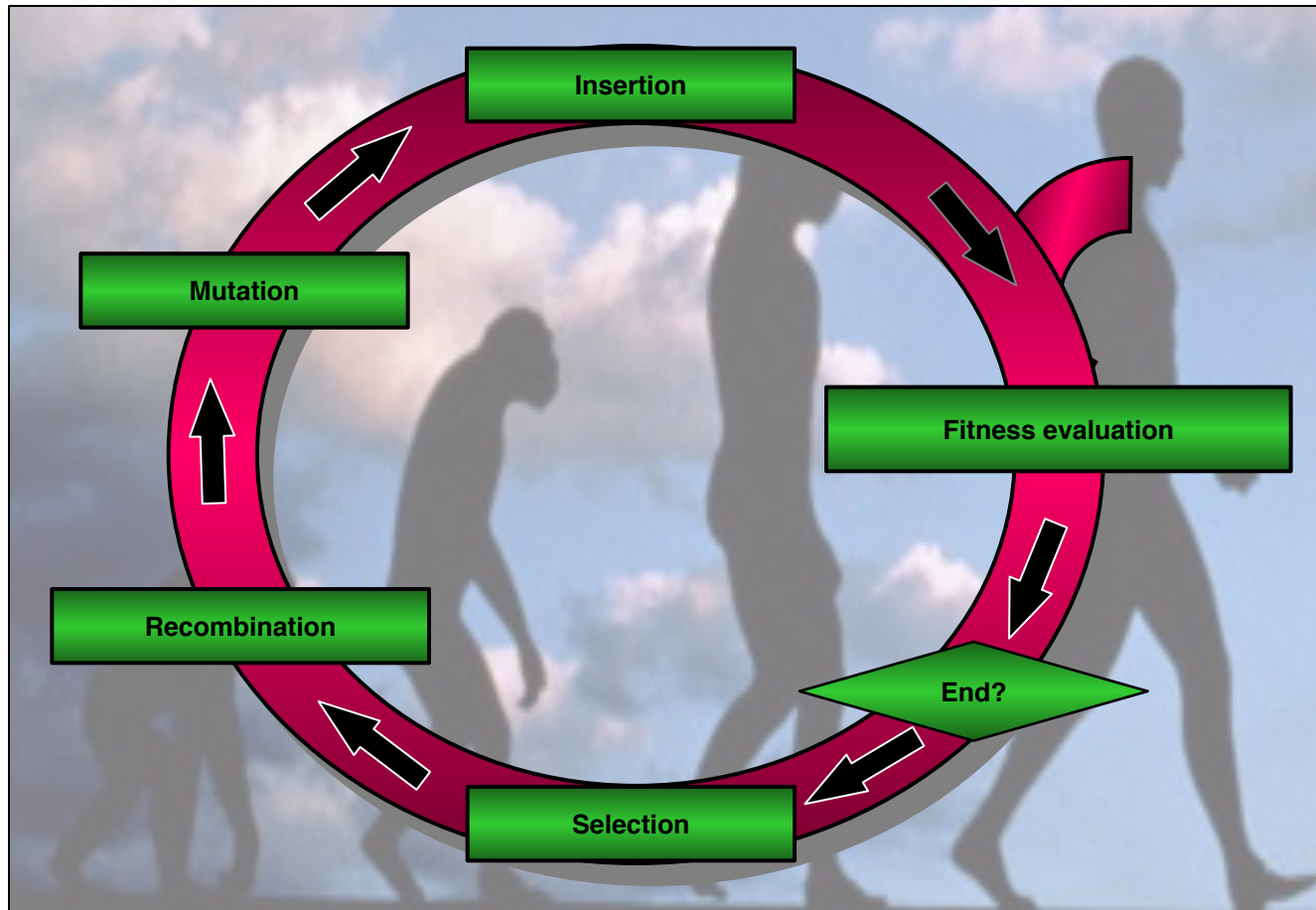
```
while(searching()) {  
    p = selectNext();  
    if(p.isBetter(bP))  
        bP = p;  
}
```

# Local vs global search

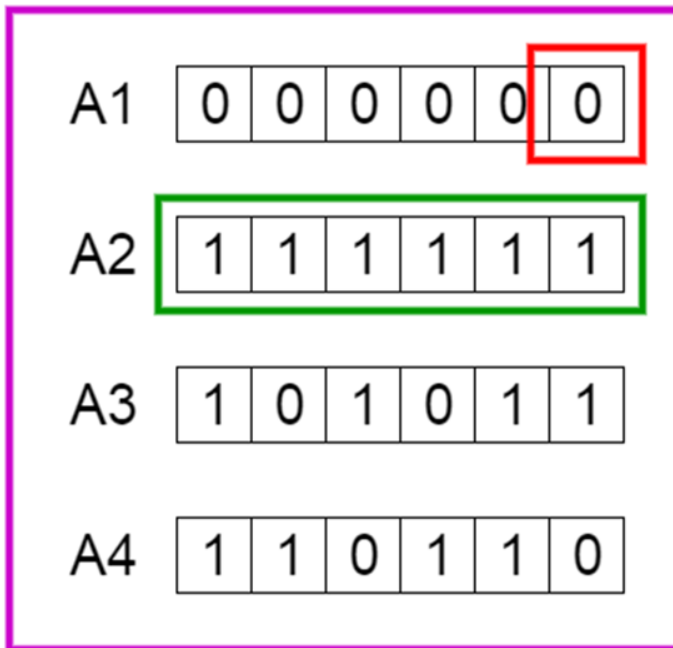
- Hill climbing performs **local** search by finding one solution at a time and moving only in the local neighborhood of the solution
- Genetic Algorithms perform **global** search, sampling many points in the search space at once



# Evolutionary Algorithms



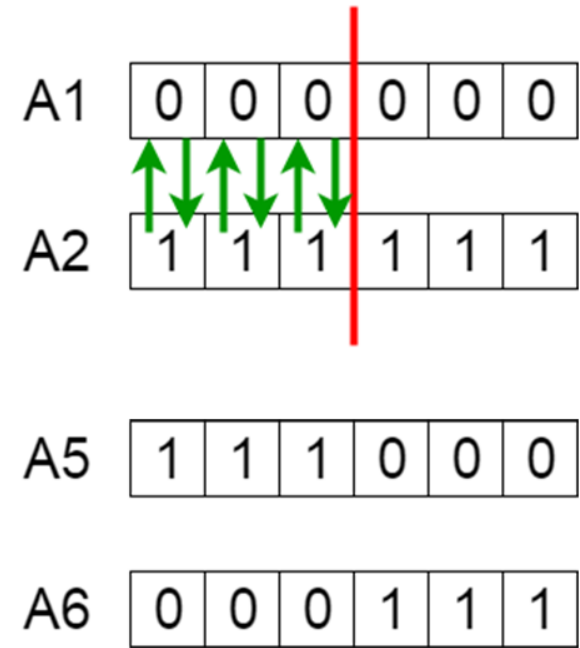
# Genetic Algorithms



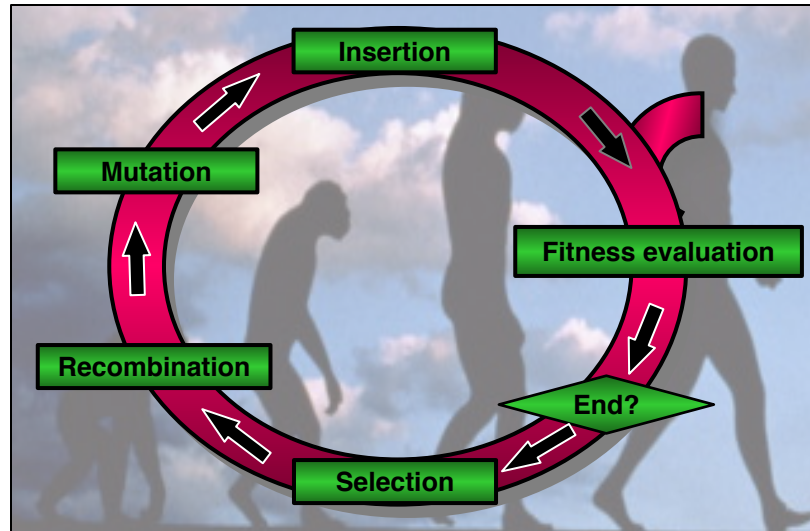
Gene

Chromosome

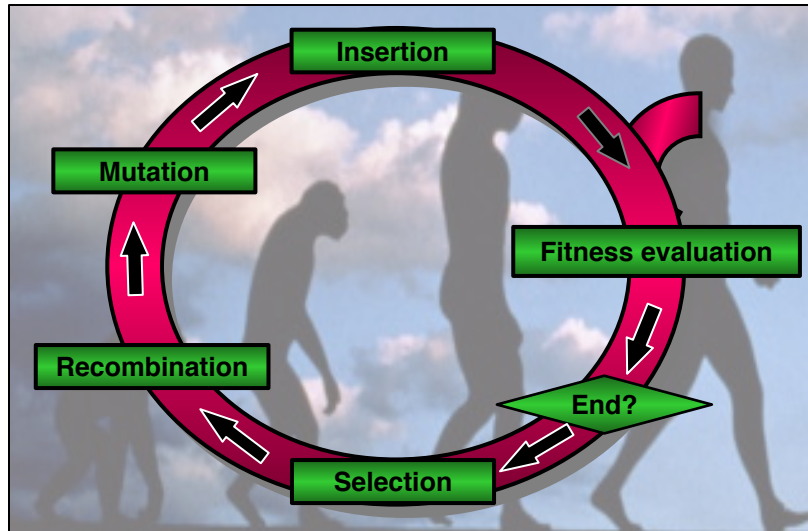
Population



# How does a GA work?

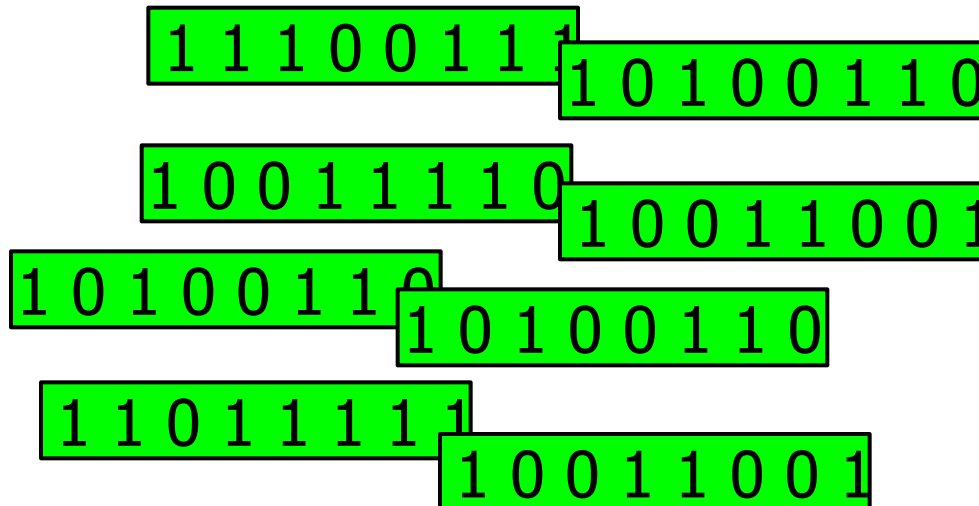


# How does a GA work?

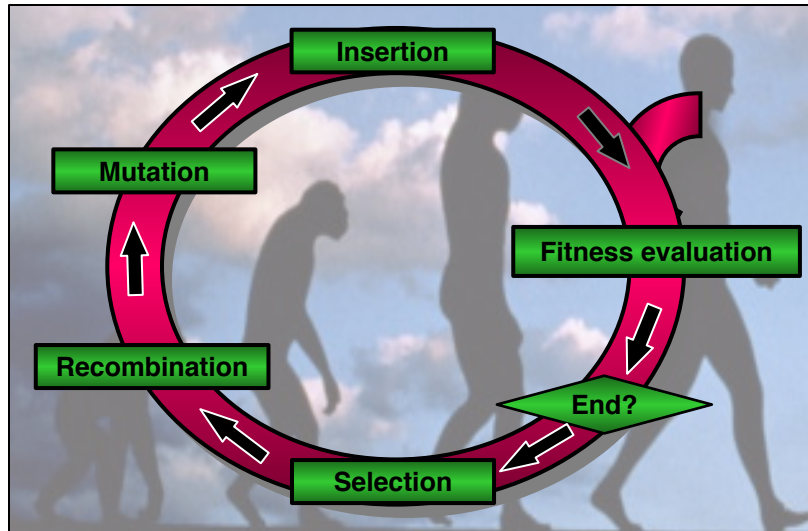


**Population**

A finite set of strings,  
arrays, ...: **the genome**



# How does a GA work?



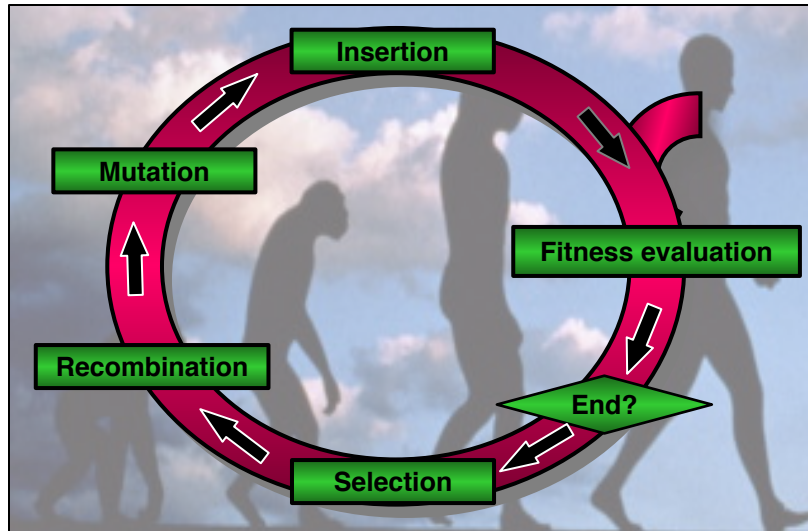
**Selection operator:**  
selects individuals for  
the reproduction

1 0 0 1 1 0 0 1

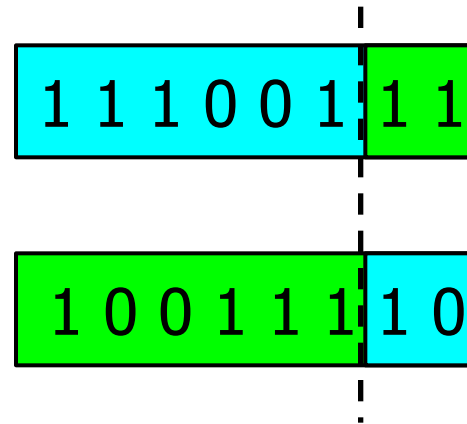
1 0 1 0 0 1 1 0

1 0 0 1 1 0 0 1

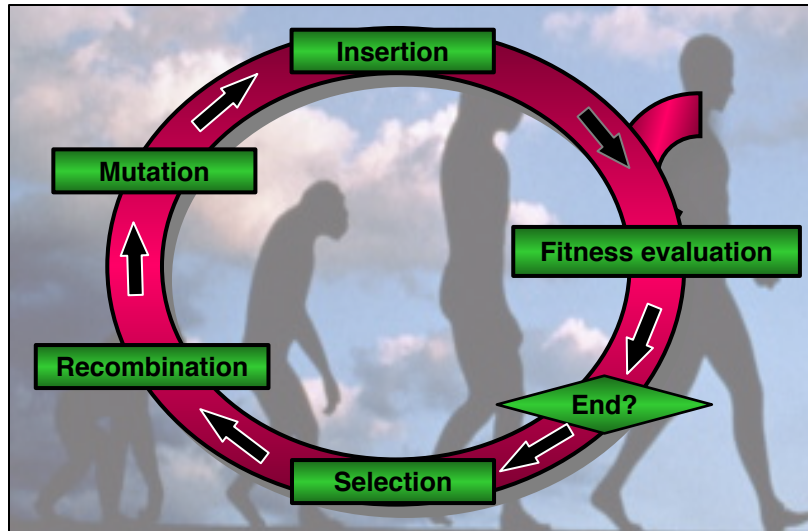
# How does a GA work?



**Crossover operator:**  
produces new individuals  
from two *parents*,  
exchanging parts of  
their chromosomes

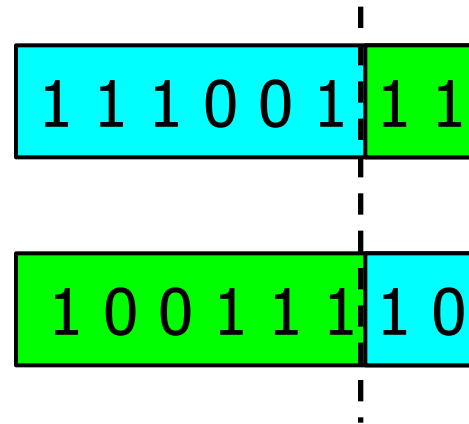


# How does a GA work?



**Mutation operator:**  
randomly modifies an individual's genome

1 1 1 | 1 0 1



# Ingredients and actions

- Chromosome (individual)
- Population
- Fitness function
- Selection
- Crossover
- Mutation
- Crossover



# Encoding a chromosome

- A chromosome contains information about a solution that represents
- The most used way of encoding is a binary string

Chromosome	1101100100110110
------------	------------------

# Encoding

- **Binary encoding**
  - Arrays of Bits
- **Permutation encoding**
  - Permutations of arrays of natural numbers
- **Value Encoding**
  - Arrays of values
- **Tree encoding**
  - Trees (e.g., control flow model)

<https://www.obitko.com/tutorials/genetic-algorithms/crossover-mutation.php>

# Crossover

- Generating offsprings from existing genomes

# Crossover on Bits

**Single point crossover** - one crossover point is selected, binary string from beginning of chromosome to the crossover point is copied from one parent, the rest is copied from the second parent

**Two point crossover** - two crossover point are selected, binary string from beginning of chromosome to the first crossover point is copied from one parent, the part from the first to the second crossover point is copied from the second parent and the rest is copied from the first parent

**Uniform crossover** - bits are randomly copied from the first or from the second parent

**Arithmetic crossover** - some arithmetic operation is performed to make a new offspring

<https://www.obitko.com/tutorials/genetic-algorithms/crossover-mutation.php>

# Crossover

arithmetic  
crossover

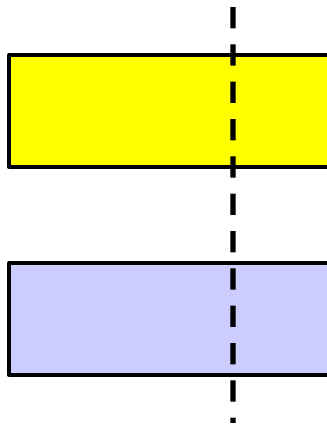
one-point  
crossover



# Crossover

arithmetic  
crossover

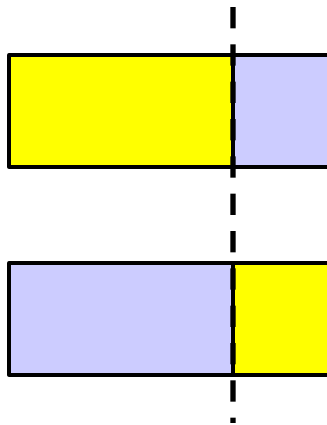
one-point  
crossover



# Crossover

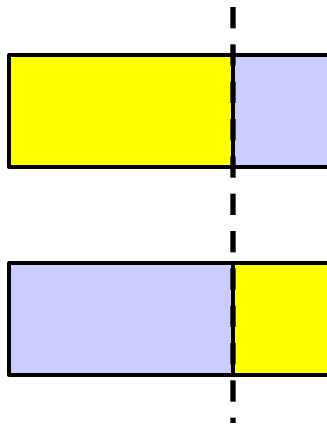
arithmetic  
crossover

one-point  
crossover



# Crossover

one-point  
crossover



arithmetic  
crossover

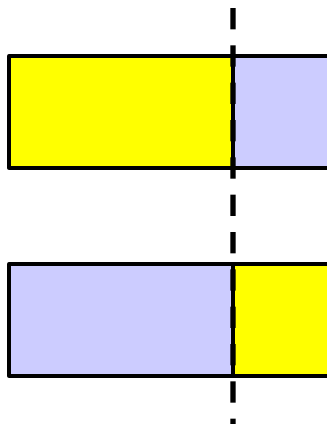
0.1	0.2	0.3	0.4	0.5
-----	-----	-----	-----	-----

0.6	0.7	0.8	0.9	1.0
-----	-----	-----	-----	-----



# Crossover

one-point  
crossover



arithmetic  
crossover

0.1	0.2	0.3	0.4	0.5
-----	-----	-----	-----	-----

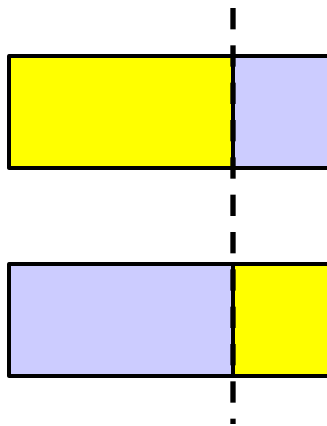
0.6	0.7	0.8	0.9	1.0
-----	-----	-----	-----	-----

$$\text{Child 1} = a \cdot x + (1-a) \cdot y$$

$$\text{Child 2} = a \cdot y + (1-a) \cdot x$$

# Crossover

one-point  
crossover

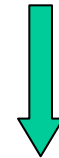


arithmetic  
crossover

0.1	0.2	0.3	0.4	0.5
-----	-----	-----	-----	-----

0.6	0.7	0.8	0.9	1.0
-----	-----	-----	-----	-----

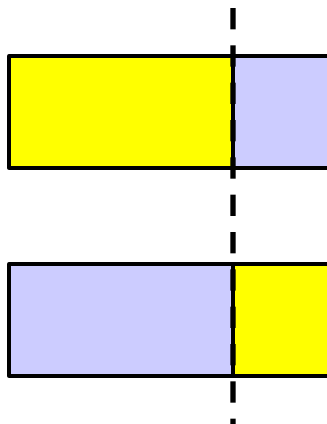
$$\text{Child 1} = a \cdot x + (1-a) \cdot y$$



$$\text{Child 2} = a \cdot y + (1-a) \cdot x$$

# Crossover

one-point  
crossover

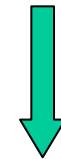


arithmetic  
crossover

0.1	0.2	0.3	0.4	0.5
-----	-----	-----	-----	-----

0.6	0.7	0.8	0.9	1.0
-----	-----	-----	-----	-----

$$\text{Child 1} = a \cdot x + (1-a) \cdot y$$



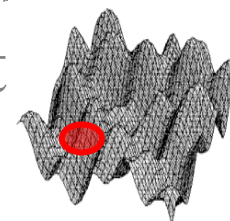
$$\text{Child 2} = a \cdot y + (1-a) \cdot x$$

0.43	0.53	0.56	0.73	0.83
------	------	------	------	------

0.27	0.37	0.47	0.57	0.67
------	------	------	------	------

# Mutation

- Mutate existing genomes
- Goal:
  - Try to **avoid local minima/maxima** by *preventing the population of chromosomes from becoming too similar to each other*, thus slowing or even stopping convergence to global optimum
  - **Introduce diversity** into the sampled population



# Mutation on Bits

- *Mutation according to a given probability*
- This probability should be set low:
  - If it is set too high, the search will turn into a *random search*



# Bit string mutation

- Bit flips at **random positions**
- Example:

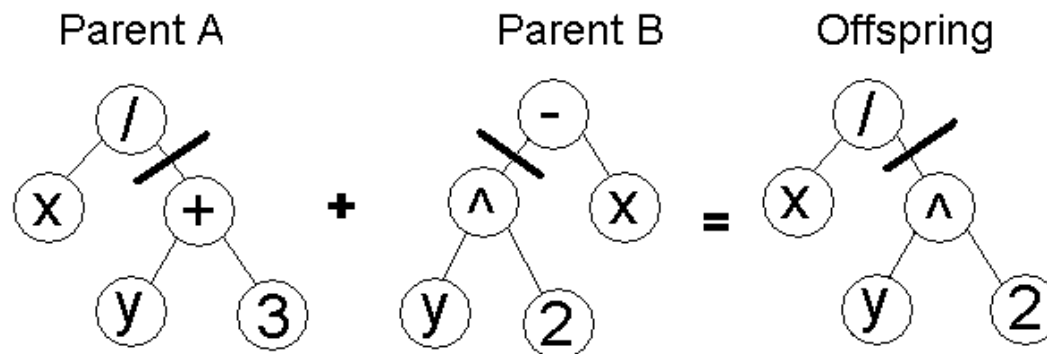
1 1 1 0 0 1

1 1 1 1 0 1

- The probability of a mutation of a bit is  $1/L$ , where  $L$  is the length of the binary vector

# Other cases

- Mutation on real numbers: adding/subtracting a small number to selected entries
- Cross-over on trees: combine two parts of the parents tree at cross-over point





# Effects of Genetic Operators

- Using *selection alone* will tend to fill the population with copies of the best individual from the population
- Using *selection and crossover* operators will tend to cause the algorithms to converge on a good but sub-optimal solution (e.g., no diversity)

# Effects of Genetic Operators

- Using *mutation alone* induces a random walk through the search space
- Using *selection and mutation* creates a parallel, noise-tolerant, hill climbing algorithm (e.g., no inheritance)

# Genetic Algorithms: pseudocode

```
Initialize population P[0];
generation=0;
while (generation <
    max_number_of_generations)
    Evaluate P[generation];
    generation=generation+1;
    Select P[generation] from
    P[generation-1];
    Crossover P[generation];
    Mutate P[generation];
end while
```

# The algorithm

- Randomly initialize population( $t$ )
- Determine fitness of population( $t$ )
- Repeat
  - Select parents from population( $t$ )
  - Perform crossover on parents creating population( $t+1$ )
  - Perform mutation of population( $t+1$ )
  - Determine fitness of population( $t+1$ )
- until best individual is good enough

# Evolutionary Testing

- Evolutionary testing aims at improving the effectiveness and efficiency of the testing process by

transforming **testing objectives into search problems** and applying evolutionary computation in order to solve them

# Evolutionary Testing: HowTo

- Search space: **input domain(s)** of the system under test (SUT)
- Test objective needs to be **defined numerically** and **transformed in a fitness function**
- Fitness is computed by **monitoring program execution results** (output, performance, etc.)
- Iterative procedure

# Testing

- Different test goals = different fitness functions

# Two assumptions

- Two assumptions in order to use search based algorithm in testing
- **Representation.** Candidate solutions must be capable of being encoded as sequences of elements
- **Fitness function.** The fitness function guides the search by evaluating candidate solutions. The fitness function is problem-specific



# Evolutionary Testing: HowTo

- Start with a set of randomly generated test input data
- Then execute on test data to gather information
- Monitored values are used to compute the fitness
- Evolution towards a testing objective, indicated in the fitness function

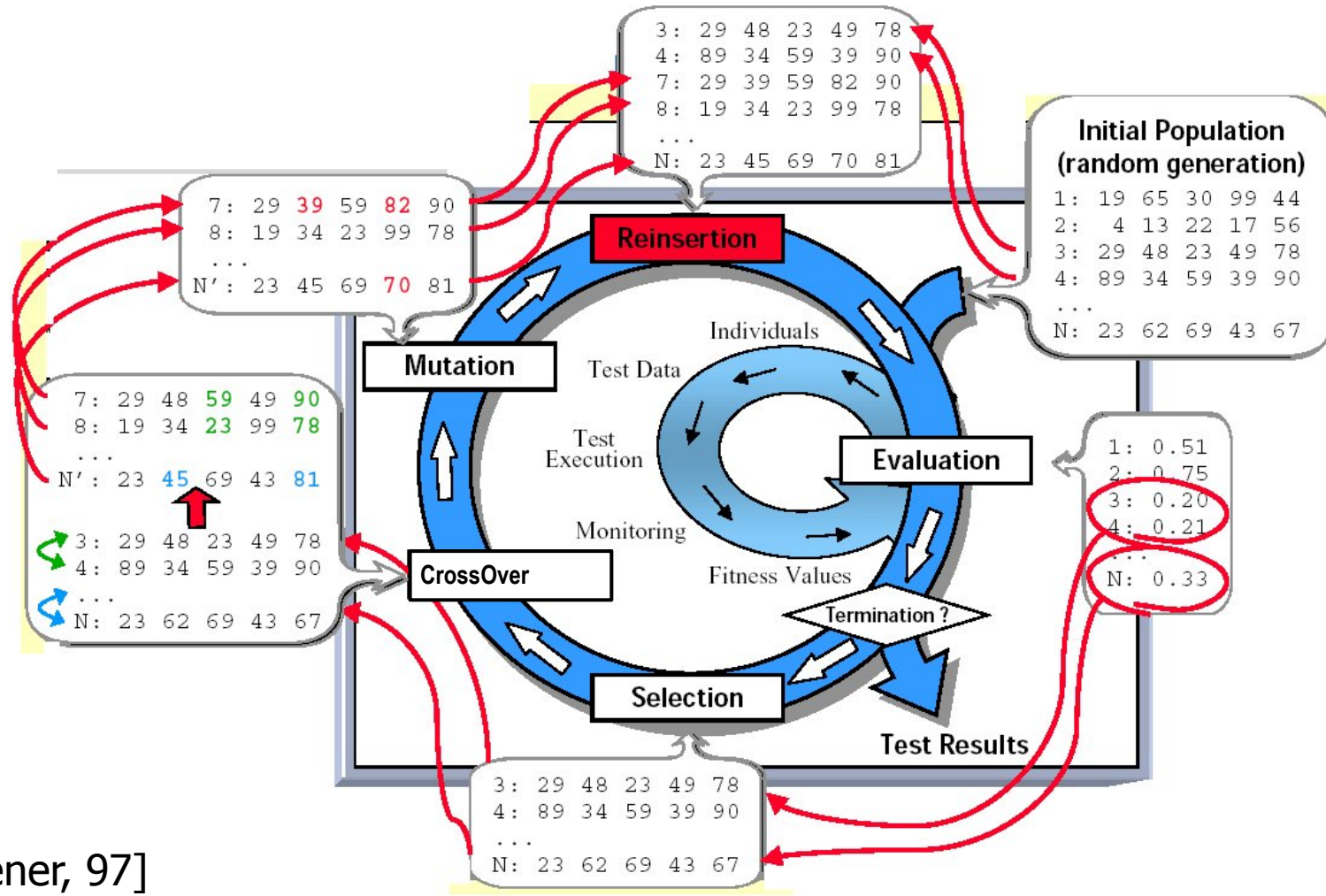
# Genome encoding

	$I_1$	$I_2$	$I_3$	...	...	$I_n$
$T_{x1}$	<24.5>	<11.3>	<abc>	...	...	<ghi>
...	...	...	...	...	...	...
$T_{x5}$	<7.6>	<4.7>	<def>	...	...	<xza>

## Typical Parameter Settings

- dim pop = 70
- n gen = 500
- P mutation = 0,01

# More Details



[Wegener, 97]

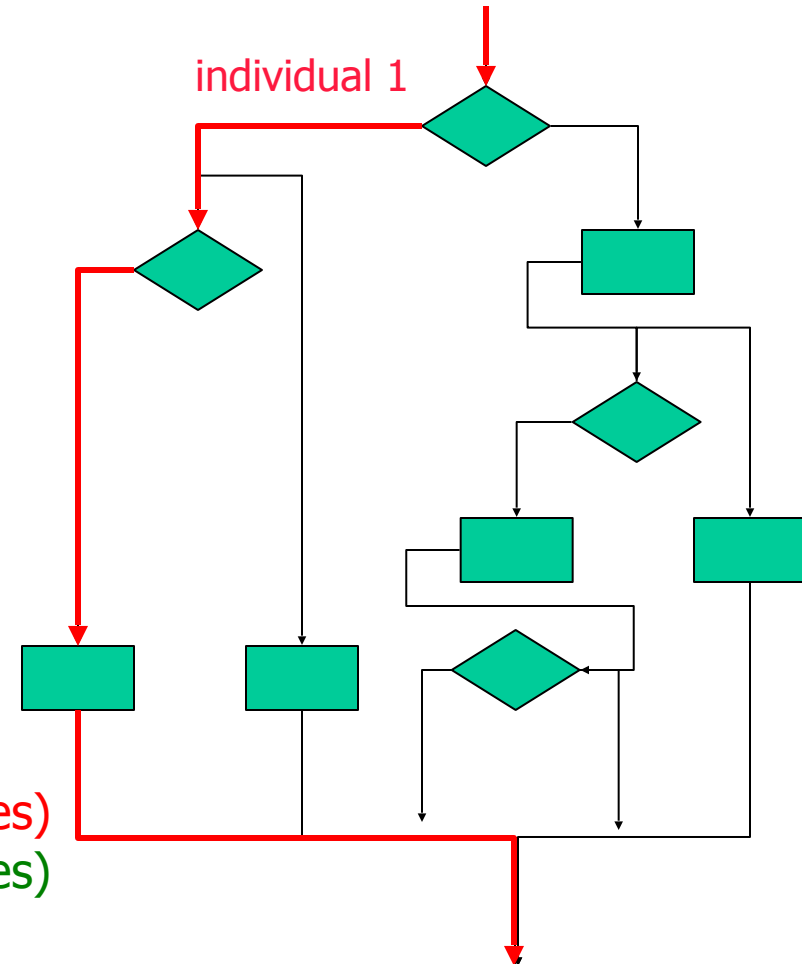
# Example: Structural Testing

- Aim
  - Generate a set of test data to **cover structural properties**
- Fitness function a normalized combination of
  - **Approach level:** fitness is number of control nodes in a path and dependent from a target one not covered by test execution with a given input
  - **Branch distance.** At the node at which the test execution diverges from the target branch at some approach level, the branch distance is computed.

# Example: Coverage-oriented approaches

Individual: path to same target

- Fitness of individual for different coverage criteria
  - % of covered statements
  - **% of covered branches**
  - Path coverage: % executed paths
- Good results, better than random testing



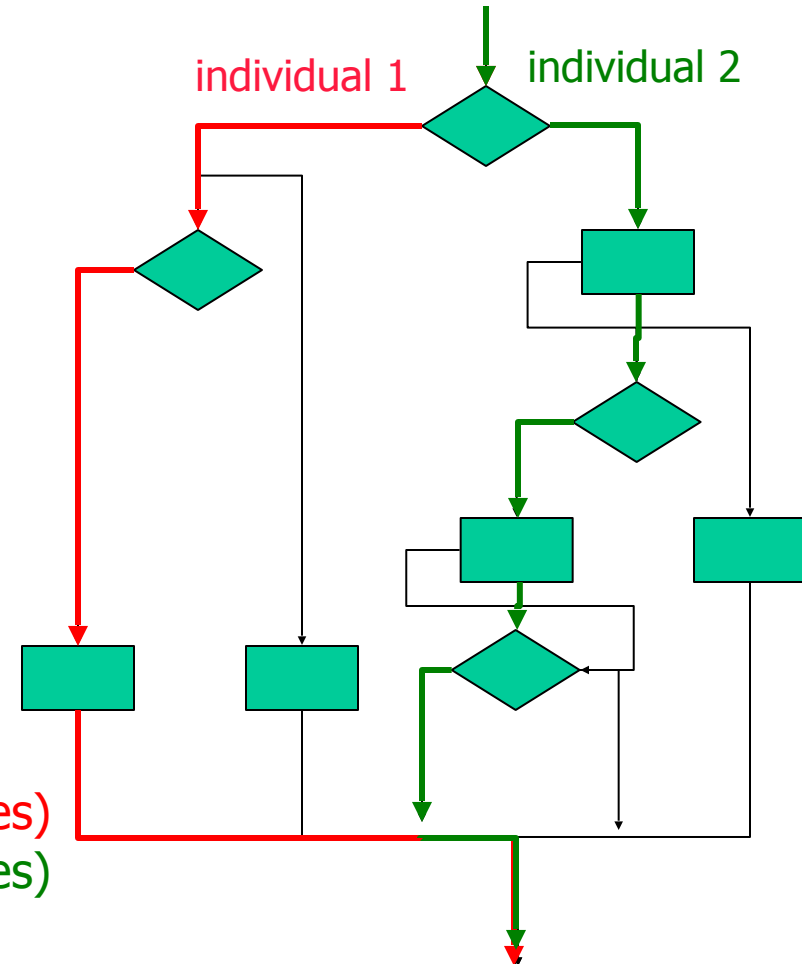
Individual 1: fitness=2 (2 branches)

Individual 2: fitness=3 (3 branches)

# Example: Coverage-oriented approaches

Individual: path to same target

- Fitness of individual for different coverage criteria
  - % of covered statements
  - **% of covered branches**
  - Path coverage: % executed paths
- Good results, better than random testing



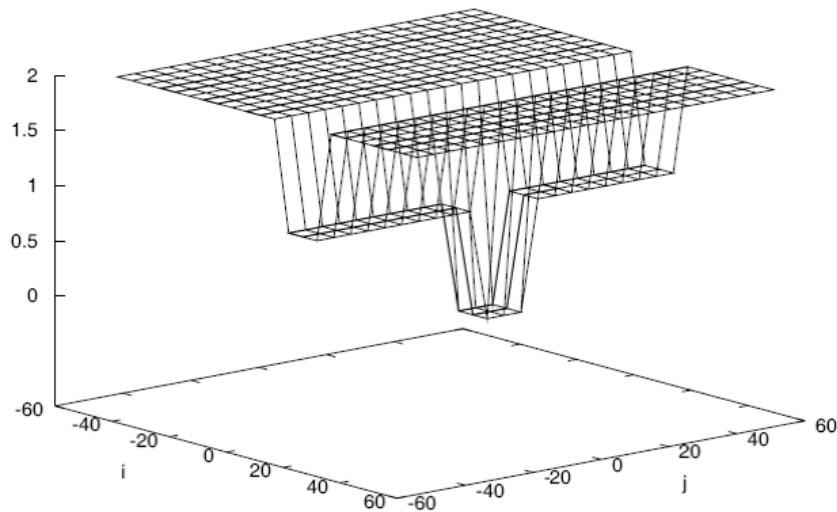
Individual 1: fitness=2 (2 branches)

Individual 2: fitness=3 (3 branches)

# Example: Control-Oriented

```
s void landscape_example(int i, int j)
  {
1   if (i >= 10 && i <= 20)
    {
2     if (j >= 0 && j <= 10)
      {
3       // target statement
        // ...
      }
    }
  }
```

Fitness function:  
True conditions  
not executed



Fitness landscape

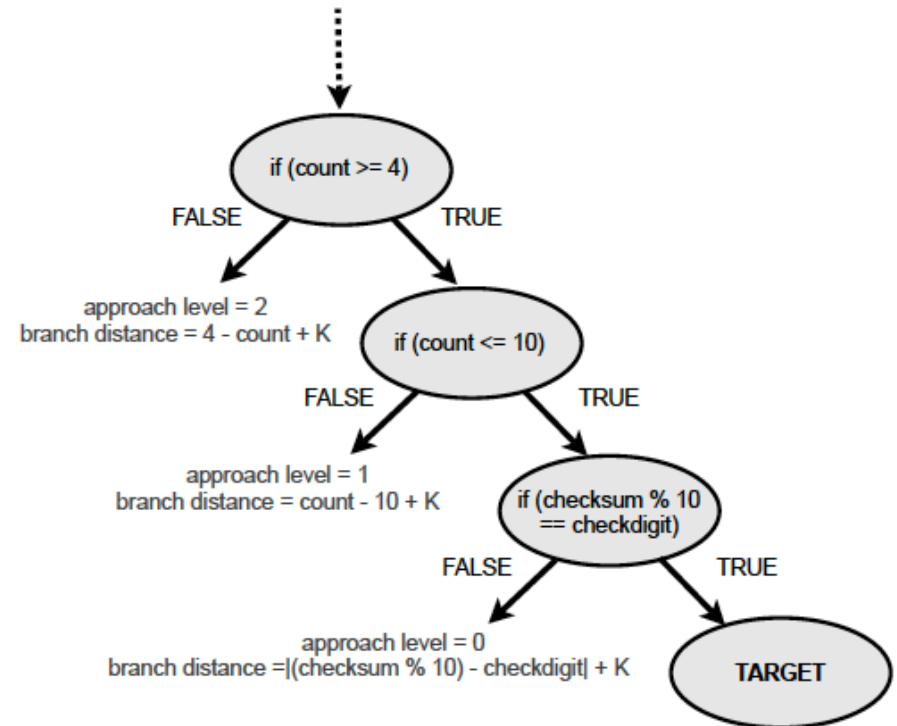
# Example

```
(1) int cas_check(char* cas) {  
(2)     int count = 0, checksum = 0, checkdigit = 0, pos;  
(3)  
(4)     for (pos=strlen(cas)-1; pos >= 0; pos--) {  
(5)         int digit = cas[pos] - '0';  
(6)  
(7)         if (digit >= 0 && digit <= 9) {  
(8)             if (count == 0)  
(9)                 checkdigit = digit;  
(10)            if (count > 0)  
(11)                checksum += count * digit;  
(12)  
(13)            count ++;  
(14)        }  
(15)    }  
(16)
```

```
(17)     if (count >= 4)  
(18)         if (count <= 10)  
(19)             if (checksum % 10 == checkdigit)  
(20)                 return 0;  
(21)             else return 1;  
(22)         else return 2;  
(23)     else return 3;  
(24) }
```

Target

Code of interest





EXAMPLE OF HOW TO APPLY THE FUNCTION  $\delta$  ON SOME PREDICATES.  $k$  CAN BE ANY ARBITRARY POSITIVE CONSTANT VALUE.  $A$  AND  $B$  CAN BE ANY ARBITRARY EXPRESSION, WHEREAS  $a$  AND  $b$  ARE THE ACTUAL VALUES OF THESE EXPRESSIONS BASED ON THE VALUES IN THE INPUT SET  $I$ .

Predicate $\theta$	Function $\delta_{\theta}(I)$
$A$	if $a$ is TRUE then 0 else $k$
$A = B$	if $abs(a - b) = 0$ then 0 else $abs(a - b) + k$
$A \neq B$	if $abs(a - b) \neq 0$ then 0 else $k$
$A < B$	if $a - b < 0$ then 0 else $(a - b) + k$
$A \leq B$	if $a - b \leq 0$ then 0 else $(a - b) + k$
$A > B$	$\delta_{B < A}(I)$
$A \geq B$	$\delta_{B \leq A}(I)$
$\neg A$	Negation is moved inward and propagated over $A$
$A \wedge B$	$\delta_A(I) + \delta_B(I)$
$A \vee B$	$min(\delta_A(I), \delta_B(I))$

$\delta$  = branch  
distance: how  
distant is the input  $I$   
to the value that makes  
the predicate  $\theta$  TRUE

# Exercise

```
[1] int foo (int a, int b, int c, int d, float e) {  
[2]   if (a == 0) {  
[3]       return 0;  
[4]   }  
[5]   int x = 0;  
[6]   if ( (a==b) || ( (c == d) && bug(a) ) ) {  
[7]       x=1;  
[8]   }  
[9]   e = 1/x;  
[10]  return e;  
[11]}
```

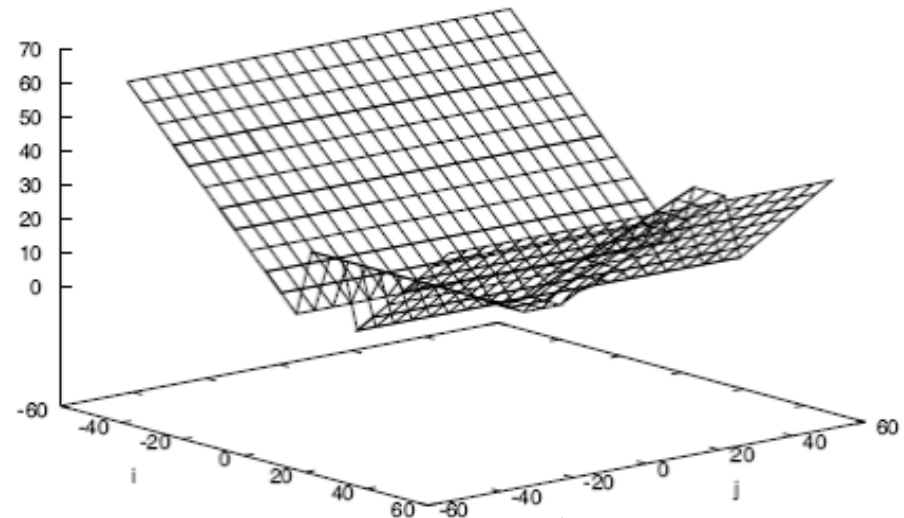
bug(a) = TRUE if !a==0 else 0

How many control nodes does  $T(0,0,0,0,0)$  execute if the target node is the output of the true branch of predicate at line [6]? Approach distance? Branch distance of  $(1,0,0,0,0)$

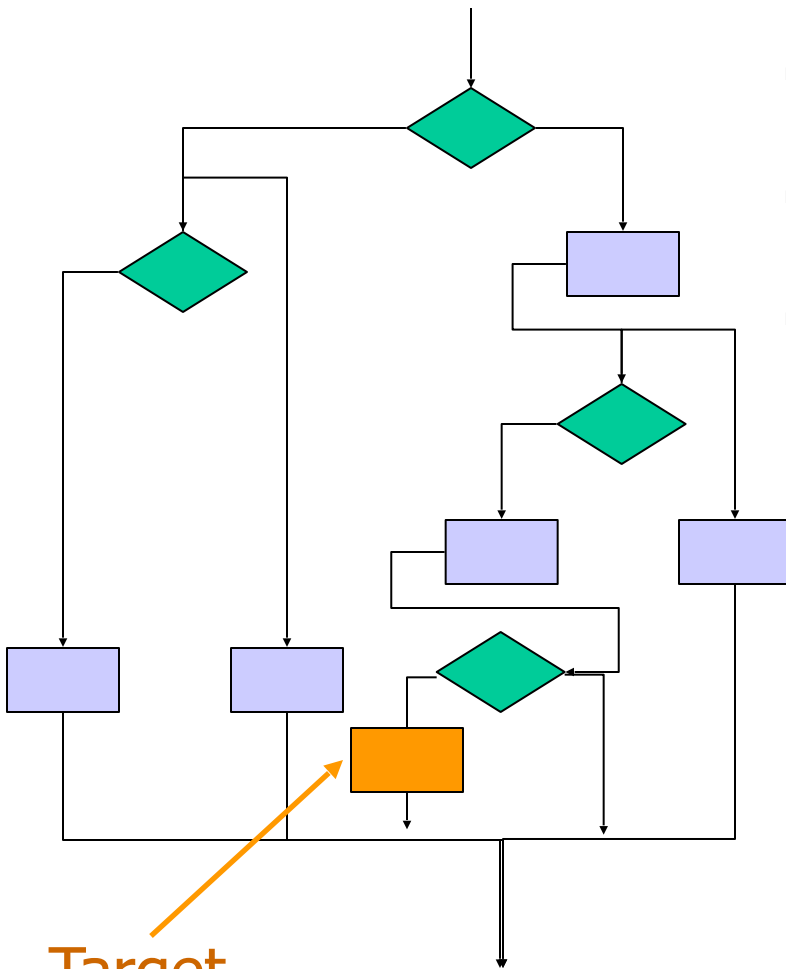
# Distance-Oriented

- Identify **relevant branching** statements from the CFG
- **Approximation level:** distance from the target
- **branch\_distance:** condition distance when a critical node is taken
- **Objective function:**

$$\frac{\text{executed}}{\text{dependent}} \times \text{branch\_distance}$$



Fitness landscape

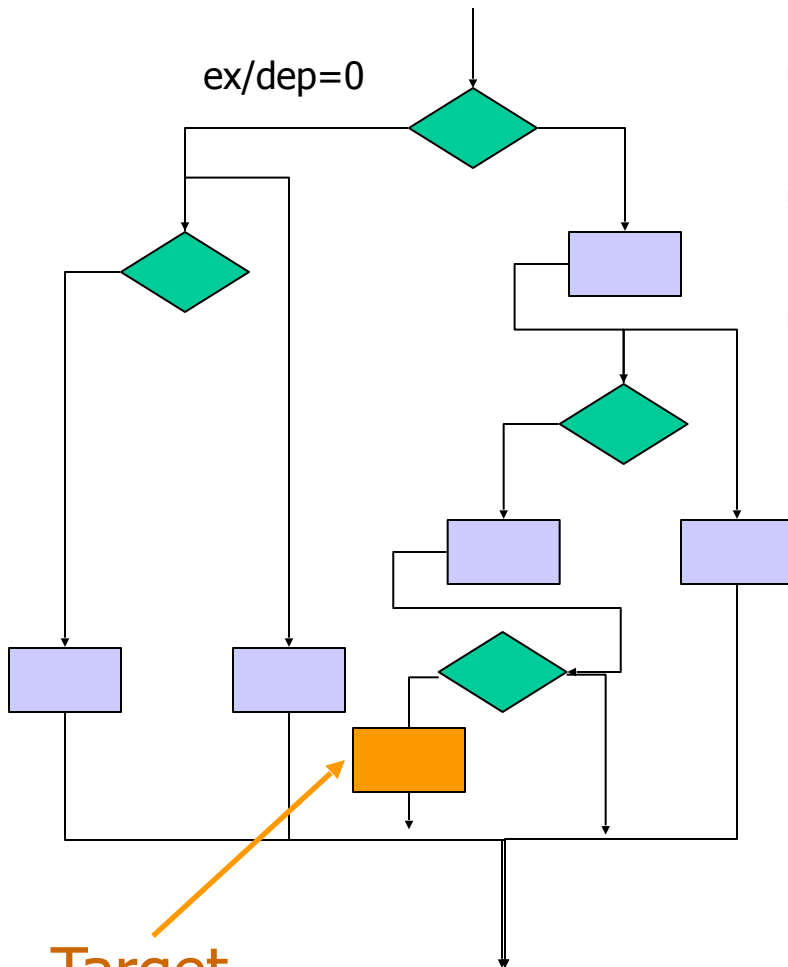
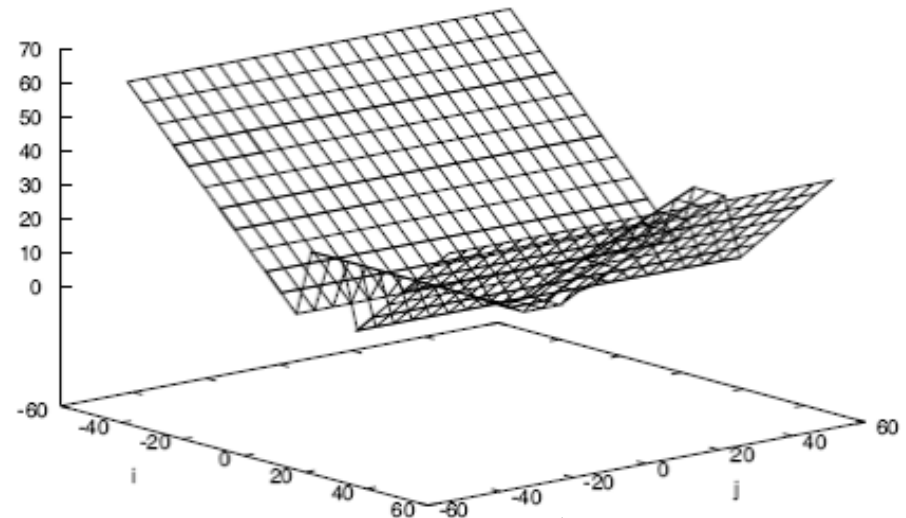


Target

# Distance-Oriented

- Identify **relevant branching** statements from the CFG
- **Approximation level:** distance from the target
- **branch\_distance:** condition distance when a critical node is taken
- **Objective function:**

$$\frac{\text{executed}}{\text{dependent}} \times \text{branch\_distance}$$

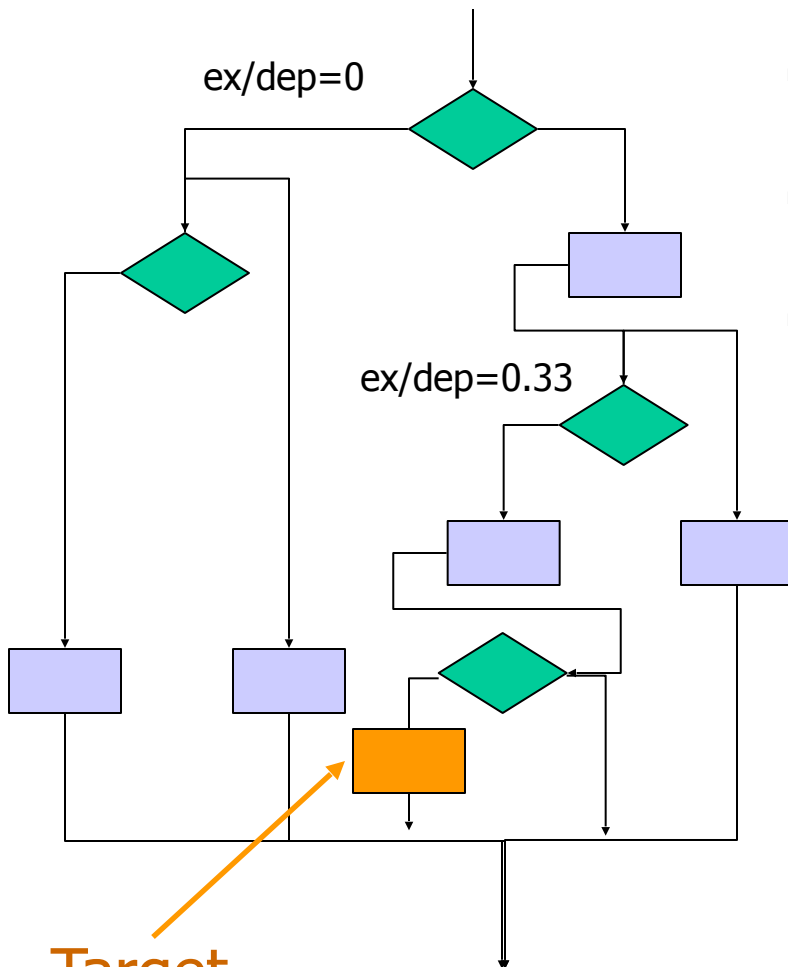
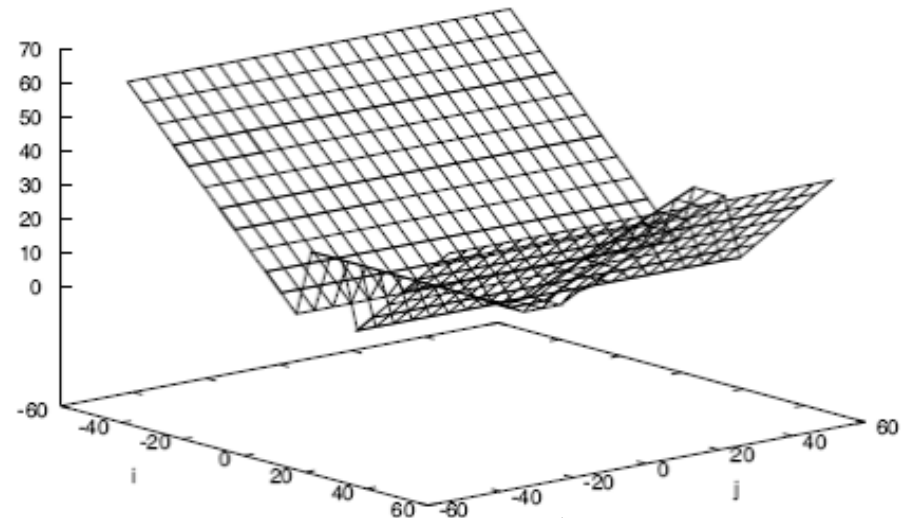


Target

# Distance-Oriented

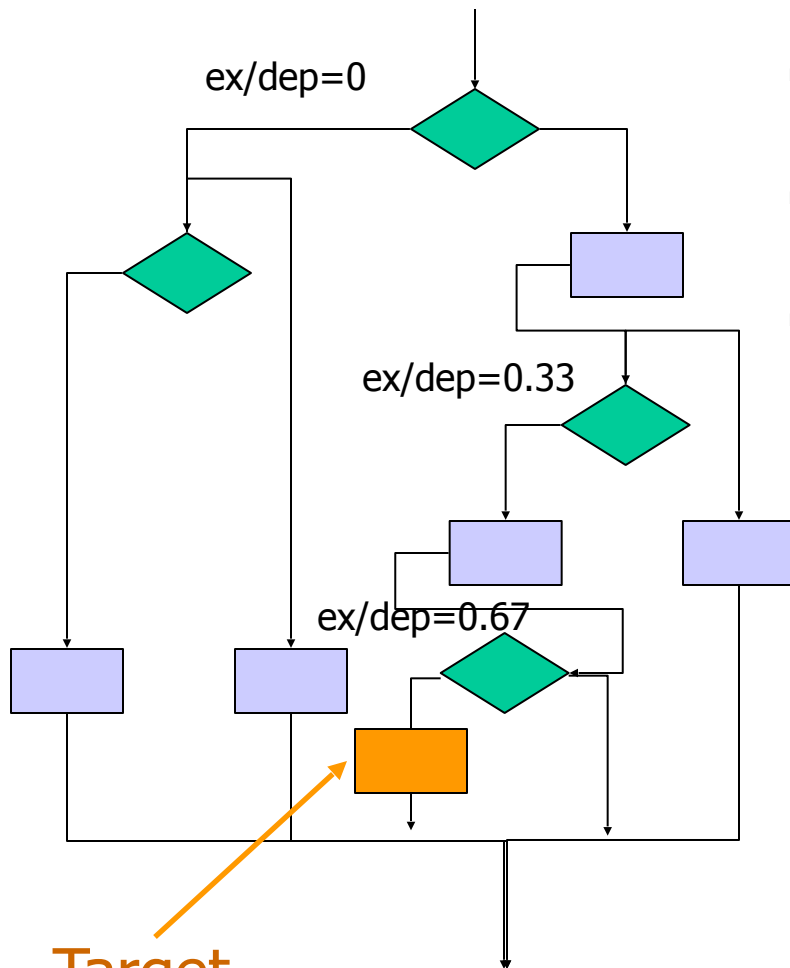
- Identify **relevant branching** statements from the CFG
- **Approximation level:** distance from the target
- **branch\_distance:** condition distance when a critical node is taken
- **Objective function:**

$$\frac{\text{executed}}{\text{dependent}} \times \text{branch\_distance}$$



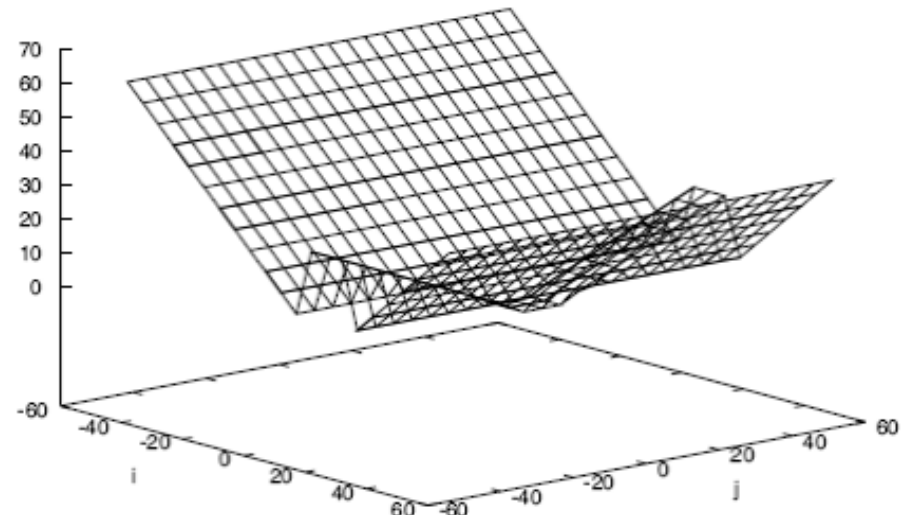
Target

# Distance-Oriented



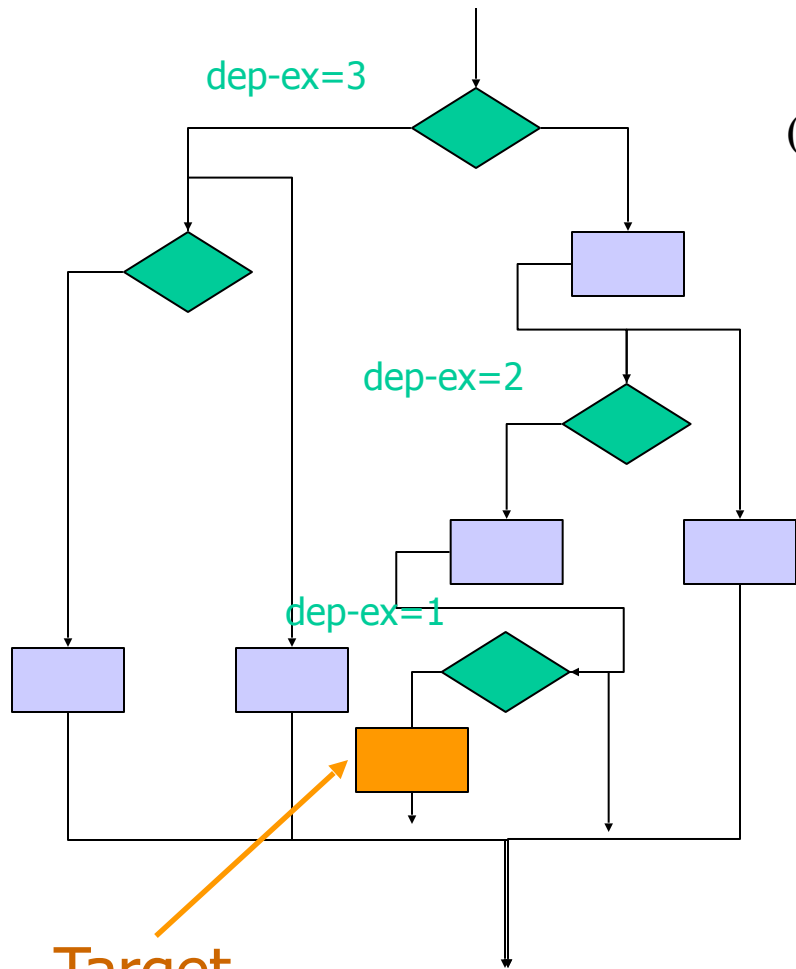
- Identify **relevant branching** statements from the CFG
- **Approximation level:** distance from the target
- **branch\_distance:** condition distance when a critical node is taken
- **Objective function:**

$$\frac{\text{executed}}{\text{dependent}} \times \text{branch\_distance}$$



Fitness landscape

# Distance-Oriented [Wegener]

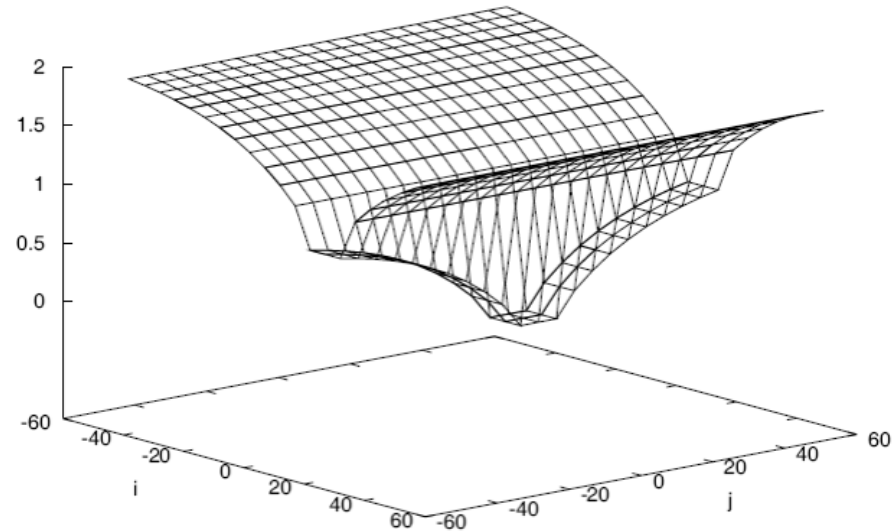


Target

- Objective function:

$(\text{dependent} - \text{executed} - 1) + m\_branch\_distance$

- $m\_branch\_distance$ :  
branch\_distance normalized in the interval [0,1]



# Multi-objective search

---

Barbara Russo

SwSE - Software and Systems Engineering

---



# Objectives of the search

- Optimization means search in the space to minimize or maximize one or more fitness functions
  - Objective of the search can be single or multiple

# Objective function

considering a  
minimization  
scenario

- Formally, it can be expressed as:

$$\operatorname{argmin}\{f_1(x); f_2(x); \dots; f_m(x)\}$$

- where  $m$  is the number of objectives and  $x$  is a solution in the feasible solution space  $X$ , i.e.,  $x \in X \subset R^n$  ( $n$  is the number of decision variables of the problem)

# Solutions

- Two components of a search algorithm:
  - The representation, i.e., how  $x$  can be structured and changed
  - The objective function, i.e., how each single  $f_i$  can be formulated to distinguish between the good and bad solutions
- A solution  $x_1$  dominates  $x_2$  if and only if  $x_1$  is **not worse than  $x_2$  for all the objectives and better for at least one objective**

# Pareto front with multiple objectives

- For a solution  $x \in X$ , if there is no solution in  $X$  dominating  $x$ , then  $x$  is **Pareto optimal**
- **Pareto optimal set**: the set of all Pareto optimal solutions
  - Its image in the objective space is the **Pareto front**

# Search budget

- **Budget:** number of evaluations and time
- **Reasonable convergence:** the best solution found does not change for some number of iterations under a search budget

# Pareto search

- Goal: to search for a set of solutions that can well represent the Pareto front
- Widely used with population-based algorithms (e.g., evolutionary algorithms)

- Examples

- **NSGA-II**: Pareto dominance relation

K. Deb, A. Pratap, S. Agarwal, and T. Meyarivan, "A fast and elitist multiobjective genetic algorithm: Nsga-ii," *IEEE Transactions on Evolutionary Computation*, vol. 6, no. 2, pp. 182-197, 2002.

- As long as they assume no clear preferences exist and seek to approximate the Pareto front:
  - **MOEA/D**: in combination with multiple weight vectors are used;
  - **AdaW** : with weights that are changed during the search
  - **IBEA** : a single dominance-preserving indicator
  - **NGA**: most used in requirements prioritization

D. E. Goldberg, *Genetic algorithms*. Pearson Education India, 2006.

# Weighted search

- Goal: convert the problem into a single-objective one through aggregating the objective functions
- For example, given a weight vector  $[w_1, w_2, \dots, w_m]$  the multi-objective problem can be converted into finding the best fitness of a weighted sum:

$$\operatorname{argmin}\{w_1 f_1(x) + w_2 f_2(x) + \dots + w_m f_m(x)\}$$

# Preference

- Weights can be unbalanced
- For instance: “the project profit is three times more important than the cost”, the weight for the profit and cost objectives can thus be 0.75 and 0.25, respectively

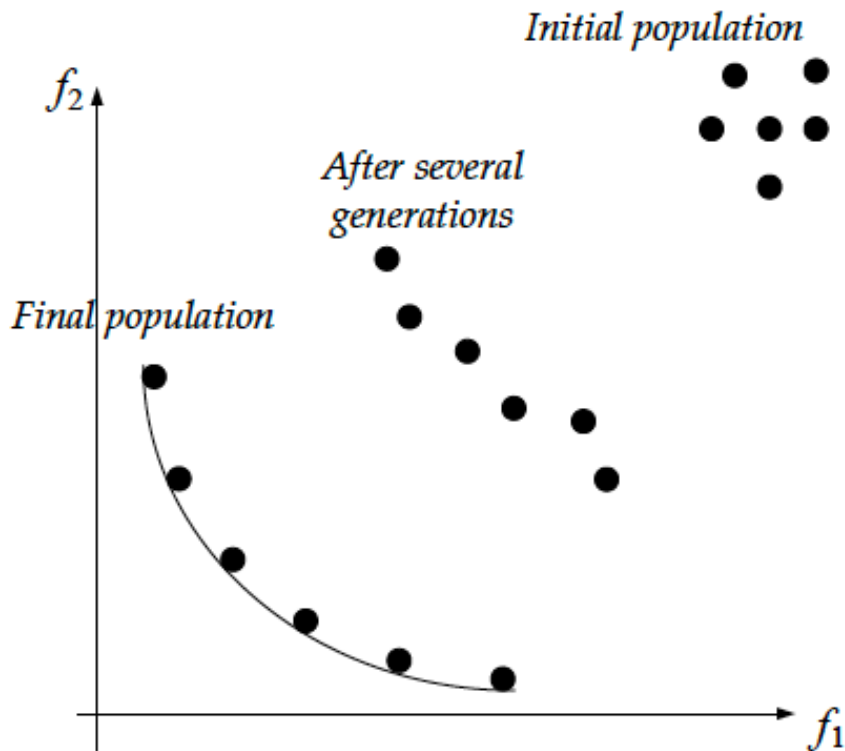


# Quantify objectives of the search

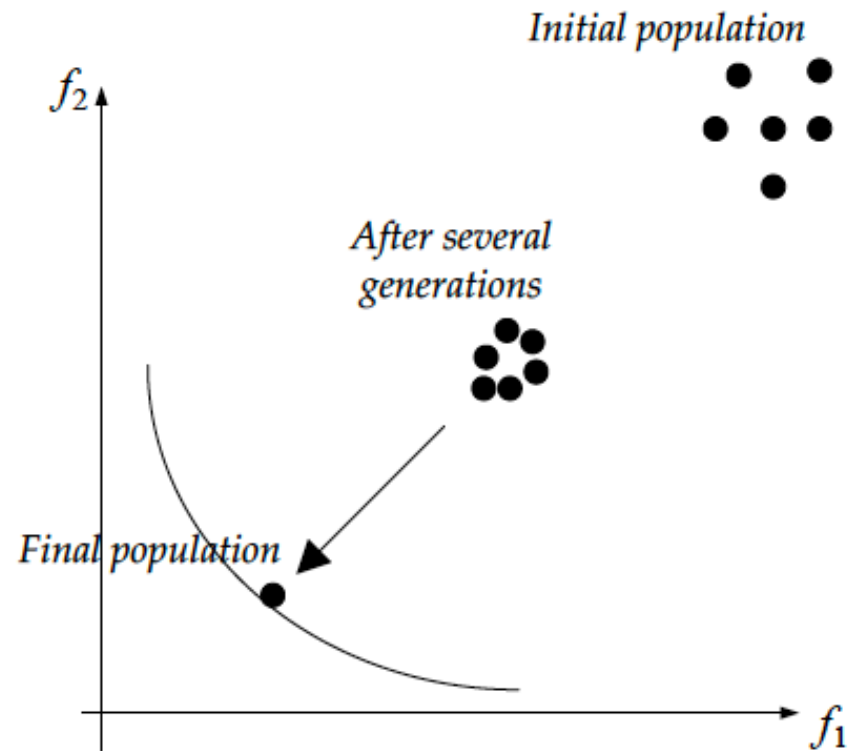
- The objectives to be optimized must be used directly to assess the quality of a search algorithm for the SBSE problem
- For example, a higher testing coverage (a search objective) may not necessarily detect more bugs

# Search process

- bi-objective minimization scenario



(a) Pareto search



(b) Weighted search